

# IRAS Low Resolution Spectrograph spectral class and M and S Miras

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**Summary.** A large sample of 177 M and S Miras, as revealed by their IRAS LRS spectral class, have been examined to determine the dependence of silicate emission on the visual light curve asymmetry factor,  $f$ . It is confirmed that  $9.7\ \mu\text{m}$  silicate emission feature not only in M but in S Miras also occurs only when  $f \leq 0.45$ . However, not all stars with  $f \leq 0.45$  show the silicate emission; this non-detection reveals dependence on other parameters like the mean visual light amplitude. Though strong emission feature in M Miras may occur for any value of  $f$ , very weak features are absent for small values of  $f$  and the strongest features tend to appear for larger values of  $f$ . Infrared excess tends to increase with the strength of the silicate emission as well as with decrease in the value of  $f$ . Probability of detection of silicate emission is very high for visual light curve classes (Ludendorff)  $\alpha_1$ ,  $\alpha_2$  and  $\alpha_3$ , decreases for  $\alpha_4$  and  $\gamma_1$ , and is negligible for  $\beta$  class.

**Key words:** stars: long period variables – stars: circumstellar matter – stars: visual light curve – stars: far infrared spectroscopy

## 1. Introduction

A large number of M spectral type Mira variables show strong silicate emission features at  $9.7$  and  $20\ \mu\text{m}$  among the Low Resolution Spectrograph (LRS) spectra obtained with the Infrared Astronomical Satellite (IRAS). Vardya et al. (1986) found that the  $9.7\ \mu\text{m}$  emission seems to occur only in the spectra of those Miras with visual light asymmetry factor  $f \leq 0.45$ ; here  $f$  is defined as the ratio of the number of days between minimum light and the next following maximum to the period. The main study was based on the visual inspection of the LRS spectra of 19 Miras, supplemented by an additional 27 Miras to check the conclusion. This has been extended by Onaka and de Jong (1987) by analysing the LRS spectra of 109 M Miras. Here, we have examined this earlier work of Vardya et al. (1988) but depart from it as well as the work of Onaka and de Jong (1987) by:

- (i) using IRAS LRS spectral class, rather than spectra itself, as given in the Point Source Catalogue, making the analysis somewhat quantitative;
- (ii) using all Mira variable stars, not only of M but of S spectral type also, which may possibly exhibit oxygen rich circumstellar chemistry, as determined by the IRAS LRS spectral classes 1n, 2n, 3n, 5n, 6n and 7n (Beichman et al., 1985), and having known value of  $f$ ; and
- (iii) using Ludendorff's visual light curve class also, besides the asymmetry factor  $f$ .

This sample thus comprises of 177 stars with 164 M and 13 S Miras.

## 2. Sample of stars

Among the objects with LRS spectral code, 1n, 2n, 3n, 5n, 6n and 7n, we have considered all the M and S Miras for which visual light asymmetry factor  $f$  is known (Kholopov, 1985). This gives a sample of 164 M Miras and 13 S Miras. We have not considered LRS class 0n, as they denote either very noisy spectra or strange band shape.

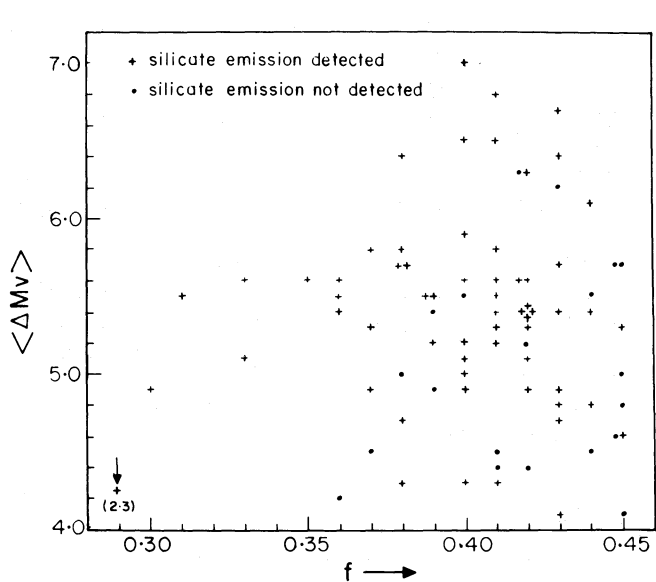
Table 1a gives the variable name of the star, period in days, visual light asymmetry factor  $f$ , spectral class, IRAS LRS spectral class, mean visual light amplitude (Kukarkin et al., 1969),  $\log S_{12}/S_{25}$ , and visual light curve class for M spectral type Mira variables; here  $S_{12}$  and  $S_{25}$  are the flux densities at 12 and  $25\ \mu\text{m}$ , respectively. Table 1b gives similar data for S Miras along with the NSS number from the S star catalogue of Stephenson (1984). The last column gives remarks if any. Flux densities of high quality (class 3) only have been included in the tables.

