

Evolutionary ecology *in silico*: Does mathematical modelling help in understanding ‘generic’ trends?

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Motivated by the results of recent laboratory experiments, as well as many earlier field observations, that evolutionary changes can take place in ecosystems over relatively short ecological time scales, several ‘unified’ mathematical models of evolutionary ecology have been developed over the last few years with the aim of describing the statistical properties of data related to the evolution of ecosystems. Moreover, because of the availability of sufficiently fast computers, it has become possible to carry out detailed computer simulations of these models. For the sake of completeness and to put these recent developments in perspective, we begin with a brief summary of some older models of ecological phenomena and evolutionary processes. However, the main aim of this article is to review critically these ‘unified’ models, particularly those published in the physics literature, in simple language that makes the new theories accessible to a wider audience.

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1. Introduction

Enormous progress has been made in the twentieth century in the domain of sub-cellular and cell biology, particularly in area of molecular genetics and genomics. One of the challenges of the twenty-first century will be to link the insight gained from the molecular level research on uni-cellular as well as multi-cellular organisms to biological research at higher levels of organization, namely, those at the levels of colonies, communities and, finally, eco-systems (Jackson *et al* 2002; Kafatos and Eisner 2004). Admittedly, at present, we are far from that goal.

In traditional paleobiology, analysis of the fossil data has always been the most popular way of understanding the causes and consequences of extinction of species as well as those of biotic recoveries from mass extinctions (Ehrlich and Ehrlich 1981; Raup 1986 1991; Miller 1998; Erwin 2001; Jablonski 2004). Unfortunately, the available record of the history of life, written on stone in the form of fossils, is incomplete and ambiguous (Raup 1991). Laboratory experiments have also played equally

important role so far in ecology and evolutionary biology. However, an alternative enterprise seeks to recreate the evolution on a computer by simulating theoretical models; this is often referred to as *in silico* experiments.

Models are normally useful in understanding the real world. In principle, models can be verbal or symbolic, graphical or abstract, qualitative or quantitative. However, throughout this paper, by the term model we shall always mean mathematical models that not only indicate qualitative features of various quantities of interest but can also make quantitative predictions. Mathematical modelling often helps in getting insight into ecological phenomena and evolutionary processes (Murray 1989; Edelshtein-Keshet 1988). Most of the ecological and evolutionary models are too complicated to be solved analytically; for such models computer simulation is one of the most powerful tools of analysis.

It has been realized in recent years that ecosystems are examples of complex adaptive systems (Levin 1998; Hartvigsen *et al* 1998; Milne 1998; Wu and Marceau 2002). Over the last ten years statistical physicists have

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used the conceptual toolbox of their profession for understanding some aspects of the dynamical evolution of ecosystems which include, for example, the ‘generic’ trends in the statistics of the data on speciation and extinction (Drossel 2001; Newman and Palmer 2002; Sole *et al* 1999). Significant progress has been made over the last three years in developing detailed models that incorporate not only ecological phenomena on short periods of time but also evolutionary processes on longer time scales. In this article we present a critical overview of the current status of the “unified generic theories” of evolutionary ecology.

Models intended to describe the spatio-temporal patterns in ecological and evolutionary processes must set the spatio-temporal scale unambiguously (Levin 2000; Allen and Hollin 2002). For example, let us consider a single aerial photograph of a landscape. While the boundaries of the photograph determine the spatial extent of the observation, the size of the pixels (grain size) in the photograph imposes the limit on the spatial resolution. Similarly, if a sequence of photographs of the same landscape is taken at regular intervals, the time difference between the first and the last photograph is a measure of the temporal extent of the observations while the time difference between the successive photographs determines the corresponding temporal resolution (Martinez and Dunne 1998). For example, in ecology the temporal resolution can be days while the temporal extent can be up to decades, whereas the temporal resolution in evolutionary biology, particularly empirical observations from fossil data varies, usually, from tens of thousands to millions of years. In this review we shall consider different classes of models with widely different scales of spatio-temporal resolution.

