## THE SPECTRUM OF NU ERIDANI\*

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## ABSTRACT

Observations in 1953–1954 confirm de Jager's and our own interpretation of our previous velocity-curves. The new results show that the absorption lines tend to be sharpest on the ascending branch near minimum and broadest on the descending branch near maximum. Three cycles show pronounced departures from the velocity-curves predicted on the basis of two interfering harmonic oscillations. There are some indications that, in addition to  $P_1 = 0$  1779 day and  $P_2 = 0$  1735 day, there is a third period,  $P_3 = 0$  064 day and  $K_3 = 5$  km/sec.

In a previous paper Struve *et al.* (1952) discussed the radial-velocity observations of  $\nu$  Eridani over a period of about fifty years. A beat phenomenon was detected, and a beat period of 6.9808 days was found to represent the observations fairly well. However, it was difficult to ascertain the exact beat period because of irregular variations in the smaller amplitude,  $K_1$ . The following periods and amplitudes were obtained:

$$P_1 = 0.1779 \text{ day}$$
,  $K_1 = < 8-15 \text{ km/sec}$ ,  $P_2 = 0.1735089 \text{ day}$ ,  $K_2 = 24.5 \text{ km/sec}$ .

C. de Jager (1953) tried to separate the dominant variation by constructing a mean curve for the period  $P_2 = 0.1735089$  day. The residuals could then be combined to form a mean curve with period  $P_1 = 0.1779$  day. These two periods represented the variation of radial velocity as well as of magnitude. They confirmed the previous value of the beat period, viz., 6.9808 days. The mean values of  $K_1$  and  $K_2$  were 10.6 and 20.2 km/sec, respectively.

The present observations confirm these results. But the radial velocity-curves show more complicated shapes, perhaps because of the greater dispersion used in the current work. It seems that the observations cannot be interpreted as a combination of two pure sine-curves.

All the measured spectrograms were obtained during 1953–1954 by Struve (on five nights) with the 100-inch coudé spectrograph of the Mount Wilson Observatory (designated "Cd") and by McNamara (on two nights) with the Mills three-prism spectrograph and the three-prism combination spectrograph with the 12-inch camera of the Lick Observatory (designated "LS"). The coudé plates taken on October 24, 1953, September 19, 1954, and November 18, 1954, have a dispersion of 4.5 A/mm, and the Lick plates taken on October 14, 1954, have a dispersion of 25 A/mm. The rest of the plates have a dispersion of 10 A/mm. The lines which were measured are listed in Table 1.

The observed radial velocities and phases, calculated from maximum radial velocity, are given in Table 2 and are plotted in Figure 1. The observed and calculated minima and maxima, and the differences (O - C) are given in Table 3. They were obtained from:

Minimum = 
$$2423709.816 + 0.1735089E$$
;  
Maximum =  $2433965.857 + 0.1735089E$ .

The differences (O - C) for the minima are small (except for October 14, 1954) and show that the period  $P_2 = 0.1735089$  is correct. The differences (O - C) for the maxima

\* The observational material used in this paper was obtained at Mount Wilson and Lick Observatories by O. Struve and D. H. McNamara, respectively.

are systematically negative except for October 21, 1954. In order to see whether this was due to the beat phenomenon, theoretical differences (O - C) were calculated for the three pairs of values of  $K_1$  and  $K_2$ , already given, by means of the formula (Struve 1950):

$$\phi = \tan^{-1} \left\{ \frac{K_1 \sin \phi}{K_2 + K_1 \cos \phi} \right\}.$$

Upon fitting these curves with the differences (O - C) for the present observations, as well as the observations of 1951–1952, it seems that the epoch of the maximum can be changed by  $8 \times 10^{-3}$  days to 2433965.849 (Fig. 2). But even after making this change, many of the points lie considerably off any of the curves.

