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Working group report: High energy and collider physics

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Abstract. This is a summary of the projects undertaken by the working group I on high energy and collider physics.

Keywords. Higgs search; supersymmetry; extra dimensions; linear collider.

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The projects undertaken in the working group I on high energy and collider physics can be classified into (i) Higgs searches, (ii) supersymmetry searches, (iii) extra dimensions and (iv) linear collider. The reports on the projects are given below under these headings.

1. Higgs searches

1.1 Potential of associated Higgs production in LHC through τ -pair mode

P Agarwal and K Mazumdar

At LHC, the standard model Higgs production in association with W-boson, $pp \to WH$ is very interesting, though in general the total production rate is dominated by gluon–gluon fusion process. There is a strong indication that the Higgs boson is not very heavy and the experimental search for Higgs mass, $m_{\rm H} \leq 150~{\rm GeV/c^2}$ is comparatively more difficult. In any case it is desirable to study all possibilities for detection of Higgs boson in this mass range to strengthen the significance of discovery via 'golden' modes. This has motivated us to probe less studied modes of Higgs boson decays via WH production. Once the Higgs boson is discovered at LHC these final states will have to be studied for confirmation anyway.

The LHC experiments, both CMS and ATLAS, have special trigger algorithm at the first level (LEVEL 1) based on calorimetric information for selecting hadronic decays of τ in the final state [1]. The τ -decay modes of supersymmetric Higgs bosons have been particularly studied for this purpose. The narrowness of a jet as in the case of hadronic τ -decays has been utilized in discriminating the transverse profile of jets. The tracker information is used at a later stage for decision at a higher level and hence leptonic decays of τ cannot be used for trigger. Of course the leptonic decays of W-boson (only electron and muon final states) can be chosen for trigger in inclusive isolated electron/muon mode. But the background is likely to be overwhelming in that case. Hence we try the possibility of triggering the signal with the τ s from the Higgs decay. This situation can be effectively utilized for the decay mode $H \to \tau^+\tau^-$ in the Higgs boson mass range $m_{\rm H} \leq 140~{\rm GeV/c^2}$ where the branching ratio is not too small, though below 10%.

According to the 'trigger menu' of CMS experiment there are two possibilities for events with at least one τ in the final state. For 95% efficiency of signal selection (SUSY Higgs decay to τ final state) the kinematic thresholds are as follows:

- 1. Inclusive τ -jet with jet transverse energy ≥ 86 GeV.
- 2. Double τ -jets with the transverse energy of each jet ≥ 59 GeV.

It remains to be checked through simulation the efficiency in the signal channel after these requirements. We need to study the spectrum of transverse momenta of the τ -jets for this.

Assuming that a reasonable fraction of events survive the trigger condition, we need to reconstruct the events. Since the τ -decays will inherently be accompanied by missing energy due to the neutrinos, we choose to select the hadronic decays of W-boson. The W mass can be reconstructed from the jets not identified as τ -tagged. Since the τ s are highly boosted, the neutrinos are expected to be almost

collinear with the direction of missing transverse energy. The mass of the Higgs boson can be reconstructed from this missing transverse energy and the visible momenta of the τ -jets.

The main SM background to this channel is WZ production with $Z \to \tau^+\tau^-$ and $W \to 2$ -jets. Discarding events for which the τ -pair invariant mass is within the Z-mass window, a good fraction of the background can be removed. We plan to make a study after detector simulation to evaluate the signal-to-background ratio. But the Higgs boson being a scalar as opposed to Z, some angular correlations between the τ -jets can be utilized. This may not be as easy as in the case with leptons of course and we plan to make a simulation study of this.

1.2 Probing the light Higgs window via charged Higgs decay at LHC in CP-violating MSSM

K Assamagan, Dilip Kumar Ghosh, Rohini M Godbole and D P Roy

It is well-known that all the observed CP violation in high energy physics can be accommodated in the CKM picture in terms of a single CP-violating phase. Unfortunately this amount of CP violation in the quark sector is not sufficient to explain quantitatively the observed baryon asymmetry in the universe. CP violation in the Higgs sector is a popular extension of the standard model, which can cure this deficiency. Of course, CP violation in the Higgs sector is possible only in multi-Higgs doublet models, such as a general two Higgs doublet model (2HDM) or the MSSM. MSSM with complex phases in the μ term and soft trilinear SUSY breaking parameters $A_{\rm t}$ (and $A_{\rm b}$), can have CP violation in the Higgs sector even with a CP-conserving tree-level scalar potential. In the presence of these phases, due to the CP-violating interactions of the Higgs boson with top and bottom squarks, the one-loop corrected scalar potential will in general have non-zero off-diagonal entries mixing the CP-even (S) and CP-odd (P) states, \mathcal{M}_{SP}^2 , in the 3 × 3 neutral Higgs mass-squared matrix. After diagonalising this one-loop corrected scalar potential one will then, in general, have three neutral Higgs boson eigenstates, denoted by H_1, H_2 and H_3 in ascending order of masses, with mixed CP parities [2-7]. Sizeable scalar-pseudoscalar mixing is possible for large $|\mu|$ and $|A_t|$ (> $M_{\rm SUSY}$). Such CPviolating phases can cause the Higgs couplings to fermions and gauge bosons to change significantly from their values at the tree-level [3,5,6].

Recently the OPAL Collaboration [8] has reported their results for the Higgs boson searches in the CP-violating MSSM Higgs sector using the parameters defined in the CPX scenario [6] using the CP-SuperH [9] as well as the FeynHiggs 2.0 [10]. They have provided exclusion regions in the $M_{\rm H_1}$ -tan β plane for different values of the CP-violating phases, assuming ${\rm arg}A_{\rm t}={\rm arg}A_{\rm b}={\rm arg}M_{\tilde g}=\Phi_{\rm CP},$ with $\Phi_{\rm CP}=90^\circ,60^\circ,30^\circ$ and 0° . The values of the various parameters in the CPX scenario are chosen so as to showcase the effects of CP violation in the Higgs sector of the MSSM. Combining the results of Higgs searches from ALEPH, DELPHI, L3 and OPAL, the authors in ref. [11] have also provided exclusion regions in the $M_{\rm H_1}$ -tan β plane as well as $M_{\rm H^+}$ -tan β plane for the above set of parameters.

Both these analyses show that for phases $\Phi_{\rm CP}=90^\circ$ and 60° , LEP cannot exclude the presence of a light Higgs boson for $\tan\beta\sim 4$ –5, $M_{\rm H^\pm}\sim 125$ –140 GeV, $M_{\rm H_1}\lesssim 60$ GeV, $\tan\beta\sim 2$ –3, $M_{\rm H^\pm}\sim 105$ –130 GeV, $M_{\rm H_1}\lesssim 40$ GeV respectively.

This happens mainly due to the reduced H_1ZZ coupling, as the lightest Higgs H_1 is mostly a pseudoscalar. In the same region the $H_1t\bar{t}$ coupling is suppressed as well. As a result this particular region in the parameter space cannot be probed neither at the Tevatron where the associated production, W/ZH_1 mode, is the most promising one; nor can it be probed at the LHC as the reduced $t\bar{t}H_1$ coupling suppresses the inclusive production mode and the associated production modes W/ZH_1 and $t\bar{t}H_1$, are suppressed as well.

It is interesting to note that in the same parameter space where H_1ZZ coupling is suppressed, $H^+W^-H_1$ coupling is enhanced because these two sets of couplings satisfy a sum-rule [9]. We have found that in these regions of parameter space, $H^{\pm} \to H_1W^{\pm}$ has a very large (~100%) branching ratio. This feature motivated us to study the possibility of probing such a light Higgs scenario in CP-violating MSSM Higgs model through the process $pp \to t\bar{t} \to (bW^{\pm})(bH^{\mp}) \to (b\ell\nu)(bH_1W) \to (b\ell\nu)(bb\bar{b})(jj)$ at LHC. Thus signal will consist of three or more b-tagged and two untagged jets along with a hard lepton and missing p_T . Similar studies have been done in the context of charged Higgs search in NMSSSM model [12].