The ‘ecological’ models, that describe population dynamics in detail using, for example, the Lotka-Volterra equations (discussed in § 3) usually ignore the slow macro-evolutionary changes in the eco-system; hardly any effects of these would be observable before the computer simulations would run out of computer time. On the other hand, in order to simulate the billion-year old history of life on earth with a computer, the elementary time steps in ‘evolutionary’ models have to correspond to thousands of years, if not millions; consequently, the finer details of the ecological processes over shorter periods of time cannot be accounted for by these models in any explicit manner. However, despite the practical difficulties, it is desirable, at least in principle, to develop one single theoretical model which would be able to describe the entire dynamics of an eco-system since the first appearance of life in it up till now and in as much detail as possible. This dream has now come closer to reality, mainly because of the availability of fast computers. It has now become feasible to carry out computer simulations of eco-system models where, each time step (i.e.

temporal resolution) would correspond to typical times for ‘micro’-evolution while the total duration (i.e. temporal duration) of each of the simulations is long enough to capture ‘macro’-evolution.

The mathematical models in evolutionary ecology can be broadly classified into different classes with different levels of detailed description, as shown in figure 1.

In the earliest mathematical models of population dynamics, only one predator species and one prey species were considered. However, for modelling the population dynamics of more than two species, one needs to know the food web which is a graphical way of describing the prey-predator relations, i.e. which species eats which one and which compete among themselves for the same food resources (Pimm 1982; Cohen *et al* 1990; Polis and Winemiller 1996; Drossel and McKane 2003). More precisely, a food web is a directed graph where each node is labelled by species’ name and each directed link indicates the direction of flow of nutrient (i.e. from a prey to one of its predators). In the early works of this type, the food web was assumed to be static, i.e. independent of time. An altogether different class of models were developed to study macro-evolution; in such models, because of the Darwinian evolution, the food web is a dynamic network. In recent times, models of evolutionary ecology have been developed by a synthesis of ecological models of population dynamics and macroevolutionary models with evolving food webs. However, a more detailed theoretical description has also been attempted by incorporating individual organisms explicitly in the model where the birth, ageing and death of each individual occurs naturally.

Almost all the models developed along the lines of models of physical systems usually reach a stationary state

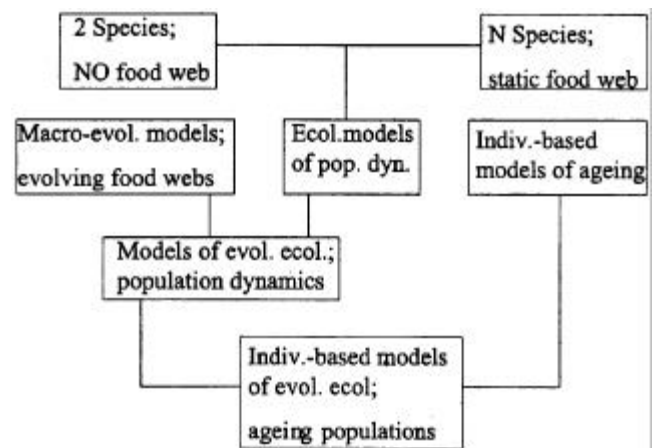


Figure 1. Broad classification of the mathematical models of evolutionary ecology with different levels of detailed description.

after sufficiently long time. In contrast to these models, the models closer to biological reality might never reach a stationary state. After all, life forms in nature have evolved over billions of years from simple bacteria and archaea to complex structures like the bodies of dinosaurs and the brains of our readers.

So far as the results of theoretical modelling are concerned, most of the recent works in physics literature have been concerned with the possibility of the existence of 'power laws' in the statistics of extinction data. For example, suppose it is claimed that the relative frequency $P(s)$ of extinctions of size s follows the power-law $P(s) \propto s^{-t}$ with $t \cong 2$. If irrefutable evidences in favour of such power laws can be gathered, either from fossil data or from mathematical modelling, it would imply that the self-organizing dynamics of eco-systems exhibit fluctuations that are statistically self-similar because a change of scale ($s @ s \mathcal{C} = b s$) leaves the form of the power law unchanged.

2. Ageing and age-structured population in single species

Biological ageing of adults is best measured through the mortality $q(a) = [S(a) - S(a + 1)]/S(a)$ where $S(a)$ is the number of survivors to the age a in suitable time units (like years for humans or days for flies and worms). More accurate is the mortality function $\mu(a) = -d \ln S(a)/da$ which is defined in terms of a derivative instead of a difference. The Gompertz law states that the mortality function for adults increases exponentially with age; this is also valid for many animals, but does not hold for the youngest and perhaps the oldest ages (Vaupel *et al* 1998). Many theories exist to explain ageing (Finch 1990; Rose 1994; Mueller and Rose 1996): accumulation of hereditary detrimental mutations (Moss de Oliveira *et al* 1999), reliability theory as known from engineering in inanimate machines (Gavrilov and Gavrilova 2001), loss of telomeres in cell division (Aviv *et al* 2003; Joeng *et al* 2004; Masa M, Cebrat S and Stauffer D, unpublished results), damage caused by oxygen radicals, trade-off between longevity and fecundity (disposable soma), wear and tear, etc. Only for the first three, several quantitative computer simulations or mathematical solutions, giving the Gompertz law, are known to us, as listed in the cited literature.