## 3. Results

Table 1 shows that the stars in our sample are equally divided among LRS classes 1n and 2n, with one star each in 3n and 5n, two in 6n class, and none in 7n. Except for five stars, all M Miras with LRS classes 2n and 6n have  $f \leq 0.45$ ; among the five exceptions (V845 Aql, X Ara, Z Sgr, IK Tau and S UMi), V845 Aql has the strongest silicate signature with LRS class 69 but its  $f$  value is uncertain, and the flux density low. The  $f$  value for IK Tau is from recent data and may not be a good average value. The remaining three stars have LRS class 21 or 22 i.e. weak silicate features. The spectra of X Ara and Z Sgr are rather noisy (Olson and Raimond, 1986), their flux density low, and the LRS class may or may not be a true indicator of silicate emission feature; the value of  $f$  for X Ara may be based on limited data. The very low values of  $\log S_{12}/S_{25}$  for V845 Aql, X Ara, and IK Tau are more appropriate for  $f \leq 0.43$ . In the fifth star, S UMi, the silicate feature is very weak, and the spectrum is an average of two spectra only. Note that the LRS classes 21 and 22 may reflect noise in some of the stars. Thus we see that this large data essentially confirms the result obtained by Vardya et al. (1986) that  $9.7\ \mu\text{m}$  silicate emission in M Miras is present only when  $f \leq 0.45$ . In rare cases, silicate feature may be present for  $f > 0.45$ , but a good case needs to be found for confirmation. Only one Mira (R Cha) has a LRS class 3n, i.e., 31, indicating  $9.7\ \mu\text{m}$  silicate absorption. This being a

very weak feature, we checked the LRS spectrum (Olson and Raimond, 1986) and found that it can be due to noise. However, not all M Miras with  $f \leq 0.45$  show  $9.7 \mu\text{m}$  silicate emission; in fact, about one fifth of these Miras have LRS class 1n. This non-detection can be due to (a) noisy spectra, (b) self absorption of the silicate feature, (c) blowing away or dissipation of the circumstellar shell, the seat of the emission feature or/and (d) dependence of this feature on parameters besides  $f$ . Examining the last possibility, we find that the maximum number of non-detection ( $\sim 60\%$ ) is in the region  $0.43 < f \leq 0.45$ , which is a kind of transition region, and for  $f < 0.36$ , all stars appear to have silicate emission feature. Further, non-detection of stars is as high as  $\sim 45\%$  for mean visual light amplitude,  $\langle \Delta M_V \rangle \leq 5^m0$  but decreases to  $\sim 18\%$  for  $\langle \Delta M_V \rangle > 5^m0$  (Fig. 1). Remember that for  $f < 0.36$ , silicate emission has been observed even from a star, DH Cyg, with  $\langle \Delta M_V \rangle = 2^m3$ .

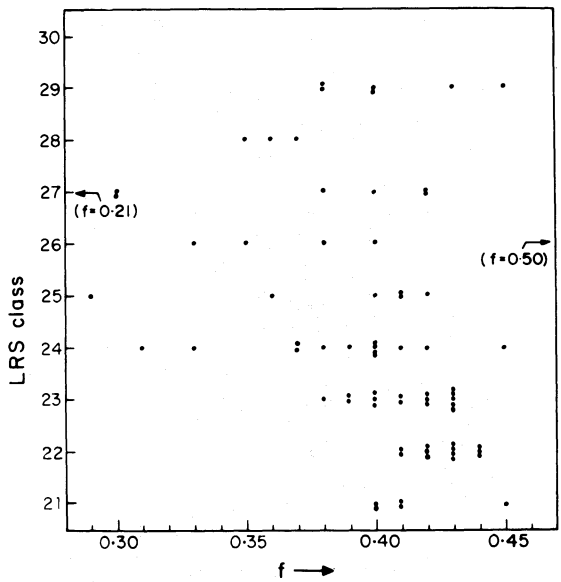
Whether RT Oph is a M spectral type star or a C star, is not certain; its spectral class, as given in Kholopov (1985) is M7e(C),



**Fig. 1.** The mean visual light amplitude vs.  $f$  for M Miras for stars with and without silicate emission features are marked plus (+) and dots (•)

but it is not in the Carbon Star Catalogue (Stephenson, 1973). Further, the  $f$  value of 0.19 for CH Pup, of 0.25 for AA Sct and of 0.5 for IK Tau may be wrong. Ignoring these four stars, if we plot the LRS spectral class (2 or 6) $n$  vs  $f$  for  $f \leq 0.45$ , we find (Fig. 2) that for LRS class (2 or 6) $n$ ,  $n \geq 4$  covers all stars with  $f < 0.37$ , but only two fifth of the stars with  $0.37 < f < 0.45$ , and for LRS class (2 or 6) $n$ ,  $n \geq 3$  covers all stars with  $f < 0.39$  but only two third stars with  $0.39 < f < 0.45$ . Further, the weakest (21, 22) and the strongest (29, 69) emission features have a tendency to appear for larger values of  $f$ . This implies that strong  $9.7 \mu\text{m}$  silicate emission can be present for any  $f \leq 0.45$ , but lower  $f$  values appears to have only strong silicate emission feature. However, all six stars with LRS spectral class (2 or 6) 9 have  $f \geq 0.38$ .