We report results obtained from a parton level Monte Carlo. We merge two partons into a single jet if the separation $\Delta R = \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2} < 0.4$. As a basic selection criteria we require:

- 1. $|\eta| < 2.5$ for all jets and leptons, where η denotes pseudo-rapidity,
- 2. $p_{\rm T}$ of the hardest three jets to be higher than 30 GeV,
- 3. $p_{\rm T}$ of all the other jets, lepton, as well as the missing $p_{\rm T}$ to be larger than 20 GeV,
- 4. a minimum separation of $\Delta R = 0.4$ between the lepton and jets as well as each pair of jets,
- 5. three or more tagged b-jets in the final state assuming a b-tagging efficiency of 50%.

In figure 1 we show the variation of signal cross-section with $M_{\rm H^+}$ and $M_{\rm H_1}$ for the CP-violating phase $\Phi_{\rm CP}=60^\circ$. We have used the CP-SuperH program [9] to calculate the masses and the couplings of the Higgses in the CPX scenario. The cross-section shown in the figure includes neither the b-tagging efficiency for the three and more jets (5/16), nor the K-factor corresponding to the NLO QCD corrections for the $t\bar{t}$ production (\sim 1.4–1.5). Hence the numbers in the figure need to be scaled down by roughly a factor of two to get the signal cross-section. From figure 1 one can see that the signal cross-section decreases with increase in $\tan \beta$. This can be explained by the fact that $H^+ \to H_1 W^+$ as well as $t \to b H^+$ branching ratios decrease with the increase in $\tan \beta$. The $t \to b H^+$ branching ratio does increase after showing a dip around $\tan \beta \sim 5$ –6. However, we are not interested in such a high value of $\tan \beta$ in the present investigation as the loss of light Higgs signal due to \mathcal{P} in the Higgs sector is not significant for these higher values of $\tan \beta$.

Note that the signal events will be very striking due to the clustering of the $b\bar{b}$, $b\bar{b}W$ invariant masses at values corresponding to $M_{\rm H_1}$ and $M_{\rm H^+}$ respectively. Also the signal events will have simultaneous clustering of $b\bar{b}bW$ invariant mass around $m_{\rm t}$. In figure 2 we show in the left panel the three-dimensional plot for the correlation between $m_{b\bar{b}}$ and $m_{b\bar{b}W}$ invariant mass distribution for $\Phi_{\rm CP}=60^\circ$, $\tan\beta=3$

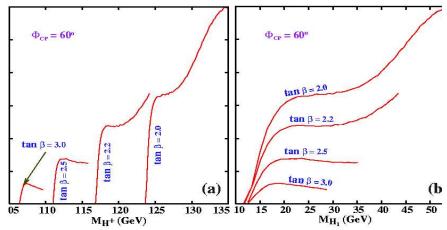


Figure 1. Variation of signal cross-section with $M_{\rm H^+}$ (a) and $M_{\rm H_1}$ (b) for the CP-violating phase $\Phi_{\rm CP}=60^\circ$.

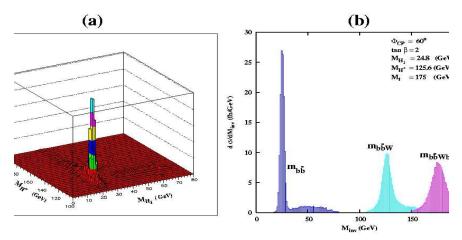


Figure 2. Clustering of the $b\bar{b}$, $b\bar{b}W$ and $\bar{b}bbW$ invariant masses around $M_{\rm H_1}$, $M_{\rm H^+}$ and $m_{\rm t}$. The parameters chosen for the signal are: CP-violating phase $\Phi_{\rm CP}=60^\circ$, $\tan\beta=3$ and $M_{\rm H^+}=107$ GeV.

and $M_{\rm H^+}=107$ GeV. The light Higgs mass corresponding to this set of input parameter is 16.78 GeV. It is clear from figure 2 that there is clustering at $M_{\rm H_1}\equiv m_{b\bar b}$ and $M_{\rm H^+}\equiv m_{b\bar bW}$. The right panel of the figure shows the same, in terms of cross-section distribution in $b\bar b$, $\bar bbW$ and $\bar bbbW$ invariant masses for the signal. This makes it very clear that the detectability of the signal is clearly controlled only by the signal size. It is clear from figure 1 that indeed the signal size is healthy over the regions of interest in the parameter space. The clustering feature can be used to distinguish the signal over the standard model background. Thus using this process one can cover, at the LHC, a region of the parameter space in $\mathcal{Q}P$ MSSM in the $\tan \beta - M_{H_1}$ plane which cannot be excluded by LEP-2, where the Tevatron has no reach and which the LHC also cannot probe if one does not use the process

under discussion [13]. Of course, in view of the jetty final state, a more rigorous experimental simulation, including detector effects and hadronisation, will be useful to add further to the strength of our observation. Such a simulation is in progress and the results will be presented elsewhere.

2. Supersymmetry searches

2.1 Fermion polarization in sfermion decays as a probe of CP phases in the MSSM

Thomas Gajdosik, Rohini M Godbole and Sabine Kraml

Introduction: CP violation is one feature of the SM that still defies a fundamental theoretical understanding, even though all the observed CP violation in high energy physics can be accommodated in the CKM picture in terms of a single CP-violating phase. However, this amount of CP violation in the quark sector is not sufficient to explain quantitatively the observed baryon asymmetry in the universe. CP violation in the Higgs sector is a popular extension of the standard model, which might cure this deficiency. MSSM with complex phases in the μ term and soft trilinear SUSY breaking parameters A_t (and A_b), can affect the Higgs sector [14,15] through loop corrections. One can then have CP-violating effects even with a CP-conserving treelevel scalar potential. It is still possible to be consistent with the non-observation of the electron EDMs (eEDM). This makes the MSSM with CP-violating phases a very attractive proposition. It has therefore been the subject of many recent investigations, studying the implications of these phases on neutralino/chargino production and decay [16], on the third generation of sfermions [17] as well as the neutral [15,18] and charged [19] Higgs sector. In these studies, the gaugino mass parmaeter M_1 is also taken to be complex in addition to the non-zero phases mentioned above. It is interesting to note that CP-even observables such as masses, branching ratios, cross-sections, etc., often afford more precise probes of these phases, thanks to the larger magnitudes of the effects as compared to the CP-odd/T-odd observables. The latter, however, are the only ones that can offer direct evidence of CP violation [16]. A recent summary of the progress in the area can be found in [20,21] and references therein.

In this project, we address the issue of probes of these phases through a study of the third generation sfermions. A recent study in this context, in the \tilde{t}, \tilde{b} sector in the second part of ref. [17], demonstrates that it may be possible to determine the real and imaginary parts of $A_{\rm t}(A_\tau)$ to a precision of 2–3% (10–20% for low $\tan\beta$ and 3–7% for large $\tan\beta$) from a fit of the MSSM Lagrange parameters to masses, cross-sections and branching ratios at a future LC. In this project [21] we have explored the longitudinal polarization of fermions produced in sfermion decays, i.e. $\tilde{f} \to f\tilde{\chi}^0$ and $\tilde{f} \to f'\tilde{\chi}^\pm$ with $f(\tilde{f})$ a third generation (s)quark or (s)lepton, as a probe of CP phases.

The average polarization of fermions produced in sfermion decays carries information on the $\tilde{f}_{\rm L}$ – $\tilde{f}_{\rm R}$ mixing as well as on the gaugino–higgsino mixing [22]. The polarizations that can be measured are those of top and tau; both can be inferred from the decay product (lepton angle and/or pion energy) distributions. The use

of polarization of the decay fermions for studies of MSSM parameter determination was first pointed out and demonstrated in refs [22,23]. An extension of these ideas for the CP-violating case and the phase dependence of the longitudinal fermion polarization had been mentioned in the studies of [20]. We provide, in this note, a detailed discussion of the sensitivity of the fermion polarization to the CP-violating phases in the MSSM.