These models do not explicitly incorporate inter-species interactions like, for example, prey-predator interactions. These models cannot capture macro-evolutionary phenomena like, for example, extinctions which depend crucially on the prey-predator interactions. Such interactions are an essential part of the ecological models which we mention briefly in the next section.

3. Ecological models of population dynamics: prey-predator interactions

Traditionally, the population dynamics of prey-predator systems have been described quantitatively in terms of the Lotka-Volterra equations (Goel *et al* 1971a,b; Pielou 1977; Emlen 1984). The nonlinearity of these deterministic differential equations leads to a rich variety of dynamical behaviour of the system. Although originally only two interacting species (predator and prey) were considered, later the approach was extended to more than two (but only a few) interacting species. Pioneering mathematical work of May (1973) raised the question of stability of these dynamical equations when the number of interacting species increases. This challenged the earlier common belief that diversity of species ensured enhanced stability of the eco-system (Svirezhev and Logofet 1983; Hofbauer and Sigmund 1988; Logofet 1993; McCann 2000; Sinha S and Sinha S, unpublished results).

Unlike the models of ageing discussed in the preceding section, these Lotka-Volterra-type models of population dynamics monitor only the increase (or decrease) of populations caused by the birth (or death) of individual organisms but, usually, do not keep track of their ageing with time.

The original formulation of the Lotka-Volterra equations assume that the population of the prey as well as that of predators are uniformly distributed in space. The absence of the spatial degrees of freedom in these equations is usually interpreted in the statistical physics literature as a mean-field-like approximation. This situation is similar to a well-stirred chemical reaction where the spatial fluctuations in the concentrations of the reactants and the products is negligibly small. On the other hand, spatial inhomogeneties in the eco-systems and migration of organisms from one eco-system to another are known to play crucial roles in evolutionary ecology (Tilman and Kareiva 1997; Czaran 1998; Bascompte and Sole 1998).

In recent years, the spatial inhomogeneity of the populations, i.e. variation in the population of the same species from one spatial patch to another (Singh *et al* 2004), that have been observed in real ecosystems has been captured by extending the Lotka-Volterra systems on discrete lattices where each of the lattice sites represents different spatial patches or habitats of the ecosystem (Tainaka 1989; Satulovsky and Tome 1994; Boccara *et al* 1994; Frachebourg *et al* 1996; Johst *et al* 1999; Lipowski 1999; Antal and Droz 2001; Antal *et al* 2001; Droz and Pekalski 2002, 2004).

For modelling the population dynamics of more than two species, one needs to know the food web which is a graphical way of describing the prey-predator relations, i.e. which species eats which one and which compete among themselves for the same food resources (Pimm 1982; Cohen

et al 1990; Polis and Winemiller 1996; Drossel and McKane 2003). The structure of foodwebs and their statistical properties have been investigated both using field data on real eco-systems as well as abstract mathematical models (Briand and Cohen 1984; Cohen *et al* 1990; Hall and Raffaelli 1991; Goldwasser and Roughgarden 1993; Martinez and Lawton 1995; Martinez and Dunne 1998; Williams and Martinez 2000; Sole and Montoya 2001; Dunne *et al* 2002a,b; Montoya and Sole 2002; Jennings and Warr 2003; Brose *et al* 2004), particularly, in the recent years in the light of scale-free and small world networks (Strogatz 2001; Albert and Barabasi 2002).

A static (time-independent) food web may be a good approximation over a short period of time. But, a more realistic description, valid over longer period of time, must take into account not only the adaptations of the species and their changing food habits, but also their extinction and creation of new species through speciation or migration of alien species into a new habitat. These processes make the food web a slowly evolving graph. Such slow time evolution of the food webs are naturally incorporated in macroevolutionary models which we summarize in the next section.

4. Modelling macroevolution and extinction: evolving food webs

These models are intended to throw light on the mechanisms of origination of species through speciation as well as their extinction arising from biotic and abiotic causes. Several models have been developed just to account for the different routes to speciation (Gavrilets *et al* 1998; Diekmann and Doebeli 1999; Gavrilets 1999, 2000, 2003; Doebeli and Diekmann 2000; Kirkpatrick and Vavigne 2002; Kaneko and Yomo 2000; Schluter 2000). However, in this section we shall focus mainly on those works that have been inspired by close similarity with concepts or phenomena in statistical physics.