Figure 3 gives a plot of  $\log S_{12}/S_{25}$  vs.  $f$ . Here  $S_{12}$  and  $S_{25}$  are the observed fluxes at 12 and  $25 \mu\text{m}$  taken from the IRAS Point Source Catalogue. Plotted are mean values of  $\log S_{12}/S_{25}$  of stars with given  $f$ . The mean of 5 or more points is shown by a circle, and of 4 stars by a square. The extent of variation at a given  $f$



**Fig. 2.** Plot of IRAS LRS spectral class vs.  $f$  for M Miras. Note that LRS class 29 includes LRS class 69 stars

**Table 1a.** Data for M spectral type Miras

Star name	Period (day)	$f \times 10^2$	Spectral type	LRS class	$\langle \Delta M_V \rangle$	$\log S_{12}/S_{25}$	l.c.c. (55)	Remarks
U And	347	41	M6e	15	4.4	0.349	$\alpha_3$	
SV	316	38	M5e-7e	16	5.0	0.411	$\alpha_2$	7
TU	317	48	M5e	15	4.0	0.430	—	1
W Aqr	381	42	M6e-8e	22	5.3	0.403	$\alpha_3$	
Y	382	43	M6.5e-9	23	5.4	0.367	$\alpha_2$	
R Aql	284	42	M5e-9e	23	5.4	0.216	$\alpha_4$	137
RR	395	30	M6e-9	27	4.9	0.343	$\alpha_3$	3
RS	410	48	M5e-8	14	5.5	0.432	$\alpha_2$	
RT	327	42	M6e-8e(S)	24	5.6	0.324	$\alpha_3$	3
SY	356	37	M5e-7e	28	4.9	0.300	$\alpha_3$	56
V845	229	50:	—	69	—	0.168	—	

Table 1a (continued)

Star name	Period (day)	$f \times 10^2$	Spectral type	LRS class	$\langle \Delta M_v \rangle$	$\log S_{12}/S_{25}$	l.c.c. (55)	Remarks
X Ara	176	51	M5e-7eII-III	22	—	0.284	—	
U Ari	371	40	M4e-9.5e	21	6.5	0.431	$\alpha_2$	4
R Aur	458	51	M6.5e-9.5e	15	5.6	0.399	$\gamma_1$	12
U	408	39	M7e-9e	23	5.5	0.324	$\alpha_2$	5
RU	466	40	M7e-9e	25	4.9	0.279	$\alpha_1$	6
SZ	454	46	M8e	15	—	0.397	—	
R Boo	223	46	M3e-8e	14	5.1	0.361	$\beta_1$	
RT	274	49	M6.5e-8e	15	4.5	0.374	—	
R Cae	391	41	M6e	23	5.2	0.371	$\alpha_2$	
V Cam	522	31	M7e	24	5.5	0.285	$\alpha_2$	45
R Cnc	362	47	M6e-9e	15	4.4	0.430	$\alpha_4$	4
W	393	40	M6.5e-9e	23	5.9	0.294	$\alpha_3$	
R CVn	329	46	M5.5e-9e	15	4.2	0.404	$\beta_2$	1
S CMi	333	49	M6e-8e	15	5.1	0.402	$\beta_1$	
V Cap	276	42	M5e-8.2	27	—	0.169	$\alpha_2$	
RU	347	36	M9e	28	5.4	0.189	$\alpha_3$	2
R Car	309	48	M4e-8e	15	5.0	0.445	$\beta_1$	245
S	149	51	K5e-M6e	17	2.8	0.509	$\beta_3$	
Z	384	37	M6e	15	4.5	0.372	$\alpha_3$	
RV	366	39	M6e	14	4.9	0.356	$\gamma_1$	
RW	319	47	M4e-7e	15	5.7	0.388	$\alpha_3$	
RZ	273	42	M4e-8e	25	5.4	0.385	—	
R Cas	430	40	M6e-10e	24	5.6	0.383	$\gamma_1$	3467
T	445	56	M6e-9.0e	15	4.0	0.381	$\gamma_1$	47
V	229	48	M5e-8.5e	16	4.3	0.436	$\beta_2$	
Y	413	43	M6e-8.5e	22	4.7	0.319	$\alpha_2$	3
RV	332	38	M4.5e-9.5e	23	5.8	0.318	$\gamma_1$	
MP	338	50	M8	51	—	-0.805		7
W Cen	202	47	M3e-8(III)e	15	4.7	0.381	$\beta_1$	
X	315	41	M5e-6.5e	23	5.4	0.416	$\alpha_4$	
RT	255	47	M6II:e	15	3.7	0.418	$\beta_3$	1
RX	328	38	M5e	15	—	0.318	$\alpha_2$	
TW	269	43	M4e-8II:	22	—	0.440	—	
T Cep	388	54	M5.5e-8.8e	15	4.3	0.452	$\gamma_1$	14
X	535	42	M4.5e-7e	23	6.3	0.311	$\alpha_2$	6?
Y	333	40	M5e-8.2e	14	5.5	0.410	$\alpha_3$	
RR	384	41	M5e-8.8e	14	4.5	0.314	$\alpha_2$	
R Cet	166	43	M4e-9	29	4.9	0.134	$\alpha_4$	
R Cha	335	41	M4e-7e	31	5.1	0.436	$\alpha_4$	
R Col	328	39	M3e-7	15	5.4	0.301	$\alpha_1$	
S	326	46	M6e-8	14	4.5	0.354	$\alpha_3$	
T	226	50	M3e-6e	16	4.4	0.427	$\beta_2$	4
R Com	363	38	M5e-8ep	24	5.7	0.277	$\alpha_2$	6
S CrB	360	33	M6e-8e	24	5.6	0.204	$\alpha_2$	3
Z Cyg	264	45	M5e-9e	69	4.6	0.083	$\alpha_2$	567
SX	411	41	M7e	21	5.3	0.340	$\alpha_2$	
TW	341	48	M6.5-10ep	16	4.5	0.408	$\alpha_4$	
UX	565	40	M4e-6.5e	29	—	0.228:	$\alpha_1$	13
BG	288	50	M7e-8e	15	—	0.423	—	1
DH	528	29	M6	25	2.3	0.185	—	6?
KZ	406	45	M8e	21	—	0.352	—	
R Del	285	45	M5e-6e	15	5.0	0.417	$\alpha_4$	
S	278	52	M5e-8	16	3.2	0.413	$\beta_2?$	27
V	534	42	M4e-6e	22	5.4	0.170	$\alpha_1$	