Fermion polarization in $\tilde{f} \to f \tilde{\chi}^0$ decays: The sfermion interaction with neutralinos is (i=1,2; n=1,...,4)

$$\mathcal{L}_{f\tilde{f}\tilde{\chi}^0} = g\,\bar{f}\,(a_{in}^{\tilde{f}}P_{\mathrm{R}} + b_{in}^{\tilde{f}}P_{\mathrm{L}})\,\tilde{\chi}_n^0\,\tilde{f}_i + \text{h.c.}$$
(1)

Thus $a_{in}^{\tilde{f}}(b_{in}^{\tilde{f}})$ determine the amplitude for the production of $f_{\rm L}(f_{\rm R})$ in the decay $\tilde{f}_i \to f \tilde{\chi}_n^0$. The gaugino interaction conserves the helicity of the sfermion while the higgsino interaction flips it. In the limit $m_f \ll m_{\tilde{f}_i}$, the average polarization of the fermion coming from the above decay can therefore be calculated as [22]

$$\mathcal{P}_{f} = \frac{\text{Br}(\tilde{f}_{i} \to \tilde{\chi}_{n}^{0} f_{R}) - \text{Br}(\tilde{f}_{i} \to \tilde{\chi}_{n}^{0} f_{L})}{\text{Br}(\tilde{f}_{i} \to \tilde{\chi}_{n}^{0} f_{R}) + \text{Br}(\tilde{f}_{i} \to \tilde{\chi}_{n}^{0} f_{L})} = \frac{|b_{in}^{\tilde{f}}|^{2} - |a_{in}^{\tilde{f}}|^{2}}{|b_{in}^{\tilde{f}}|^{2} + |a_{in}^{\tilde{f}}|^{2}}.$$
 (2)

We obtain for the $\tilde{f}_1 \to f \tilde{\chi}_n^0$ decay (omitting the overall factor g^2 and dropping the sfermion and neutralino indices for simplicity):

$$\begin{split} |b_{1n}|^2 - |a_{1n}|^2 &= |h_{\rm L}\cos\theta\,\mathrm{e}^{-i\varphi} + f_{\rm R}\sin\theta|^2 \\ - |f_{\rm L}\cos\theta\,\mathrm{e}^{-i\varphi} + h_{\rm L}^*\sin\theta|^2 \\ &= (|h_{\rm L}|^2 - |f_{\rm L}|^2)\cos^2\theta - (|h_{\rm L}|^2 - |f_{\rm R}|^2)\sin^2\theta \\ &+ \sin2\theta\,\big[\mathcal{R}e\,(f_{\rm R} - f_{\rm L})\,(\mathcal{R}e\,h_{\rm L}\cos\varphi + \mathcal{I}m\,h_{\rm L}\sin\varphi) \\ &+ \mathcal{I}m\,(f_{\rm R} + f_{\rm L})\,(\mathcal{I}m\,h_{\rm L}\cos\varphi - \mathcal{R}e\,h_{\rm L}\sin\varphi)\big], \end{split} \tag{3}$$

where θ, φ are the sfermion mixing angle and phase, and $f_{\rm L}, f_{\rm R}$ and $h_{\rm L}, h_{\rm R}$ are the gaugino and higgsino couplings of the left- and right-chiral sfermions respectively (for details see [21]) and contain the dependence on the phases in the gaugino-higgsino sector, ϕ_1, ϕ_μ . We see that the phase dependence of \mathcal{P}_f is the largest for maximal sfermion mixing ($\theta_{\tilde{f}} = 3\pi/4$) and if the neutralino has both sizeable gaugino and higgsino components. It is, moreover, enhanced if the Yukawa coupling h_f is large. Furthermore, \mathcal{P}_f is sensitive to CP violation even if just one phase, in either the neutralino or the sfermion sector, is non-zero. In particular, if only A_f and thus only the sfermion mixing matrix has a non-zero phase, the phase-dependent term becomes

$$|b_{1n}|^2 - |a_{1n}|^2 \stackrel{\phi_1 = \phi_\mu = 0}{\sim} h_{\rm L}(f_{\rm L} - f_{\rm R}) \sin 2\theta \cos \varphi$$
. (4)

The polarization \mathcal{P}_f (eq. (2)), depends only on couplings but not on masses. For the numerical analysis we therefore use M_1 , M_2 , μ , $\tan \beta$, $\theta_{\tilde{f}}$ and $\varphi_{\tilde{f}}$ as input parameters, assuming $\phi_{\mu} \approx 0$ to satisfy EDM constraints more easily: assuming

cancellations for the 1-loop contributions and the CP-odd Higgs mass parameter $m_A > 300 \text{ GeV}$, 1-loop and 2-loop contributions to the electron EDM (eEDM), as well as their sum, stay below the experimental limit [21,24]. In order not to vary too many parameters, we use, moreover, the GUT relation $|M_1| = \frac{5}{3} \tan^2 \theta_W M_2$ and choose $\tan\beta=10$ and $\theta_{\tilde{t}}=\theta_{\tilde{\tau}}=130^{\circ};$ i.e., large but not maximal mixing. The free parameters in this analysis are thus M_2 , $|\mu|$, and the phases ϕ_1 , $\varphi_{\tilde{f}}$. Figure 3 shows the average τ polarization in $\tilde{\tau}_1 \to \tau \tilde{\chi}_1^0$ decays as functions of M_2 and $|\mu|$, for values consistent with the LEP constraints, for $\tan \beta = 10$, $\theta_{\tilde{\tau}} = 130^{\circ}$ and various choices of ϕ_1 and $\varphi_{\tilde{\tau}}$. We find that \mathcal{P}_{τ} is quite sensitive to CP phases for $|\mu| < M_2$, when $\tilde{\chi}_1^0$ has a sizeable higgsino component. Similarly the average top polarization in $t_1 \to t \tilde{\chi}_1^0$ decays can be studied. We find that not only does it have a strong dependence on the CP phases if the neutralino has a sizeable higgsino component, but it is also significant when $|\mu| \sim M_2$, due to the much larger value of $m_{\rm t}$ compared to m_{τ} . Since one expects a future e^+e^- linear collider (LC) to be able to measure the τ polarization to about 3-5% and the top polarization to about 10% [25], the effects of CP-violating phases may well be visible in \mathcal{P}_t and/or \mathcal{P}_{τ} , provided μ is not too large.

The phase dependence is further studied in figure 4 where we show $\mathcal{P}_{\rm t}$ as a function of ϕ_1 , for $M_2=380$ GeV, $|\mu|=125$ GeV and $\varphi_{\tilde{\rm t}}=0,\,\frac{\pi}{2},\,-\frac{\pi}{2}$ and π . Since for fixed M_2 and $|\mu|$ the $\tilde{\chi}_1^0$ mass changes with ϕ_1 , we show in addition in figure 4b $\mathcal{P}_{\rm t}$ as a function of $\varphi_{\tilde{\rm t}}$ for various values of ϕ_1 , with $|\mu|=125$ GeV and M_2 adjusted such that $m_{\tilde{\chi}_1^0}=100$ GeV. We thus see that if the neutralino mass parameters, $\tan\beta$ and $\theta_{\tilde{\rm t}}$ are known, $\mathcal{P}_{\rm t}$ can hence be used as a sensitive probe of these phases (although additional information will be necessary to resolve ambiguities and actually determine the various phases). The influence of uncertainties in the knowledge of the SUSY model parameters can be studied by choosing the case of $M_2=380$ GeV, $|\mu|=125$ GeV and vanishing phases as reference point and assume that the following precisions can be achieved: $\delta M_1=\delta M_2=\delta\mu=0.5\%$, $\delta \tan\beta=1$, $\delta\theta_{\tilde{\rm t}}=3.5^\circ$, and $\delta\phi_1=\delta\phi_\mu=0.1$. Varying the parameters within this

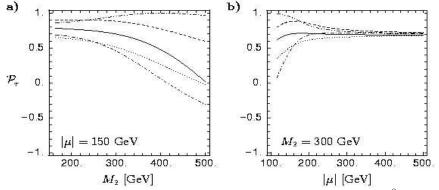


Figure 3. Average polarization of the τ lepton coming from $\tilde{\tau}_1 \to \tau \tilde{\chi}_1^0$ decays in (**a**) as a function of M_2 , in (**b**) as a function of $|\mu|$. The full, dashed, dotted, dash-dotted, and dash-dot-dotted lines are for $(\phi_1, \varphi_{\tilde{\tau}}) = (0, 0), (0, \frac{\pi}{2}), (\frac{\pi}{2}, 0), (\frac{\pi}{2}, \frac{\pi}{2}), \text{ and } (\frac{\pi}{2}, -\frac{\pi}{2}), \text{ respectively. } M_2 \text{ and } \mu \text{ are taken to be real.}$

range around the reference point and adding experimental resolution $\delta \mathcal{P}_t^{\rm exp} \simeq 0.1$ in quadrature gives $\mathcal{P}_t = -0.48 \pm 0.22$ at $\varphi_{\tilde{t}} = 0$, indicated as an error bar in figure 4b. The figure shows that in this scenario \mathcal{P}_t would be sensitive to $|\varphi_{\tilde{t}}| \gtrsim 0.15\pi$. If more accurate measurements of the SUSY parameters should be available such that $\delta \mathcal{P}_t^{\rm par}$ would be negligible compared to the experimental resolution of \mathcal{P}_t , then it would be possible to derive information on A_t using the \mathcal{P}_t measurement.