4.1 Self-organized critical models of eco-systems

Inspired by the work of Bak and Sneppen (1993), a large number of evolutionary models have been developed over the last ten years (Bak and Sneppen 1993; Paczuski *et al* 1996; Newman and Sneppen 1996; Sneppen and Newman 1997; Kramer *et al* 1996; Newman 1996, 1997, 2000; Roberts and Newman 1996; Sole and Bascompte 1996; Sole and Manrubia 1996, 1997; Sole *et al* 1996 1997; Vandewalle and Ausloos 1996; Head and Rodgers 1997; Kirchner and Weil 1998; Manrubia and Paczuski 1998; Sole 1999; Wilke and Martinetz 1997). Most of these works, including that of Bak and Sneppen (1993), claimed the discovery of self-organized criticality (Jen-

sen 1998) in the statistics of the numerical data on extinction. They also drew attention to the close relation of these observations with the concept of ‘punctuated equilibrium’ introduced many years ago, by Gould and Eldredge (1977, 1993) in the context of extinction of species (Bak and Boettcher 1997).

4.2 Modelling evolution as a walk on a fitness landscape

An alternative approach views macroevolution as random walk in a rugged ‘fitness landscape’ (Kauffman 1993). In recent years this approach has been extended by allowing slow evolution of the landscape itself to incorporate the effect of co-evolution of species (Peliti 1995, 1997; Wilke *et al* 2001). The notion of ‘fitness’ has been used often loosely to mean different things (Brookfield 2001).

4.3 Modelling eco-system as network of interacting species

A network model of ecosystems was developed by Sole and Manrubia (1996, 1997). The system consists of N species, each labelled by an index i ($i = 1, 2, \dots, N$). The state of the i th species is represented by a two-state variable S_i ; $S_i = 0$ or 1 depending on whether it is extinct or alive, respectively. The inter-species interactions are captured by the interaction matrix \mathbf{J} ; the element J_{ij} denotes the influence of the species j on the species i . If $J_{ij} > 0$ while, simultaneously, $J_{ji} < 0$ then i is the predator and j is the prey. On the other hand, if both J_{ij} and J_{ji} are positive (negative) the two species cooperate (compete).

The dynamics of the system consists in updating the states of the system (i.e. to determine the state at the time step $t + 1$ from a complete knowledge of the state at the time t) in the following three steps:

Step (i): One of the input connections J_{ij} for each species i is picked up randomly and assigned a new value drawn from the uniform distribution in the interval $[-1, 1]$, irrespective of its previous magnitude and sign (this, we believe, is not a very realistic description of the inter-species interaction).

Step (ii): The new state of each of the species is decided by the equation

$$S_i(t+1) = \Theta \left(\sum_{j=1}^N J_{ij} S_j(t) - \mathbf{q}_i \right) \quad (1)$$

where \mathbf{q}_i is a threshold parameter for the species i and $\Theta(x)$ is the standard step function, i.e. $\Theta(x) = 1$ if $x > 0$ but zero otherwise. If $S(t + 1)$ becomes zero for m spe-

cies, then an extinction of size m is said to have taken place.

Step (iii): All the niches left vacant by the extinct species are refilled by copies of one of the randomly selected non-extinct species.

Sole and Manrubia (1996, 1997) recorded extinctions of sizes as large as 500 and the distributions of the sizes of these extinctions could be fitted to a power law of the form $N(m) \sim m^{-a}$ with an exponent $a \leq 2.3$. Moreover, the periods of stasis t_s were also found to obey a power law $N(t_s) \sim t_s^{-g}$ with the exponent $g \leq 3.0$. However, surprisingly, in none of their papers (Sole and Manrubia 1996, 1997), did Sole and his collaborators report the distributions of the lifetimes of species which, according to some claims (see, for example, Drossel 2001; Newman 2002 for references to the experimental literature and data analysis), also follows a power law.