Table 1a (continued)

Star name	Period (day)	$f \times 10^2$	Spectral type	LRS class	$\langle \Delta M_v \rangle$	$\log S_{12}/S_{25}$	l.c.c. (55)	Remarks
Y Del	468	43	M8e	23	4.1	0.222	$\alpha_1$	
R Dra	246	45	M5e-9eIII	16	4.8	0.390	$\alpha_4$	
U	316	47	M6e-8	15	4.3	0.406	$\beta_1$	1
Y	326	45	M5e	24	5.3	0.397	$\alpha_2$	
T Eri	252	45	M3e-5e	16	4.8	0.452	$\alpha_4$	
W	377	40	M7e-9	24	5.2	0.362	$\alpha_3$	3
RT	371	46	M7e	15	—	0.407	—	
S Gem	293	42	M4e-8e	17	5.2	0.399	$\alpha_3$	2
X	264	49	M5e-8e(Tc)	17	5.0	0.412	$\beta_2$	
R Gru	332	42	M5e-7II-IIIe	15	6.3	0.374	$\alpha_4$	
S	402	43	M5e-8IIe	22	6.7	0.349	$\gamma_1$	
U Her	406	40	M6.5e-9.5e	23	5.0	0.445	$\gamma_1$	3
RU	485	43	M6e-9	23	5.7	0.344	$\gamma_1$	47
R Hor	408	40	M5e-8eII-III	24	7.0	0.370	$\alpha_3$	13
R Hya	389	49	M6e-9eS(Tc)	15	5.0	0.434	$\gamma_1$	1247
S	257	49	M4e-8e	16	4.9	0.481	$\beta_3$	
T	299	49	M3e-9:e	16	4.8	0.458	$\beta_3$	1
X	301	42	M7e-8.5e	15	4.4	0.406	$\alpha_3$	3
RS	339	45	M6e	14	4.1	0.380	$\beta_1$	1
RU	332	35	M6e-8.8e	26	5.6	0.299	$\alpha_2$	156
S Ind	400	41	M6e-M8eII-Ib	22	6.8	0.231	$\alpha_2$	
Y	304	52	M6(II)e-7e	14	—	0.392	—	
R LMi	372	41	M6.5e-9.0e(Tc)	24	5.5	0.384	$\alpha_4$	3
T Lep	368	47	M6e-9e	15	4.6	0.282	$\beta_1$	4
RR Lib	277	47	M4e-8e	15	5.6	0.450	$\alpha_2$	1
RS	218	48	M4e-8.5e	15	4.5	0.458	$\beta_2$	1
RU	317	46	M5e-6e	17	5.9	0.436	$\alpha_4$	1
R Lup	236	48	M5e	14	4.0	—	—	
Y	397	37	M7e	24	5.3	0.275	$\alpha_2$	1
RW	197	36	Mb	15	—	0.284	—	
U Lyn	434	42	M7e-9.5e	27	4.9	0.371	$\gamma_1$	156
V Lyr	374	33	M7e	26	5.1	0.206	$\alpha_2$	6
RW	504	38	M7e	27	4.3	0.107	$\alpha_1$	56
U Mic	334	39	M5e-7e	24	5.2	0.274	$\alpha_2$	56
V Mon	341	46	M5e-8e	16	6.1	0.466	$\alpha_4$	1
FX	429	35	M1-8	28	—	0.335	—	6
T Nor	241	41	M3e-6e	25	5.8	0.329	$\alpha_4$	1
R Oct	405	44	M5.5e	15	4.5	0.325	$\alpha_2$	
S	259	42	M4(II)e-5e	22	5.1	0.380	$\alpha_4$	
U	308	47	M4e-6(II-III)e	16	5.7	0.411	$\beta_2$	1
R Oph	307	45	M4e-6e	16	5.7	0.454	$\alpha_4$	1
T	367	36	M6.5e	15	4.2	0.367	$\alpha_2$	
X	329	53	M5e-9e	15	2.0	0.447	$\beta_1$	12
RR	292	46	M3e-7	15	5.7	0.456	$\alpha_4$	1
RT	426	36	M7e(C)	22	5.5	0.339	$\alpha_2$	156
SS	181	47	M5e	16	4.8	0.462	$\beta_1$	1
S Ori	414	48	M6.5e-9.5e	15	4.5	0.374	$\beta_1$	124
U	368	38	M6e-9.5e	26	5.7	0.420	$\alpha_3$	13
BK	354	50	M7e	16	—	0.448	—	1
W Pav	283	40	M4e-7e	24	5.1	0.316	$\alpha_4$	
P Peg	378	44	M6e-9e	22	5.4	0.398	$\alpha_3$	13
Z	335	50	M6e-8.5e(Tc)	15	4.8	0.376	$\beta_2$	1
RV	397	38	M6e	29	4.7	0.235	$\alpha_2$	17
SW	396	42	M4e	16	—	0.371	—	
TU	322	45	M7e-8e	15	—	0.347	—	1