Fermion polarization in $\tilde{f} \to f' \tilde{\chi}^{\pm}$ decays: Analogous to the decay into a neutralino (eq. (2)), the average polarization of the fermion coming from the $\tilde{f}_i \to f' \tilde{\chi}_j^{\pm}$ decay (i,j=1,2) can be calculated once we know the $\tilde{f}_i f' \tilde{\chi}_j^{\pm}$ coupling. These can be read off from the interaction Lagrangian:

$$\mathcal{L}_{f'\tilde{f}\tilde{\chi}^{\pm}} = g \,\bar{u} \,(l_{ij}^{\tilde{a}} P_{\mathcal{R}} + k_{ij}^{\tilde{a}} P_{\mathcal{L}}) \,\tilde{\chi}_{j}^{+} \,\tilde{d}_{i}
+ g \,\bar{d} \,(l_{ij}^{\tilde{a}} P_{\mathcal{R}} + k_{ij}^{\tilde{a}} P_{\mathcal{L}}) \,\tilde{\chi}_{j}^{+c} \,\tilde{u}_{i} + \text{h.c.},$$
(5)

where u (\tilde{u}) stands for up-type (s)quark and (s)neutrinos, and d (\tilde{d}) stands for down-type (s)quark and charged (s)leptons. The average polarization is then given by

$$\mathcal{P}'_{f} = \frac{\operatorname{Br}(\tilde{f}_{i} \to \tilde{\chi}_{j}^{\pm} f_{R}') - \operatorname{Br}(\tilde{f}_{i} \to \tilde{\chi}_{j}^{\pm} f_{L}')}{\operatorname{Br}(\tilde{f}_{i} \to \tilde{\chi}_{j}^{\pm} f_{R}') + \operatorname{Br}(\tilde{f}_{i} \to \tilde{\chi}_{j}^{\pm} f_{L}')} = \frac{|k_{ij}^{\tilde{f}}|^{2} - |l_{ij}^{\tilde{f}}|^{2}}{|k_{ij}^{\tilde{f}}|^{2} + |l_{ij}^{\tilde{f}}|^{2}}.$$
(6)

Since only top and τ polarizations are measurable, we studied $\tilde{b} \to t\tilde{\chi}^-$ and $\tilde{\nu}_{\tau} \to \tau\tilde{\chi}^+$ decays. The latter case is especially simple because \mathcal{P}'_{τ} depends only on the parameters of the chargino sector: A measurement of \mathcal{P}'_{τ} may hence be useful to supplement the chargino parameter determination. However, only for the decay

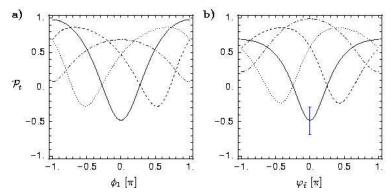


Figure 4. Average polarization of the top quark coming from $\tilde{t}_1 \to t \tilde{\chi}_1^0$ decays for $\theta_t = 130^\circ$, and $\tan \beta = 10$: in (a) as a function of ϕ_1 for $M_2 = 225$ GeV and $|\mu| = 200$ GeV; in (b) as a function of $\varphi_{\tilde{t}}$ for $|\mu| = 200$ GeV and M_2 adjusted such that $m_{\tilde{\chi}_1^0} = 100$ GeV. The full, dashed, dotted, and dash-dotted lines are for $\varphi_{\tilde{t}}$ (ϕ_1) = 0, $\frac{\pi}{2}$, $-\frac{\pi}{2}$, π in (b). The error on \mathcal{P}_t indicated by the vertical bar in (b) has been estimated as described in the text.

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into the heavier chargino, the effect of a non-zero phase may be sizeable. Recall that unless huge cancellations are invoked, ϕ_{μ} is severely restricted by the non-observation of the eEDM. Moreover, the measurement of $(\mathcal{P}'_{\tau})_2$ will be diluted by $\tilde{\nu}_{\tau} \to \tau \tilde{\chi}_1^+$.

The top polarization in $b \to t \tilde{\chi}^-$ decays is more promising. Again we find that the phase dependence of \mathcal{P}'_t is proportional to $h_b \sin 2\theta_{\tilde{b}}$ and the amount of gauginohigsino mixing of the charginos; it will therefore be largest for $|M_2| \sim |\mu|$, $\theta_{\tilde{b}} = 3\pi/4$ and large $\tan \beta$. Again, there is a non-zero effect even if there is just one phase in either the sbottom or chargino sector. Note, however, that the only CP phase in the chargino sector is ϕ_{μ} , which also enters the sfermion mass matrices. As a result, depending on values of A_b , $\tan \beta$ and μ , $\varphi_{\tilde{b}}$ and ϕ_{μ} get related. For the sake of a general discussion of the phase dependence of \mathcal{P}'_t (and since A_b is still a free parameter), we nevertheless use ϕ_{μ} and $\varphi_{\tilde{b}}$ as independent input parameters. If ϕ_{μ} and $\varphi_{\tilde{b}}$ have the same sign, the difference in \mathcal{P}'_t from the case of vanishing phases is larger than if they have opposite signs. In particular, we find $\mathcal{P}'_t(\phi_{\mu} = -\varphi_{\tilde{b}}) \sim \mathcal{P}'_t(\phi_{\mu} = \varphi_{\tilde{b}} = 0)$ over large regions of the parameter space. With an experimental resolution of the top polarization of about 10% this implies that in many cases $\varphi_{\tilde{b}} \sim -\phi_{\mu}$ cannot be distinguished from $\varphi_{\tilde{b}} = \phi_{\mu} = 0$ by measurement of \mathcal{P}'_t .

As an example of the phase dependence of the polarization \mathcal{P}'_t we show some of our results in figure 5 which shows \mathcal{P}'_t as a function of $\varphi_{\tilde{h}}$, for $|\mu|=200$ GeV, $\tan\beta=10$, $\theta_{\tilde{b}} = 140^{\circ}$, and various values of ϕ_{μ} . M_2 is chosen such that $m_{\tilde{\chi}_{\pm}^{\pm}} = 155$ GeV (i.e. $M_2 = 225 \text{ GeV}$ for $\phi_{\mu} = 0$). The range obtained by varying m_b within 2.5–4.5 GeV is shown as grey bands for two of the curves, for $\phi_{\mu} = 0$ and $\phi_{\mu} = -\varphi_{\tilde{b}}$. We estimate the effect of an imperfect knowledge of the model parameters in the same way as in the previous section. For $M_2=225\pm1.125~{\rm GeV}, |\mu|=200\pm1~{\rm GeV}, \tan\beta=10\pm1,$ $\theta_{\tilde{b}} = 140 \pm 3.4^{\circ}$ and $\phi_{\mu} = 0 \pm 0.1$, we get $\mathcal{P}'_{t} = 0.89 \pm 0.06$ at $\varphi_{\tilde{b}} = 0$. Varying in addition $m_b = 2.5$ –4.5 GeV gives $\mathcal{P}_t' = 0.89^{+0.06}_{-0.16}$. Adding a 10% measurement error on \mathcal{P}'_{t} in quadrature, we end up with $\delta \mathcal{P}'_{t} = 0.12$ (0.19) without (with) the m_{b} effect. These are shown as error bars in figure 5. We see that the case of $\varphi_{\tilde{b}} = -\phi_{\mu}$ cannot be distinguished from $\varphi_{\tilde{b}} = \phi_{\mu} = 0$ in this scenario. However, \mathcal{P}'_{t} turns out to be quite a sensitive probe of $\delta_{\phi} = \varphi_{\tilde{b}} + \phi_{\mu}$, i.e. the deviation from the 'natural' alignment $\varphi_{\tilde{b}} = -\phi_{\mu}$. In the example of figure 5, $|\delta_{\phi}| \gtrsim 0.24\pi$ (0.31 π) can be resolved if h_b is (not) known precisely, quite independently of ϕ_{μ} . Observing such a δ_{ϕ} also implies a bound on $|A_b|$ of $|A_b| > 1363$ (1678) GeV. If the precision on M_2 and $|\mu|$ is 0.1% and $\tan \beta = 10 \pm 0.1$, we get $(\delta \mathcal{P}_t')^{\text{par}} = 0.03$ at $\varphi_{\tilde{b}} = 0$, so that the error is dominated by the experimental uncertainty. However, the resultant improvement in the sensitivity is limited to $|\delta_{\phi}| \gtrsim 0.22\pi$ and $|A_b| > 1294$ GeV.