Amaral and Meyer (1999) considered a hierarchical food web which was assumed to be organized into trophic levels; a species in level l feeds on some species at the level $l-1$ (except for those at $l=1$ which are autotrophic). Origination of species through speciation was assumed to take place as follows: an empty niche is occupied by a non-extinct species at the same trophic level and the prey of the new species are selected randomly from among those at the level immediately below the trophic level of the new species. However, Amaral and Meyer (1999) did not treat the population dynamics of the species explicitly. Instead, a fraction p of the species at the lowest level is randomly selected and made extinct. Then, any species in the next higher level for which all prey species became extinct are also made extinct; this procedure is repeated for all the levels up to the highest one. Although this may be a more realistic description of inter-species interactions than that in the Sole-Manrubia model, the dynamics of the model is oversimplified. From the point of view of mathematical analysis, the advantage of this model is that its properties can be obtained not only numerically (Amaral and Meyer 1999; Camacho and Sole 2000) but also analytically (Drossel 1998).

The main limitation of these models (see also Wilmsers *et al* 2002) is that the individual organisms do not appear explicitly. On the other hand, it is the individual organisms, rather than species, which are the primary objects of selection (Lloyd and Gould 1993; Mayr 1997; Gould and Lloyd 1999; Johnson and Boerlijst 2002). Moreover, the extinction of a species is nothing but eventual demise of all the individual organisms. Furthermore, direct experimental evidences (Thompson 1998a,b; 1999; Fussmann *et al* 2003; Stockwell *et al* 2003; Turchin 2003; Yoshida *et al* 2003) have established that significant evolutionary changes can occur over ecologically relevant time scales.

In other words, the dynamics of ecology and evolution are inseparable.

5. 'Unified' models of evolutionary ecology

The need for 'unification' of the various ecological sub-disciplines, e.g. population ecology, community ecology and evolutionary ecology, has been felt for quite some time (Martinez 1995). In the recent years attempts have been made to model evolutionary ecology in terms of 'unified' models that describe both micro- and macro-evolution. Some of these models describe population dynamics in terms of one single dynamical variable and, therefore, fail to account for the age-structured populations of each species. However, only in the last two years it has been possible to develop detailed models that describe the birth, ageing and death of individual organisms. This is partly because of the availability of relatively fast computers.

Abramson (1997) considered a simple evolving ecosystem where each site of a one-dimensional lattice of finite length L represent a species such that the species i feeds on the species $i-1$ and its eaten by the species $i+1$. The species l , which feeds at a constant rate on the environment, represents the species at the lowest level of the hierarchy whereas the species L , occupying the top of the chain, is not eaten by any other species. Such a linear food web is not realistic, but the importance of the model lies in its its simplicity.

A species is considered extinct when its population falls below a preassigned threshold. Because of the one-dimensional nature of the food web, the system would break into disjoint parts if any site is allowed to remain vacant following extinction of the corresponding species. In order to avoid such a situation, each niche that is left vacant by the extinction of a species is re-filled by another new species which interacts with the two neighbouring species with interactions whose strengths are drawn from a uniformly distributed random fraction. However, Abramson (1997) did not monitor the ageing of each individual organisms. Instead, he monitored only the time evolution of the total populations of each species in the eco-system.

McKane, Higgs and collaborators (Caldarelli *et al* 1998; Drossel *et al* 2001; Quince *et al* 2004a,b) also modelled the population dynamics in terms of one single dynamical variable. But, unlike, Abramson (1997), they took into account the hierarchical organization of the species in food webs. In their webworld model, each species is represented by a set of L features (or, phenotypic characters) chosen from a set of K possible features. Evolution of the webworld model of eco-system is implemented by speciation events during which a new species is created from a randomly chosen existing species; the new species differs

from the parent species by just one randomly chosen feature. There are some close similarities between this model and some models developed in recent years incorporating the individual organisms explicitly in the model.

Over the last two years, a few 'unified' models of evolutionary ecology have been developed incorporating the individual organisms explicitly (Hall *et al* 2002; di Collobiano *et al* 2003; Chowdhury *et al* 2003; Chowdhury and Stauffer 2003, 2004, 2005; Rikvold and Zia 2003; Stauffer and Chowdhury 2004, 2005; Stauffer *et al* 2005).

Each individual organism in the Rikvold-Zia model (Rikvold and Zia 2003) has a genome of L genes, each of which can take one of two possible values, namely, 0 and 1. Thus the total number of different genotypes is 2^L . Rikvold and Zia (2003) assumed that each of the different genotypes represent a separate species. A plausible justification, suggested by Rikvold and Zia, is that each binary 'gene' actually represents a group of real genes in a coarse-grained sense. The spirit in which such 'coarse-grained genes' are used in this model is somewhat similar to that of using the 'phenotypic' characters in the web-world model (Caldarelli *et al* 1998; Drossel *et al* 2001; Quince *et al* 2004a,b). The number of individuals of genotype I in generation t is $n_I(t)$; the total population is $N_{\text{tot}}(t) = \sum_I n_I(t)$.