Table 1a (continued)

Star name	Period (day)	$f \times 10^2$	Spectral type	LRS class	$\langle \Delta M_v \rangle$	$\log S_{12}/S_{25}$	l.c.c. (55)	Remarks
PZ Per	396	21	M8	27	—	0.223	—	
S Pic	428	36	M6.5e-8e(II-III)	25	5.7	0.338	$\alpha_2$	16
R Psc	345	44	M3e-6e	22	6.1	0.343	$\alpha_3$	1
S	405	42	M5e-7e	23	5.4	0.358	$\alpha_2$	1
U Pup	318	41	M5e-8e	25	4.3	0.235	$\alpha_2$	1
Z	509	38	M4e-9e	29	6.4	0.301	$\alpha_1$	13
RW	341	47	M3e-6e	17	—	0.424	—	1
AS	325	50	M7e-9	15	3.2	0.403	—	1
CH	506	19	Me	23	—	0.285	—	17
R Ret	278	48	M4e-7.5e	15	5.7	0.437	$\alpha_4$	1
KK Sge	438	40	M7	29	—	0.231	—	
NO	345	50	M5	15	—	0.402	—	
PT	530	40	M10	26	—	0.333	—	7
PV	435	60	M6	15	—	0.422	—	
R Sgr	270	46	M4e-6e	16	5.2	0.490	$\beta_2$	1
Z	450	47	M4e-6(Se)	22	7.4	0.354	$\alpha_2$	7
RR	336	43	M4e-9e	23	6.4	0.418	$\alpha_4$	156
RT	306	47	M5e-7e	16	6.3	0.451	$\alpha_4$	1
RU	240	43	M3e-6e	23	5.6	0.405	$\alpha_4$	1
RV	316	47	M4e-9	16	6.3	0.451	$\beta_1$	1
SW	290	51	M5e-8	15	—	0.410	$\beta_1$	1
Z Sco	343	49	M5.5e-7e	16	4.2	0.422	$\beta_1$	1
RU	371	54	M7II-IIIe	16	4.0	0.447	$\gamma_1$	1
RW	389	40	M5e	27	—	0.244	$\alpha_2$	3
S Scl	363	48	M3e-9e (Tc)	15	6.2	0.435	$\gamma_1$	15
AA Sct	265	25	M4-6	14	—	0.438	—	7
R Ser	356	41	M5IIIe-9e	22	6.5	0.430	$\alpha_4$	145
S	372	43	M5e-6e	22	4.8	0.371	$\gamma_1$	13
R Tau	321	41	M5e-9e	21	5.6	0.287	$\gamma_1$	13
RX	332	47	M6e-7e	15	4.4	0.374	$\alpha_4$	156
IK	470	50	M6e-10e	26	—	0.290	—	37
R Tel	462	43	M5IIe-7e	15	6.2	0.393	$\gamma_1$	
R Tri	267	44	M4IIe-8e	16	5.5	0.464	$\beta_2$	15
R UMa	302	39	M3e-9e	23	5.5	0.235	$\alpha_3$	5
S UMi	321	50	M6e-9e	21	3.6	0.393	$\beta_2$	1
W Vel	395	44	M5-8IIIe	22	4.8	0.378	$\alpha_3$	16
Y	450	40	M8e-9.5	23	4.3	0.314	$\alpha_1$	1
Z	411	46	M9e	15	5.3	0.405	$\gamma_1$	1
RS	410	40	M7e	21	—	0.346	—	1
RW	443	50	M7III (II)e	15	—	0.387	—	1
R Vir	146	50	M3.5IIIe-8.5e	17	4.6	0.452	$\beta_2$	14
S	375	45	M6IIIe-9.5e	16	5.7	0.391	$\alpha_4$	145
RS	354	37	M6III-8e	24	5.8	0.221	$\alpha_3$	13
S Vol	395	54	M4e	16	5.0	0.422	$\beta_1$	1

## Remarks to Table 1

1: period varies, 2: visual binary, 3: H<sub>2</sub>O, OH, SiO maser/emission, 4: SiO maser, 5: H<sub>2</sub>O maser, 6: OH maser/emission, 7: see special note below.