Summary: We have investigated the sensitivity of the longitudinal polarization of fermions (top and tau) produced in sfermion decays to CP-violating phases in the MSSM. We have found that both \mathcal{P}_t and \mathcal{P}_τ can vary over a large range depending on ϕ_1 and $\varphi_{\tilde{t},\tilde{\tau}}$ (and also ϕ_μ , though we did not discuss this case explicitly) and may thus be used as sensitive probes of these phases. To this aim, however, the neutralino mass parameters, $\tan \beta$ and the sfermion mixing angles need to be known with high precision. Given the complexity of the problem, a combined fit of all available data seems to be the most convenient method for the extraction of the

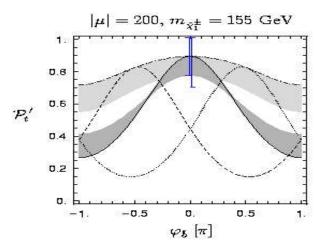


Figure 5. Average polarization of the top quark coming from $b_1 \to t\tilde{\chi}_1^-$ decays as a function of $\varphi_{\tilde{b}}$. The full, dashed and dotted lines are for $\phi_{\mu} = 0$, $\frac{\pi}{2}$ and $-\frac{\pi}{2}$, respectively, while for the dash-dotted lines $\phi_{\mu} = -\varphi_{\tilde{b}}$. The grey bands show the range of \mathcal{P}'_{t} due to varying m_b within 2.5–4.5 GeV for the cases $\phi_{\mu} = 0$ and $\phi_{\mu} = -\varphi_{\tilde{b}}$. The error bars show the estimated errors on \mathcal{P}'_{t} as described in the text.

MSSM parameters. For the decays into charginos, the τ polarization in $\tilde{\nu}_{\tau} \to \tau \tilde{\chi}^+$ decays depends only little on ϕ_{μ} . \mathcal{P}'_{τ} is hence not a promising quantity to study CP phases, but may be useful for (consistency) tests of the gaugino–higgsino mixing. The top polarization in $\tilde{b} \to t \tilde{\chi}^-$ decays, on the other hand, can be useful to probe ϕ_{μ} , $\varphi_{\tilde{b}}$ and/or $\delta_{\phi} = \phi_{\mu} + \varphi_{\tilde{b}}$ in some regions of the parameter space. The measurement of \mathcal{P}'_{t} , revealing phases or being consistent with vanishing phases, may also constrain $|A_b|$. For a more detailed report of our investigations, see [21].

3. Extra dimensions

3.1 Collider signals for Randall-Sundrum model (RS1) with SM gauge and fermion fields in the bulk

K Agashe, K Assamagan, J Forshaw and R M Godbole

This work is based on the model in [26] to which the reader is referred for further details and for references.

Consider the Randall–Sundrum (RS1) model which is a compact slice of AdS₅,

$$ds^{2} = e^{-2k|\theta|r_{c}}\eta^{\mu\nu}dx_{\mu}dx_{\nu} + r_{c}^{2}d\theta^{2}, -\pi \leq \theta \leq \pi,$$

$$(7)$$

where the extra-dimensional interval is realized as an orbifolded circle of radius r_c . The two orbifold fixed points, $\theta = 0, \pi$, correspond to the 'UV' (or 'Planck') and

'IR' (or 'TeV') branes respectively. In warped space-times the relationship between 5D mass scales and 4D mass scales (in an effective 4D description) depends on location in the extra dimension through the warp factor, $e^{-k|\theta|r_c}$. This allows large 4D mass hierarchies to naturally arise without large hierarchies in the defining 5D theory, whose mass parameters are taken to be of order the observed Planck scale, $M_{\rm Pl} \sim 10^{18}$ GeV. For example, the 4D massless graviton mode is localized near the UV brane while Higgs physics is taken to be localized on the IR brane. In the 4D effective theory one then finds

Weak scale
$$\sim M_{\rm Pl} {\rm e}^{-k\pi r_c}$$
. (8)

A modestly large radius, i.e., $k\pi r_c \sim \log{(M_{\rm Pl}/{\rm TeV})} \sim 30$, can then accommodate a TeV-size weak scale. Kaluza–Klein (KK) graviton resonances have $\sim ke^{-k\pi r_c}$, i.e., TeV-scale masses since their wave functions are also localized near the IR brane.

In the original RS1 model, it was assumed that the entire SM (including gauge and fermion fields) resides on the TeV brane. Thus, the effective UV cut-off for the gauge, fermion and Higgs fields, and hence the scale suppressing higher-dimensional operators, is \sim TeV. However, bounds from electroweak precision data on this cut-off are \sim 5–10 TeV, whereas those from flavor changing neutral currents (FCNC's) (for example, $K-\bar{K}$ mixing) are \sim 1000 TeV. Thus, stabilizing the electroweak scale requires fine-tuning, i.e., even though RS1 explains the big hierarchy between Planck and electroweak scale, it has a 'little' hierarchy problem.

A solution to this problem is to move the SM gauge and fermion fields into the bulk. Let us begin with how bulk fermions enable us to evade flavor constraints. The localization of the wave function of the massless chiral mode of a 5D fermion (identified with the SM fermion) is controlled by the c-parameter. In the warped scenario, for c > 1/2 (c < 1/2) the zero mode is localized near the Planck (TeV) brane, whereas for c = 1/2, the wave function is flat. So, we choose c > 1/2 for light fermions so that the effective UV cut-off \gg TeV and thus FCNC's are suppressed. Also this naturally results in a small 4D Yukawa coupling to the Higgs on TeV brane without any hierarchies in the fundamental 5D Yukawa couplings. Left-handed top and bottom quarks are close to c = 1/2 (but < 1/2) – we can show $c_{\rm L} \sim 1/2$ is necessary to be consistent with $Z \to \bar{b}_{\rm L} b_{\rm L}$ for KK masses \sim few TeV – whereas right-handed top quark is localized near the TeV brane to get O(1) top Yukawa coupling. Furthermore, few (3-4) TeV KK masses are consistent with electroweak data (S and T parameters) provided we enhance the electroweak gauge symmetry in the bulk to $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$, thereby providing a custodial isospin symmetry sufficient to suppress excessive contributions to the T parameter.

We can show that in such a set-up (with bulk gauge fields) *high*-scale unification can be accommodated which is an added motivation for its consideration.

In this project, our goal is to identify/study collider signals for this model. We can show that the Higgs couplings to electroweak gauge KK modes are enhanced (compared to that of zero-modes, i.e., SM gauge couplings) by $\sim \sqrt{k\pi r_c} \sim 5$ –6 since the Higgs is localized on the TeV brane and the wave functions of the gauge KK mode are also peaked near the TeV brane. Thus, longitudinal W,Z (eaten Higgs component) fusion into electroweak gauge KK modes (with masses \sim few TeV) is enhanced. In turn, these KK modes have sizeable decay widths to longitudinal W/Z's:

High energy and collider physics

$$W_{\text{long.}}$$
 $Z_{\text{long.}}$ $(W_{\text{long.}})$ $\stackrel{g\sqrt{k\pi r_c}}{\longrightarrow} W^{\pm (n)}, Z^{(n)}, \tilde{W}^{\pm (n)}, Z'^{(n)}$
$$\stackrel{g\sqrt{k\pi r_c}}{\longrightarrow} W_{\text{long.}} Z_{\text{long.}} (W_{\text{long.}}, W_{\text{long.}})$$
 (9)

(here the subscript (n) denotes a KK mode).