In each generation, the genomes of the individual organisms are subjected to random mutation with probability μ/L per gene per individual where L is the total size of the genome. Thus, by working with the genomes, Rikvold and Zia account for the genetic mutations explicitly and use the genotypes to label the different species.

In order to keep the model as simple as possible, Rikvold and Zia assumed the successive generations to be nonoverlapping. More precisely, the organisms are incapable of living through successive reproduction cycles; an individual organism produces a litter of F offspring and immediately thereafter it dies. Consequently, this model does not describe age-structured populations of any species.

Rikvold and Zia (2003) considered a random food web where the effects of species j on the population of the species i is modelled by the element J_{ij} of the interaction matrix \mathbf{J} , exactly as in the Sole-Manrubia model (Sole and Manrubia 1996, 1997). In this model \mathbf{J} is taken to be a time-independent random matrix, with vanishing diagonal elements, whose off-diagonal elements are selected randomly from a uniform distribution over the interval $[-1, 1]$.

In each generation, the probability that an individual of genotype I produces a litter of F offspring before it dies is $P_I(\{n_I(t)\})$ whereas the probability that it dies without giving birth to offspring is $1 - P_I$. The reproduction probability P_I is assumed to be given by (Rikvold and Zia 2003).

$$P_I(\{n_J(t)\}) = \left\{ 1 + \exp \left[- \frac{\sum_J J_{IJ} n_J}{N_{\text{tot}}(t)} + \frac{N_{\text{tot}}(t)}{N_0} \right] \right\}^{-1}. \quad (2)$$

Here the second term in the exponential, commonly called the Verhulst factor, represents an environmental carrying capacity where N_0 is determined by the limited shared resources like, for example, space, water, light, etc.

The tangled nature model (Hall *et al* 2002; di Collobiano *et al* 2003) is slightly more general than the model studied by Rikvold and Zia (2003) because overlapping generations are allowed. An individual organism is removed from the system with a constant probability p_{kill} per time step. The algorithm used for reproduction probability in the tangled nature model is also slightly different from that used by Rikvold and Zia. However, to our knowledge, there is no *a priori* justification at present for preferring either of these.

In our works (Chowdhury and Stauffer 2003, 2004, 2005; Chowdhury *et al* 2003; Stauffer and Chowdhury 2004; Stauffer *et al* 2005), we have provided the most detailed description of the ecological as well as the evolutionary processes. We have incorporated not only the hierarchical architecture of the natural food webs in a simplified manner but also the emergence of this architecture through self-organization as well as the possibility of migration of populations from one 'patch' to another of the same eco-system for predation or merely for occupying a habitat.

We have modelled the eco-system as a dynamic hierarchical network (see figure 2). Each node of the network represents a niche, rather than a species. Each niche can be occupied by at most one species at a time. The 'micro'-evolution, i.e. the birth, growth (ageing) and natural

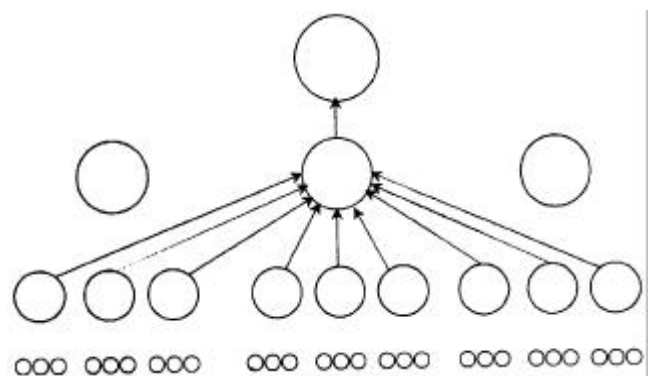


Figure 2. A schematic representation of the network model, with hierarchical foodweb architecture (Chowdhury and Stauffer 2003). The circles represent the niches in the eco-system. Each arrow represents direction of nutrient flow. All possible nutrient flows to the species occupying the second node at the second level and that occupying the highest level are shown explicitly.

death of the individual organisms, in our model is captured by the intra-node dynamics. The ‘macro’-evolution, e.g. adaptive co-evolution of the species, is incorporated in the same model through a slower evolution of the network itself over longer time scales. Moreover, as the model eco-system evolves with time, extinction of species is indicated by vanishing of the corresponding population; thus, the number of species and the trophic levels in the model eco-system can fluctuate with time. Furthermore the natural process of speciation is implemented by allowing re-occupation of the vacant nodes by mutated versions of non-extinct species.