## Special notes

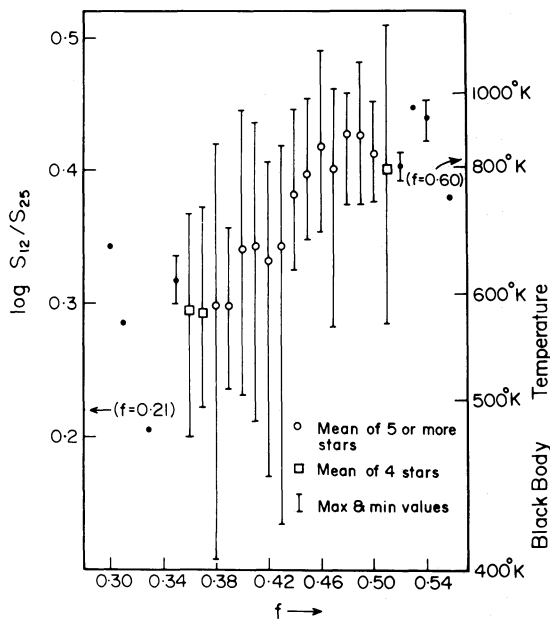
Table 1a: SV And – maximum magnitude varies periodically; R Aql – radio bursts; R Cas – sometimes H<sub>2</sub>O emission; T Cas – ZrO bands in the IR region; MP Cas – in the nebula NGC 7635 and its  $\log S_{12}/S_{25}$  too small; Z Cyg – its  $\log S_{12}/S_{25}$  is too low; RU Her – composite spectrum at minimum (a companion ?); R Hya – not in Stevenson (1984); RV Peg – magnitude at maximum varies by more than 3<sup>m</sup>; CH Pup –  $f$  value, if correct, is the lowest; PT Sge –  $p$  component of a close binary; Z Sgr – not in Stevenson (1984); AA Sct – its period is 153 days and  $f=0.43$  according to Kukarkin et al. (1969): this value of  $f$  will match better with its value of  $\log S_{12}/S_{25}$ ; IK Tau – the value of  $\log S_{12}/S_{25}$  is rather low and is more appropriate for  $f \leq 0.43$ , unless affected by other conditions.

**Table 1b.** Data for S spectral type Miras

Star name	NSS no.	Period (days)	$f \times 10^2$	Spectral class	LRS class	$\langle \Delta Mv \rangle$	$\log S_{12}/S_{25}$	l.c.c. (55)	Remarks
W And	49	396	42	S6, 1e-9, 2e	22	6.3	0.366	$\alpha_3$	
X And	6	346	37	S2, 9e-5, 5e	16	5.8	0.400	$\alpha_3$	
RW And	14	430	36	S6, 2e	22	6.1	0.290	$\alpha_2$	
W Aql	1115	490	37	S3, 9e-6, 9e	22	5.7	0.372	$\alpha_2$	7
T Cam	103	373	47	S4, 7e-8.5, 8e	17	5.8	0.539	$\gamma_1$	7
S Cas	28	612	43	S3, 4e-5, 8e	22	5.1	0.243	$\gamma_1$	
W Cet	1346	351	50	S6, 3e-9, 2e	16	6.8	0.525	$\gamma_1$	7
R Cyg	1150	426	35	S2.5, 9e-6, 9e (Tc)	22	6.4	0.304	$\alpha_3$	2
R Gem	307	370	36	S2, 9e-8, 9e(Tc)	16	6.4	0.457	$\alpha_4$	27
R Lyn	283	379	44	S2.5, 5e-6, 8e:	16	5.9	0.502	$\alpha_4$	
RR Mon	326	395	39	S7, 2e-8, 2e	16	5.6	0.363	$\alpha_2$	1
ST Sgr	1096	395	44	S4, 3e-9, 5e	21	6.2	0.431	$\alpha_1$	
RT Sco	954	449	39	S7, 2	22	9.0:	0.380	$\alpha_2$ :	

*Table 1b:* W Aql – composite spectrum near minimum, a companion (F5-8) may exist; T Cam – spectrum resembles class R(HD catalogue); W Cet –  $f$  value from Kukarkin et al. (1969); R Gem – spectrum resembles class R (HD catalogue)

value is indicated by the line bracketing the extreme values at that value of  $f$ ; partly, this range may be due to difference in phases at which observations were made, besides other variations among individuals stars. We have excluded Z Cyg, MP Cas and IK Tau in averaging as their values are too low compared to other stars of similar  $f$ . Hence using mean values at each value of  $f$  is preferable to derive any conclusion, rather than individual values. We have preferred to use fluxes observed by IRAS itself rather than taking



**Fig. 3.** Plot of flux density ratio,  $\log S_{12}/S_{25}$ , at 12 and 25  $\mu\text{m}$  from IRAS against  $f$  values for M Miras. Circles denote average of 5 or more stars and squares of 4 stars. The vertical lines give the extreme range for a given value of  $f$ . Black body temperature is given on the left. Z Cyg, MP Cas and IK Tau have not been included in averaging; see text for the reasons

one of the near-IR wavelengths like 2.2  $\mu\text{m}$  or 3.6  $\mu\text{m}$  for the colour index to ensure that the fluxes going into the colour index determination correspond to the same phase for a given star. The figure shows that  $\log S_{12}/S_{25}$  has a tendency to increase as  $f$  increases; i.e. the emission is from grains at higher temperature for stars with higher value of  $f$ . This implies that the circumstellar shell, where the grains are centred, is located farther out from the stellar surface when  $f$  is small than when  $f$  is large. The problem is complex but can be qualitatively understood if  $f$  is inversely correlated to the strength of the outward shock (cf Vardya et al., 1986). A stronger shock drives the grains farther out from the surface than a weaker shock, thus giving rise to cooler grains when  $f$  is small than when  $f$  is large. Whether this is really so requires detailed calculations of shock propelled circumstellar shell with condensation chemistry.