Note that the rise with energy of the $W_{\rm long.}, Z_{\rm long.}$ cross-section is softened by Higgs exchange, considerably below the energies of these resonances in longitudinal W/Z scattering.

As per the AdS/CFT correspondence, this RS model is dual to a strongly coupled large-N 4D conformal field theory (CFT) with $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ global symmetry whose $SU(3)_c \times SU(2)_L \times U(1)_Y$ subgroup is gauged. A Higgs on the TeV brane corresponds to a composite of the CFT responsible for spontaneous breaking of $SU(2)_L \times SU(2)_R$ symmetry. That is, this model is dual to a particular type of composite Higgs model. The electroweak gauge KK modes are techni- ρ 's in the dual interpretation. Thus, the enhanced coupling of Higgs to electroweak gauge KK modes was expected from their CFT dual interpretation as strongly coupled composites.

This is similar to technicolor models where one might anticipate a signal at the LHC in longitudinal W/Z scattering for ~ 2 TeV techni- ρ 's. This process is illustrated in figure 6. Whether there exists an observable signal for 3 TeV gauge KK modes requires a calculation of the cross-section and a simulation of the process and associated backgrounds, which is in progress. In particular, one needs to determine whether the strong coupling to these new particles can compensate the suppression in rate due to the largeness of the resonant mass.

There are also possible signals with final states involving either two, three or four top quarks which are also illustrated in figure 6. All three channels benefit from the fact that $t_{\rm R}$ is strongly coupled, i.e. $\sqrt{k\pi r_c}$ -enhanced, to the gluon and/or $W_{\rm R}$ KK modes since its wave function is localized near TeV brane. The final channel illustrated in figure 6 benefits from an enhanced Higgs- $t_{\rm R}$ - $b_{\rm L}^{(n)}$ coupling $\sim \lambda_{\rm t} f(c_{\rm L}) \sim \sqrt{10}$ (where $f(c_{\rm L}) \approx \sqrt{2/(1-2c_{\rm L})}$ and $c \sim 0.4$ for $(t,b)_{\rm L}$) which leads to $b_{\rm L}^{(n)}$ production via longitudinal $W-t_{\rm R}$ fusion. Such studies are underway.

4. Linear collider

4.1 Transverse beam polarization and CP-violating triple-gauge-boson couplings in $e^+e^-\to \gamma Z$

B Ananthanarayan, A Bartl, Saurabh D Rindani, Ritesh K Singh

The project was to study the benefits from significant transverse polarization at the linear collider through the window of CP violation. Two of the members of the collaboration had recently studied the possibility of observing CP violation in the reaction $e^+e^- \to t\bar{t}$. It had been concluded in that study that CP violation only from (pseudo-)scalar (S) or tensor (T) type interactions due to beyond the standard

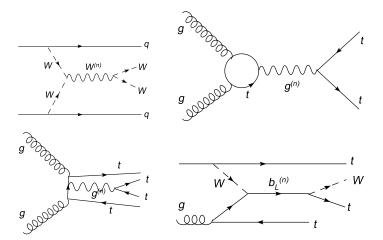


Figure 6. Possible production mechanisms for KK states at the LHC.

model physics could be probed in the reaction when no final state polarization is observed, in the presence of transverse beam polarization. This result was obtained by generalizing certain results due to Dass and Ross from the 1970s [26a].

Discussions at WHEPP-8 took place around the works cited above. It was realized that in a reaction involving self-conjugate neutral particles in the final state, transverse beam polarization could assist in probing CP violation that arose not necessarily from S and T currents. This stems from the fact that in the latter reaction, the matrix elements for the reaction receive contribution from the t- and u-channels. As a result, one project that was isolated was to carry out a full generalization of the results of Dass and Ross that were pertinent to s-channel reactions, to those which involve t- and u-channels.

As a first step therefore, one wished to study specific examples. For instance, the members of the collaboration wished to study the reaction $e^+e^- \to \gamma Z$ as an example. In particular, all beyond the standard model physics was assumed to arise from anomalous triple-gauge-boson couplings. The task was to compute the differential cross-section for the process in the presence of anomalous couplings and transverse beam polarization, and then to construct suitable CP-odd asymmetries. A numerical study was proposed to place suitable confidence limits on the anomalous couplings for realistic polarization and integrated luminosity at a design LC energy of $\sqrt{s}=500~{\rm GeV}$.

After WHEPP-8 the members of the collaboration carried out the project and the results are published in [27]. Two of the members of the collaboration have also considered more recently the most general gauge-invariant and chirality-conserving interactions that would contribute to CP violation in $e^+e^- \to \gamma Z$ [27a].

Another possible example that was considered by the members of the collaboration was a reaction with a slepton pair in the final state. Work is yet to begin on this. $4.2\ Decay\ lepton\ angular\ distribution\ in\ top\ production$ – $decoupling\ from\ anomalous\ tbW\ vertex$

Rohini M Godbole, Manas Maity, Saurabh D Rindani, Ritesh K Singh

The project was to study the (in)dependence of decay lepton angular distribution, on any anomalous coupling in top-decay vertex, for different production processes of the top-quark. It is known in literature that the angular distribution of decay lepton, in pair production of top-quarks, is independent of the anomalous tbW coupling to linear order. This result is independent of the initial state and hence valid for all colliders. Thus decay lepton angular distribution provides, at all colliders, a pure probe of possible anomalous interaction in the pair production of top-quarks, uncontaminated by any new physics in decay of top-quark. This result, though very attractive and useful, lacks a fundamental understanding. At WHEPP-8, we discussed possible approaches to understand the above said decoupling and explore the possibilities of extending this 'decoupling theorem' to processes involving single top production and top pair production in $2 \to 3$ processes. If the decoupling is observed in $2 \to 3$, it possibly can be extended to $2 \to n$ processes of top production.

4.3 Graviton resonances in $e^+e^- \rightarrow \mu^+\mu^-$ with Beamstrahlung and ISR

Rohini M Godbole, Santosh Kumar Rai and Sreerup Raychaudhuri

The next generation of high-energy e^+e^- colliders [28,29] will necessarily be linear colliders to avoid losses due to synchrotron radiation. However, as a linear collider will have single-pass colliding beams, the bunches constituting a beam would have to be focused to very small dimensions to get an adequate luminosity. This is an essential part of the design of all the proposed machines. The high density of charged particles at the interaction point would necessarily be accompanied by strong electromagnetic fields. The interactions of beam particles with the accelerating field generates the so-called initial state radiation (ISR), while their interactions with the fields generated by the other beam also generates radiation, usually dubbed Beamstrahlung [30].

Traditionally, ISR and Beamstrahlung have been considered nuisances which cause energy loss and disrupt the beam collimation. The energy-spread due to these radiative effects has led to a requirement of realistic simulations for physics processes which would require the knowledge of the energy spectrum of the colliding beams at the interaction point. The beam designs being considered are usually such that these effects are minimized.

In this note we argue that instead of just being a nuisance which we have to live with, photon radiation from initial states can actually be of great use in probing new physics scenarios under certain circumstances. As a matter of fact tagging with ISR photons has been used effectively in the LEP experiments, to search for final states which do not leave too much visible energy in the detectors; for example, a $\tilde{\chi}^+\tilde{\chi}^-$ (chargino) pair with $\tilde{\chi}^+$ and the LSP $\tilde{\chi}^0_1$ being almost degenerate [31]. Here, we look at a different aspect and usage of these radiative effects. To illustrate it we look at one of the simplest processes at an e^+e^- collider, viz.