The prey-predator interaction between two species that occupy the nodes i and k at two adjacent trophic levels is represented by J_{ik} ; the three possible values of J_{ik} are ± 1 and 0. The sign of J_{ik} indicates the direction of trophic flow, i.e. from the lower to the higher level. J_{ik} is $+1$ if i is the predator and k is the prey species and it is -1 if k is the predator and i denotes the prey. If there is no prey-predator relation between the two species i and k , we must have $J_{ik} = 0$. This formulation of the inter-species interactions is very similar to that in the Sole-Manrubia model (Sole and Manrubia 1996, 1997). Although there is no direct interaction between species at the same trophic level in our model, they can compete, albeit indirectly, with each other for the same food resources available in the form of prey at the next lower trophic level.

The elements of the matrix J account not only for the inter-species interactions (as in the Sole-Manrubia type models) but also for the intra-species interactions arising from the competition of individual organisms for the same food resources. In order to understand this interesting feature of the matrix J , consider now the two sums

$$S_i^\pm = \pm \sum_{j=1}^N \frac{(J_{ij}^\pm - J_{ji})}{2} n_j, \quad (3)$$

where the superscript \pm on J_{ij} indicates that the sum is restricted to only the positive (negative) elements J_{ij} . The sum S_i^+ is a measure of the total food currently available to the i th species whereas $-S_i^-$ is a measure of the total population of the i th species that would be, at the same time, consumed as food by its predators. If the food available is less than the requirement, then some organisms of the species i will die of starvation, even if none of them is killed by any predator. This way the matrix J can account for the shortfall in the food supply and the consequent competition among the organisms of the species i .

The intra-species competition among the organisms of the same species for limited availability of resources, other than food, imposes an upper limit n_{\max} of the allowed population of each species; n_{\max} is a time-independent

parameter in the model. Our model captures the starvation deaths and killing by the predators, in addition to the natural death due to ageing.

In our approach, each species is characterized by three features, namely, the minimum reproductive age A_{rep} , the maximum possible age A_{max} and the litter size M . An organism becomes mature enough for reproduction only on attaining the age A_{rep} ; beyond this age, the probability that it gives birth (simultaneously to M offsprings) varies with its age A . The probability of its death due to ageing is also a function of its age A but becomes a certainty on attaining the age A_{max} provided it survives till then evading its predators. Although these three characteristics of each species are reminiscent of the features of the species in the webworld model (Caldarelli *et al* 1998; Drossel *et al* 2001; Quince *et al* 2004a,b), in our model these features are not fixed parameters but are determined by self-organizing dynamics of the eco-system.

In the original version of our ‘unified’ model, we assumed that the population of the prey as well as that of predators are uniformly distributed in space. This situation is similar to a well-stirred chemical reaction where the spatial fluctuations in the concentrations of the reactants and the products is negligibly small. On the other hand, spatial inhomogeneities in the eco-systems and migration of organisms from one spatial ‘patch’ to another are known to play important roles in evolutionary ecology (Czaran 1998; Bascompte and Sole 1998; Tilman and Kareiva 1997). We have captured the spatial inhomogeneities of the populations and characteristics of the species from one patch to another by extending our ‘unified’ model on discrete lattices where each of the lattice sites represents different spatial ‘patches’ or ‘habitats’ of the eco-system (Stauffer *et al* 2005). Thus, the eco-system is a network of spatial ‘patches’ each of which is endowed with a food web; in other works, the eco-system is a network of networks (see figure 3).

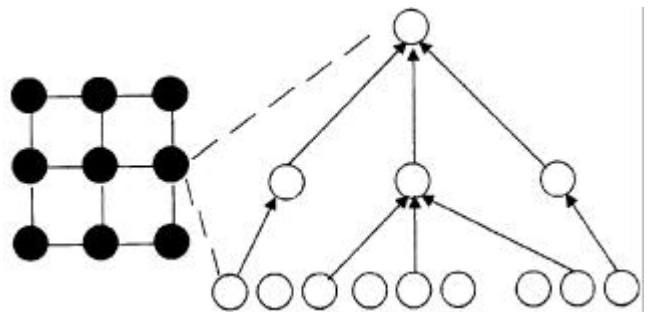


Figure 3. The eco-system is a network (represented schematically by the square lattice) of spatial ‘patches’ each node of which is endowed with a food web, another hierarchical network.