The mean values of  $\log S_{12}/S_{25}$  appear to cluster around three values, 0.3, 0.34 and 0.4. If this is not due to selection effect, this may be due to the composition and size distribution of grains for stars with different values of  $f$ . It appears that the mean value of  $\log S_{12}/S_{25}$  reaches a peak at  $f=0.48$  and decreases thereafter as  $f$  increases. Whether this is statistical or real is difficult to say as the number of stars with  $f \geq 0.51$  are very few.

Note that even the largest value of  $\log S_{12}/S_{25}$  in Fig. 3 corresponds to a black body colour temperature of about 1000 K, and if the grains have an emissivity proportional to  $1/\lambda$ , then to grain temperature of 500 K or less; hence grains exist even when silicate emission is absent.

Figure 4 gives a plot of mean values of  $\log S_{12}/S_{25}$  vs the LRS spectral class. The point at LRS class 29 includes two stars with LRS class 69, as objects of class  $m=6$  are qualitatively similar to that of  $m=2$  (cf Gal et al., 1987). The circles are mean of 6 or more stars, the pentagon for LRS class 26 for 5 stars and the triangle for 28 is mean of 3 stars only. The figure shows that  $\log S_{12}/S_{25}$  decreases as the strength of silicate emission band, represented by the second digit ( $n$ ) of the LRS class, increases, if we join the mean of 6 or more points. Note that the point for LRS=26 shifts very close to the mean curve if U Ori is neglected; the value  $\log S_{12}/S_{25}$



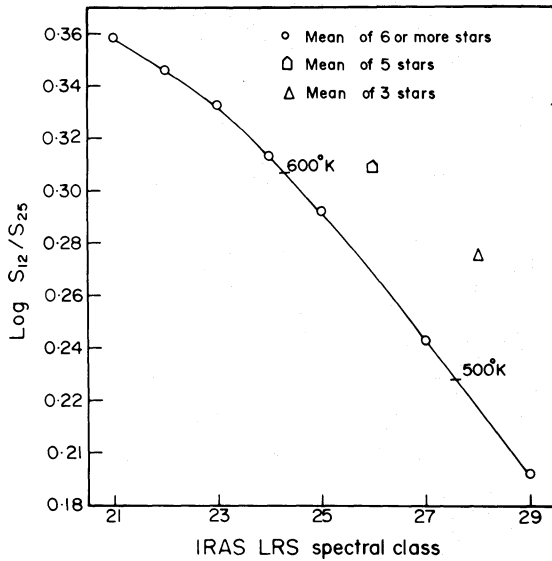


Fig. 4. Plot of mean flux density ratio,  $\log S_{12}/S_{25}$  vs. LRS spectral class. Circles denote mean of 6 or more stars, pentagon for 5 stars, and triangles of 3 stars. Solid line is a free hand curve of average values of 6 or more stars. The horizontal bars denote black body temperature

for this star is very large for this LRS class. This essentially implies that, on the average, the circumstellar dust temperature is lower for stars with stronger  $9.7 \mu\text{m}$  silicate emission. No correlation was found for  $\log S_{60}/S_{25}$  vs.  $\log S_{12}/S_{25}$  or LRS class.

If one looks at the light curves, one finds that it is not always easy to determine the  $f$  value. Besides, using  $f$  value implies that the shape of light curves are similar except for the steepness of the ascending branch. This is of course not true. Though  $f$  value has been found to be a useful parameter, it is worth examining the probability of detecting silicate emission based on the shape of the light curve. We will use the Ludendorff's classification, which is partly based on the steepness of the ascending branch of the light curve. In Table 1, visual light curve class (l.c.c. 55), as given by Vardya (1988), is also given. Figure 5 gives the probability of detection of silicate emission in a sample of 131 stars. The highest probability of 88% is for  $\alpha_1$  stars, and decreases to 42% for  $\alpha_4$  class stars. The detectability is essentially zero for  $\beta_1$ ,  $\beta_2$  and  $\beta_3$  stars but for  $\gamma_1$  stars it is 47%. There are no stars with  $\beta_4$  and  $\gamma_2$  class in our sample. However, the two  $\gamma_2$  stars in the sample of Vardya (1988), both show silicate emission, with LRS spectral class 22 and 23. Silicate emission feature strength, as measured by the second digit ( $n$ ) of the LRS spectral class is on the average, highest for the  $\alpha_1$  class ( $n = 5.4 \pm 2.9$ , 7 stars), decreases (to  $n \approx 4 \pm 2.2$ ) for ( $\alpha_2$ ,  $\alpha_3$ ,  $\alpha_4$ )-classes, and is lowest for the  $\gamma_1$  class ( $n = 3.1 \pm 1.3$ , 8 stars). The fact that the probability of detection and the variation of average strength of silicate emission is similar but different than the detection of  $1.35 \text{ cm H}_2\text{O}$  line in M Miras (Vardya, 1987) is perhaps a reflection of their origin. Silicate emission strongly depends on the steepness of the ascending branch of the light curve.