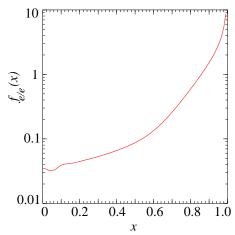


Figure 7. Illustrating the effective electron luminosity at TESLA-800 as a function of $x = E_{\rm e}/E_{\rm beam}$, the energy fraction of the electron after radiating a photon. The Beamstrahlung parameter is $\Upsilon = 0.09$.

$$e^+e^- \to X^* \to \mu^+\mu^-,$$

where X can be either a massive scalar, vector or tensor. In the standard model, $X = \gamma, Z$. For any heavy particle X, there will be resonances in the s-channel process, observable as peaks in the invariant mass $M_{\mu^+\mu^-}$ distribution. At LEP, for example, this process was used to measure the Z-resonance line shape. In this note, we focus our attention on tensor particle resonances, the tensors being the massive Kaluza–Klein gravitons as predicted in the well-known brane-world model of Randall and Sundrum [32].

The central point in our argument is that it is very likely that the next generation linear colliders would run at one (or a few) fixed value(s) of centre-of-mass energy. For example, TESLA [28] is planned to run at $\sqrt{s} = 500$ GeV and 800 GeV. However, the predicted massive graviton excitations of the Randall–Sundrum (RS) model may not lie very close to these energy values. Consequently, the new physics effect due to exchange of RS gravitons will be off-resonance and hence strongly suppressed. However, a spread in beam energy would cause *some* of the events to take place at a lower effective centre-of-mass energy around the resonance(s) and hence provide an enhancement in the cross-section. A similar effect, for example, was observed in Z-resonances at LEP-1.5 and dubbed the 'return to the Z-peak'. We, therefore, investigate 'return to the graviton peak' in the process $e^+e^- \to \mu^+\mu^-$.

In our analysis of radiative effects we use the structure function formalism for ISR and Beamstrahlung developed in [33,34]. Specifically, we use the expression for the electron spectrum function presented in [34]. Figure 7 shows the electron energy spectrum for the given design parameters for the linear collider at TESLA [28] running at $\sqrt{s} = 800$ GeV. It is worth noting that the large spread in the distribution function is more due to Beamstrahlung than due to ISR effects [34].

In the two-brane model of Randall and Sundrum, the standard model is augmented by a set of Kaluza–Klein excitations of the graviton, which behave like

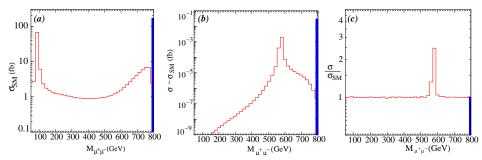


Figure 8. Invariant mass distribution with (outlined histogram (red)) and without (solid histogram (blue)) radiative effects. The figures show (a) the bin-wise cross-section $\sigma_{\rm SM}$ for the SM background, (b) the bin-wise excess cross-section $\sigma - \sigma_{\rm SM}$ predicted in the RS model and (c) the signal-to-background ratio $\sigma/\sigma_{\rm SM}$.

massive spin-2 fields with masses $M_n = x_n m_0$, where x_n are the zeroes of the Bessel function of order unity, n is a non-negative integer and m_0 is an unknown mass scale close to the electroweak scale. Search possibilities for these gravitons at future e^+e^- colliders have been studied in [35]. Experimental data from the Drell–Yan process at the Tevatron constrain m_0 to be more or less above 130 GeV [36]. Another undetermined parameter of the theory is the curvature of the fifth dimension, expressed as a fraction of the Planck mass $c_0 = \mathcal{K}/M_{\rm P}$. Feynman rules for the Randall–Sundrum graviton excitations can then be read-off from the well-known Feynman rules given in [37] by making the simple substitution $\kappa \to 4\sqrt{2\pi}c_0/m_0$. Noting that the massive graviton states exchanged in the s-channel can lead to Breit–Wigner resonances, it is now a straightforward matter to calculate the cross-section for the process $e^+e^- \to \mu^+\mu^-$ and implement it in a simple Monte Carlo event generator.

Our numerical analysis has been performed for values $m_0=150~{\rm GeV}$ and $c_0=0.01$, which implies that the lightest (n=1) massive excitation has mass $M_1=574.5~{\rm GeV}$, putting it well beyond the present reach of Run-II data at the Tevatron [36]. With this choice, however, the next excitation is predicted to have mass $M_2>1~{\rm TeV}$, which puts it well beyond the reach of TESLA-800. We expect, therefore, to detect one, and only one, resonance. The value of c_0 has been chosen at the lower end of the possible range, since this leads to a longer life-time for the Kaluza–Klein state and hence a sharper resonance in the cross-section. Following standard practice for linear collider studies, we eliminate most of the backgrounds from beam–beam interactions and two-photon processes by imposing an angular cut $10^{\circ} < \theta_{\mu^{\pm}} < 170^{\circ}$ on the final-state muons. Some of our results are illustrated in figure 8, which shows the bin-wise distribution of invariant mass $M_{\mu^{+}\mu^{-}}$ of the (observable) final state. In figure 8a, we have plotted the distribution predicted in the standard model (SM). Figure 8b shows the excess over the SM prediction expected in the Randall–Sundrum model and figure 8c shows the signal-to-background ratio.

At a linear collider with fixed center-of-mass energies, all the events for the above process should be concentrated in a single invariant mass bin at $M_{\mu^+\mu^-} \sim \sqrt{s}$ in the lab frame. In figure 8 these correspond to the solid (blue) bins in the $M_{\mu^+\mu^-}$

distribution. Comparison of figures 8a and 8b shows that the expected signal is very small indeed, about 1 in 10^4 . Consequently the ratio exhibited in figure 8c is almost precisely unity. This is because our parameter choice leads to a graviton of mass 574.5 GeV, and decay width of a few GeV, which is far away from the centre-of-mass energy $\sqrt{s} = 800$ GeV.

The outlined (red) histograms in figure 8 show the invariant mass distribution when radiative effects are included. It is immediately apparent that the invariant mass and hence the effective centre-of-mass energy $\sqrt{s'} = M_{\mu^+\mu^-}$ is spread out from the beam energy \sqrt{s} . In (a), we can see a distinct peak at the lower end which represents 'return to the Z-peak'. The cross-section for this peak is not as high as one might expect for a narrow resonance like Z because this corresponds to an extremely large value for the energy fraction x taken away by the photon, for which the luminosity is extremely small. The shape of the rest of the histogram is simply a reflection of the electron luminosity shown in figure 1. A similar phenomenon happens in (b) due to the large spread in the energy of the colliding beams. Here the radiative return to the resonant KK-graviton is quite apparent. In fact, excitation of the graviton resonance leads to a greatly enhanced cross-section, as this graph shows. The outlined (red) histogram in (c), shows the signal-to-background ratio. This ratio removes the Z-peak and clearly throws into prominence the graviton resonance, presenting us with a clear signal for a new resonant particle. To confirm that it is indeed a graviton, one must run various tests, such as plotting the angular distribution. These will be discussed in a forthcoming publication [38]. Note also that the method can be used with effect only for final states not involving strongly interacting particles, as two-photon processes can give rise to a substantial two-jet production for invariant masses quite a bit smaller than the nominal centre-of-mass energy of the collider [34].

It is thus clear that ISR and Beamstrahlung can play a non-trivial role in the identification of new physics effects. This is a positive feature of these radiative phenomena, which has not often been considered, and the main purpose of this work is to emphasize this aspect.

4.4 Probing R-parity violating models of neutrino mass at the linear collider

A Bartl, S P Das, A Datta, R M Godbole and D P Roy

The observation of neutrino oscillations and the measurement of oscillation parameters by the SUPERK Collaboration [39] and others [40,41] have established that at least two of the neutrino masses are non-zero albeit their magnitudes are several orders of magnitude smaller than that of the other fermions.

A natural explanation of the smallness of the neutrino masses is perhaps the most challenging task of current high energy physics. The see-saw mechanism [42] is certainly the most popular model. However, the simplest version of this model – a supersymmetric grand unified theory (SUSY GUT) of the grand desert type, which can also explain coupling constant unification [43], has practically no other crucial prediction for TeV scale physics. If an intermediate scale is allowed then both SUSY and non-SUSY GUTs, the latter being plagued by the notorious fine tuning problem, may serve the purpose. But there is no compelling reason within the framework of either of these models for new physics at the TeV scale.