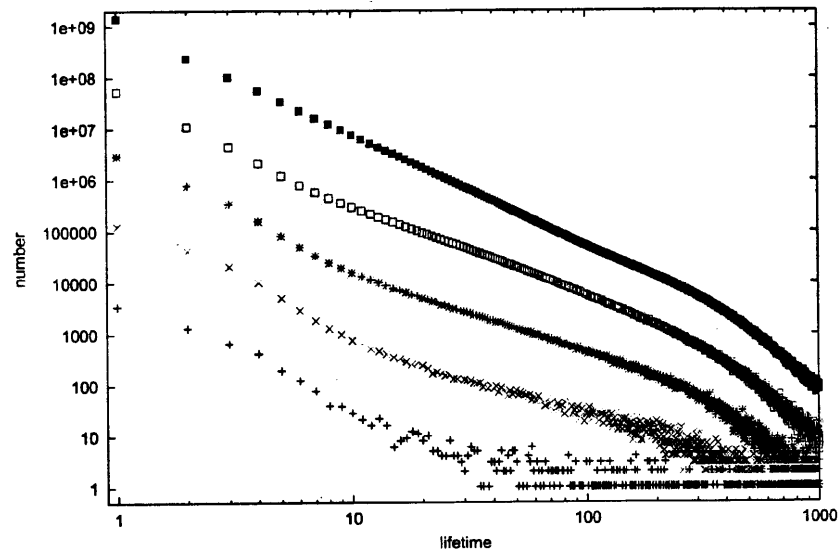


Figure 4. Distributions of the lifetimes of the species in the latest version of our ‘unified’ model of evolutionary ecology. The size of the eco-system is 5×5 in an appropriate dimensionless unit where each unit corresponds to a large patch. The lifetimes of the species are indicated along the X-axis whereas the number of times species with a given lifetime are encountered in our simulation, is plotted along the corresponding Y-axis. The symbols +, \times , *, open and filled squares correspond, respectively, to $t = 10^3$, 10^4 , 10^5 , 10^6 and 10^7 , where t is the time in dimensionless units (but, can be interpreted, for example, as one year) for which the ecosystem evolves following the dynamics of our model.

As an example, in figure 4 we show the distribution of the lifetimes of the species in the latest version of this model. Very recently it has been pointed out, through independent computer simulations by Singh and Ramaswamy (2004), that the deviation from power-law observed in the distributions of the lifetimes in the ‘unified’ model is not any artefact of the simplified strengths $J_{ij} = \pm 1$ but is a generic feature of the model with even more general interactions.

6. Conclusion

Field studies and laboratory experiments have convincingly established that evolutionary changes can take place in ecosystems over relatively short ecological time scales (Thomposn 1998a,b, 1999; Fussmann *et al* 2003; Stockwell *et al* 2003; Turchin 2003; Yoshida *et al* 2003). Motivated by these observations and because of the availability of sufficiently fast computers, several ‘unified’ models of evolutionary ecology have been developed over the last few years (Hall *et al* 2002; Chowdhury and Stauffer 2003, 2004, 2005; Chowdhury *et al* 2003; di Collobiano *et al* 2003; Rikvold and Zia 2003; Stauffer and Chowdhury 2004; Stauffer *et al* 2005). All of these models treat an ecosystem as a dynamically evolving net-

work of species. This modelling strategy is very similar to that followed for modelling complex adaptive systems, an active area of research in statistical physics. These models provide a ‘unified’ description of the ‘generic’ features of ecology and evolution-ecological changes, e.g. variation of populations of different species, take place over relatively short time scales while evolutionary changes, e.g. speciation and extinction occur slowly over longer time scales. In this paper we have critically reviewed the results of computer simulations of such ‘unified’ models of evolutionary ecology.

For the sake of completeness and to put the recent developments in the proper perspective, we have also mentioned briefly some earlier works, from simple to complicated models. Simple models have the advantage that they often give clear results with limited computational effort, like power laws for the distributions of lifetimes and avalanches of extinctions of species. Complicated models are usually more realistic but, because of the lack of the simplicity, these may give a superposition of several different laws in different regimes and require enormous computational efforts. Nevertheless, it has been possible not only to capture birth, ageing of individual organisms and the prey-predator interactions as well as extinctions and speciation but also the emergence of self-organized hierarchical architecture of the food webs. We

hope this critical review of the recent models published in the physics literature will stimulate interactions between physicists and evolutionary ecologists.

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