The mean values of  $\log S_{12}/S_{25}$  are smaller for M Miras with silicate emission (LRS Spectral class  $2n$  and  $6n$ ) than without it for visual light curve classes  $\alpha_1$ ,  $\alpha_2$ ,  $\alpha_3$ ,  $\alpha_4$  and  $\gamma_1$ . The difference can be as large as 0.08. Though the number of stars are small in a few

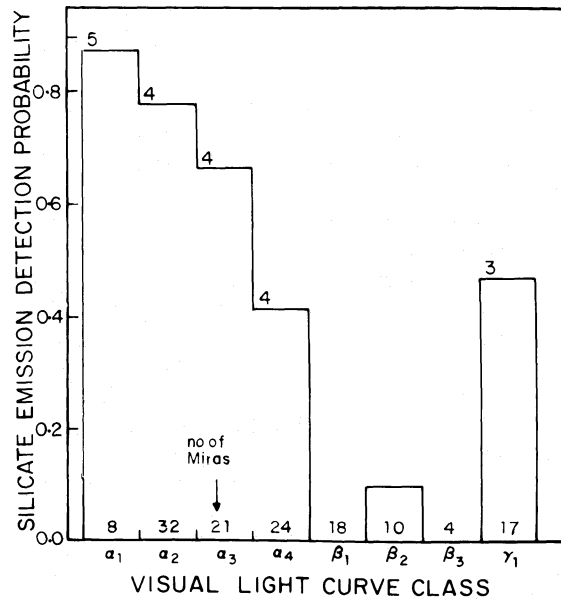


Fig. 5. Detection probability for silicate emission in M Mira variables for different visual light curve classes (Ludendorff). The number of stars in each visual light curve class is given at the bottom. The numbers at the top give mean value of the strength of the silicate emission feature as measured by  $n$  of LRS spectral class  $mn$

cases, this indicates that the far infrared colour temperatures of the circumstellar shells around M Miras is lower by about  $\sim 100\text{--}150 \text{ K}$  for stars with silicate emission than without it. Further, mean value of  $\log S_{12}/S_{25}$  is the smallest for  $\alpha_1$  class and increases as we proceed to  $\alpha_2$ ,  $\alpha_3$ ,  $\alpha_4$  and  $\gamma_1$  classes. Thus, the value of  $\log S_{12}/S_{25}$  anticorrelates with the strength of the silicate emission as well as with the probability of detecting silicate emission.

Table 1b for S Miras follow M stars in the sense that all seven LRS class  $2n$  stars have  $f \leq 0.45$  though two stars with  $f \leq 0.45$  have LRS class  $1n$  also. All S Miras with LRS class  $2n$  have weak silicate emission as  $n$  is either 1 or 2; this is not surprising as elemental abundance ratio oxygen/carbon is very close to unity in the photosphere of these stars and in all probability in the circumstellar shell as well and hence not very conducive to formation of silicates. It is possible that condensates formed in these stars have slightly different composition and structure, and hence have peak slightly away from  $9.7 \mu\text{m}$ , or have a broad shallow feature, resulting in weak features in LRS  $2n$  classification (cf. Little, Little-Marenin and Price 1987). It is, however, surprising that not a single S Mira show strong silicate feature, indicating remnant M phase shell when even a C Mira, RV Cen shows it (Little-Marenin and Wilton 1986). This may imply a gradual change from M to S phase.

#### 4. Discussion and conclusions

We have found here that IRAS LRS spectral class is useful in deriving statistical properties, though it is no substitute for detailed analysis using spectra itself (cf. Onaka and de Jong, 1987). Using it, we have confirmed the findings of Vardya et al. (1986), that only those M Miras show silicate emission which have

$f \leq 0.45$ ; however, there are M Miras with  $f \leq 0.45$  which do not show silicate emission. Though strong emission features are present for all values of  $f$ , Miras with  $f \leq 0.37$  exhibiting silicate emission correspond to LRS class (2 or 6)4 or stronger only. Alternatively, it is found that M Miras with visual light curve class  $\alpha_1$  has the highest probability of showing silicate emission feature and decreases gradually as we go to  $\alpha_2$ ,  $\alpha_3$ , and  $\alpha_4$  visual light curve classes; average strength of the silicate feature is highest for  $\alpha_1$  class stars and somewhat lower for  $\alpha_2$ ,  $\alpha_3$ , and  $\alpha_4$ . This can be understood qualitatively in terms of the explanation given in Vardya et al. (1986) assuming steepness of the ascending branch of the visual light curve being a measure of the shock strength, produced by pulsation, which drives the mass loss in these stars resulting in complete freezing of the condensation close to the surface of the star. The fact that some M Miras with  $f \leq 0.45$  do not show silicate emission may indicate its dependence on other parameters; one of them may be mean visual light amplitude. What these parameters are and how their combination work needs to be investigated. A quantitative treatment of pulsation, shock waves, and condensation chemistry is essential for proper understanding.

S Miras have elemental abundance ratio  $O/C > 1$  but very close to unity and are therefore akin to M stars. The fact that S stars follow the same trend as M Miras is therefore understandable.

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