In contrast, within the framework of *R*-parity violating (RPV) SUSY, Majorana masses of the neutrinos can be generated both at the tree-level and at the one-loop level quite naturally. More importantly the physics of this mechanism is entirely governed by TeV scale physics (sparticle masses and couplings) which can in principle be verified at the next round of collider experiments.

Neutrino masses within the framework of RPV SUSY have been studied by several groups [44]. Such masses may arise both at the tree-level as well as at the one-loop level. As an example, we refer to [45], where upper bounds on RPV bilinear and trilinear terms were derived (see tables III–VIII of [45]) using some simplifying assumptions about the *R*-parity-conserving (RPC) sector (see below).

In this working group project we try to further sharpen these predictions. We obtain several combinations of lepton number violating trilinear (λ_{ijk} , λ'_{ijk} , i, j, k = 1, 2, 3) and bilinear ($\mu_i, i = 1, 2, 3$) couplings which are consistent with the current ranges of the oscillation parameters [46].

The squared mass differences of different neutrinos are defined as:

$$\Delta m_{\rm sun}^2 \equiv |\Delta m_{12}^2|, \quad \Delta m_{\rm atm}^2 \equiv |\Delta m_{23}^2|, \tag{10}$$

where $\Delta m_{12}^2 = m_2^2 - m_1^2 > 0$ and $\Delta m_{23}^2 = m_3^2 - m_2^2$ assuming $m_1^2 < m_2^2 < m_3^2$. The limits on them are 5E-05 $< \Delta m_{\rm sun}^2 ({\rm eV}^2) < 10$ E-05 and 1E-03 $< \Delta m_{\rm atm}^2 ({\rm eV}^2) < 4$ E-03. Similarly the mixing angle constraints are $0.29 < \tan^2 \theta_{12} < 0.82,\ 0.45 < \tan^2 \theta_{23} < 2.3,\ 0.0 < \tan^2 \theta_{13} < 0.05$ for solar, atmospheric and

Since our results are basically illustrative, we employed the same simplifying assumptions as in [45].

- \bullet All masses and mass parameters in the RPC sector of the MSSM are $\approx\!100$ GeV.
- $\tan \beta = 2$.

CHOOZ data [46].

This leads to the following tree-level and loop-level mass matrices [45]:

$$\mathcal{M}_{\nu_{ij}}^{\text{tree}} = C\mu_i\mu_j,\tag{11}$$

$$\mathcal{M}_{\nu}^{\text{loop}} = \begin{pmatrix} K_{1}\lambda_{133}^{2} + K_{2}\lambda_{133}^{\prime 2} & K_{1}\lambda_{133}\lambda_{233} + K_{2}\lambda_{133}^{\prime}\lambda_{233}^{\prime} & K_{2}\lambda_{133}^{\prime}\lambda_{333}^{\prime} \\ K_{1}\lambda_{133}\lambda_{233} + K_{2}\lambda_{133}^{\prime}\lambda_{233}^{\prime} & K_{1}\lambda_{233}^{2} + K_{2}\lambda_{233}^{\prime 2} & K_{2}\lambda_{233}^{\prime}\lambda_{333}^{\prime} \\ K_{2}\lambda_{133}^{\prime}\lambda_{333}^{\prime} & K_{2}\lambda_{233}^{\prime}\lambda_{333}^{\prime} & K_{2}\lambda_{233}^{\prime 2} \end{pmatrix},$$

$$(12)$$

where the constants are given by $C \approx 5.3 \times 10^{-3} \text{ GeV}^{-1}$, $K_1 \approx 1.8 \times 10^{-4} \text{ GeV}$ and $K_2 \approx 4.7 \times 10^{-3} \text{ GeV}$. In [45] several scenarios were considered with five non-zero RPV couplings (see table III of [45]). For the purpose of illustration we consider scenario 1 where the non-vanishing parameters are the three μ 's, λ_{133} and λ_{233} .

Now we try to fit the above oscillation parameters by varying the above five parameters randomly subject to the existing bounds (see table V of [45]; we have considered the MSW large mixing angle solution only). By generating 10,000 sets of parameters we have obtained only three solutions in (see, table 1). It is gratifying to

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Table 1. Allowed RPV parameters consistent with the neutrino data in [46].

Solution No.	$\mu_1 \; (\text{GeV})$	$\mu_2 \; (\mathrm{GeV})$	$\mu_3 \; (\mathrm{GeV})$	λ_{133}	λ_{233}
I	1.1E-05	5.9E-05	8.2E-05	1.5E-04	1.9E-04
II	4.4E-06	6.5E-05	8.0E-05	1.4E-04	2.1E-04
III	8.0E-06	4.3E-05	7.9E-05	1.6E-04	2.1E-04

Table 2. Lightest neutralino decay branching ratios and decay lengths for the first two scenario of table 1.

Solution No.	BR	Decay length (c $\times \tau$ in cm)
I	(a) 0.186 (b) 0.323 (c) 0.491	35.82
II	(a) 0.156(b) 0.352(c) 0.492	37.66

note that even the rather loose constraints on the oscillation parameters currently available are sufficiently restrictive to yield a remarkably small set of solutions.

Although $\tilde{\chi}_1^0$ (LSP) decay is generic in RPV models, the above examples illustrate that the branching ratios and the life-time of the LSP, which we assume to be the lightest neutralino, will have very specific patterns if the oscillation constraints are imposed. In the scenario under consideration the allowed decay modes are

(a)
$$\tilde{\chi}_1^0 \to e \tau \not\!\!E_T$$
, (b) $\tilde{\chi}_1^0 \to \mu \tau \not\!\!E_T$ and (c) $\tilde{\chi}_1^0 \to \tau \tau \not\!\!E_T$, (13)

where the missing energy (E_T) is carried by the neutrinos. Charge conjugate modes are included in our analysis.

In table 2 we have presented some LSP decay characteristics calculated by CompHEP [47] using the first two solutions in table 1. We find that in order to distinguish solutions number I from II, the BR(a), (b) and the decay length have to be measured with accuracy better than 17.4%, 8.5% and 5.6% respectively.

Although our calculations were based on very specific assumptions, there are reasons to believe that the restricted nature of the predictions of this model will continue to hold even without these assumptions. Improvement in the precision of the magnitudes of the oscillation parameters in the future long baseline experiments will impose even tighter constraints on model parameters. For example, we have tested that the ranges of oscillation parameters in [45] (see table 1) based on old data lead to many more solutions.

Moreover, measurements of superparticle masses, couplings and some of the branching ratios (BRs) will be available [48] from LHC within the first few years of its running, if SUSY exists. This may enable one to fix the constants C, K_1 and K_2 within reasonable ranges without additional assumptions. Precision measurements

of LSP decay properties to verify the RPV models of neutrino mass seem to be a challenging, but perhaps feasible, task for the next linear collider (LC).

It is interesting to analyse the possible information one may seek at the linear collider to be able to do this job. In case it is the RPV version of SUSY that is realized in nature, even the LHC will offer a rather good measurement of the mass of the LSP, particularly if the λ, λ' RPV couplings are the dominant ones. The LC on the other hand will offer a chance for accurate measurement of the LSP mass as well as its life-time provided the RPV couplings are large and the LSP has macroscopic decay length. We see from table 2, that for the particular solutions path lengths of a few cms are possible for the LSP. Studies of possible accuracies of such measurement need to be performed. It will be possible to measure the mass of the decaying LSP at an LC using either the kinematic end-point measurements and/or through the threshold scans. Very preliminary studies [49] of the possibilities of the mass measurements of the LSP in the production of $\tilde{\chi}_1^0 \tilde{\chi}_2^0, \tilde{\chi}_1^+ \tilde{\chi}_1^-$, followed by the decay of the $\tilde{\chi}_2^0, \tilde{\chi}_1^{\pm}$ and the LSP in the end exist. These studies need to be refined. Further, the LSP decay may also depend on the masses of the third generation sparticles and mixing, precision information for which may also be available only from the LC. These features as well as the possible interplay between the LHC and the LC to pin down RPV SUSY as the origin of neutrino mass need to be studied. Finally we note that if the λ' couplings are indeed $\mathcal{O}(10^{-4})$ as required by models of ν mass [45], lighter top squark decays may provide additional evidence in favour of these models [50].

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