In order to verify the beat period, the observed values 2K, given in Table 4, were plotted against the phases of the beat period. Figure 3, which contains these points, as well as three theoretical curves, shows that the estimated period of 6.9808 days is fairly accurate. But it appears that  $K_1$  and to some extent  $K_2$  are irregularly variable. This and the scatter of points in Figure 2 indicate that the oscillations involved are not simple

TABLE 1
LIST OF MEASURED LINES

Wave Length	Identification	Plate*	Wave Length	Identification	Plate*
3964 73	Не 1	Cd	4349 43	0 11	$Cd, LS_2$
3973 26	<i>O</i> 11	Cd	4387 93	He I	$Cd$ , $LS_2$
4026 19	He I	Cd	4414 91	0 11	$Cd, LS_2$
4072 16	O II	$\operatorname{Cd}$	4416 98	0 11	$Cd, LS_2$
4075 87	<i>O</i> 11	$\operatorname{Cd}$	4471 48	He I	$Cd$ , $LS_2$ , $LS_3$
1101 74	$H\delta$	$\operatorname{Cd}$	4481 23	Mg II	$Cd$ , $LS_2$ , $LS_3$
4119.22	On	$\operatorname{Cd}$	4552 65	SiIII	$Cd$ , $LS_2$ , $LS$
4120 81	He I	$\operatorname{Cd}$	4567 87	Si III	$Cd$ , $LS_2$ , $LS_1$
4143 76	He 1	$\operatorname{Cd}$	4574 78	Si III	$Cd$ , $LS_2$ , $LS_1$
1340 47	$H\gamma$	$Cd, LS_2$	4590 97	<i>O</i> 11	$Cd, LS_1$
1345 56	Оп	$Cd$ , $LS_2$	4596 17	<i>O</i> 11	$Cd$ , $LS_1$
1347 42	Оп	$Cd$ , $LS_2$			,

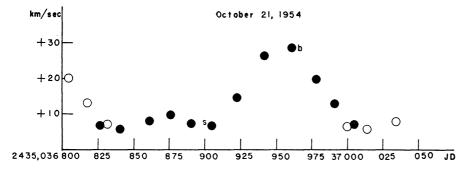
<sup>\*</sup> CD = Mount Wilson coudé; LS1 = Lick 10 A/mm; LS2 = Lick 25 A/mm

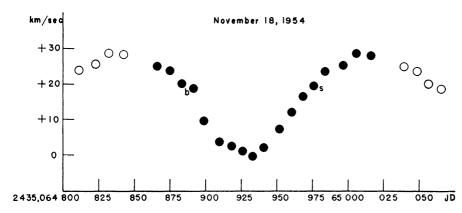
harmonic. Also the radial velocity-curves are complicated, particularly when 2K is small. Unlike DD Lacertae, BW Vulpeculae, and  $\sigma$  Scorpii, no doubling of spectral lines was observed on any of the plates. But the lines showed broadening near the maximum, on the descending branch of the velocity-curve. The plates on which the lines were sharpest are marked by s, and those on which the lines were broadest are marked by b in Figure 1. We note that on all curves the sharpest lines occur on the ascending branch near the minimum and the broadest lines are found on the descending branch near the maximum. This agrees with the previous result that the line broadening is associated with period  $P_2$ .

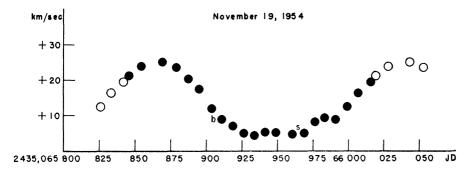
In the curve for December 8, 1954, we find two distinct maxima. In this case the lines are sharpest on the main ascending branch at the point marked ss. They become broad on the descending portion after the first maximum. The lines become sharp again on the ascending portion of the second maximum, but they are not so sharp as in the first case. Hence this point is marked by a single s. Finally, the lines again become broad on the main descending branch of the curve. It is interesting to note that a similar sharpening and broadening of the lines has been observed in the case of BW Vulpeculae (McNamara et al. 1955).

At first sight it is tempting to interpret the flat portion of the velocity-curve on December 8, 1954, between 0.790 and 0.825 as a "stillstand" of the kind observed pre-









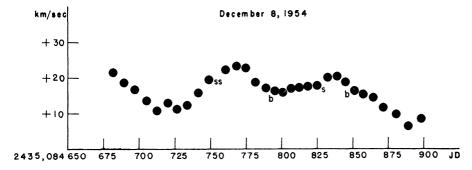


Fig. 1a—Individual radial velocities of  $\nu$  Eridani

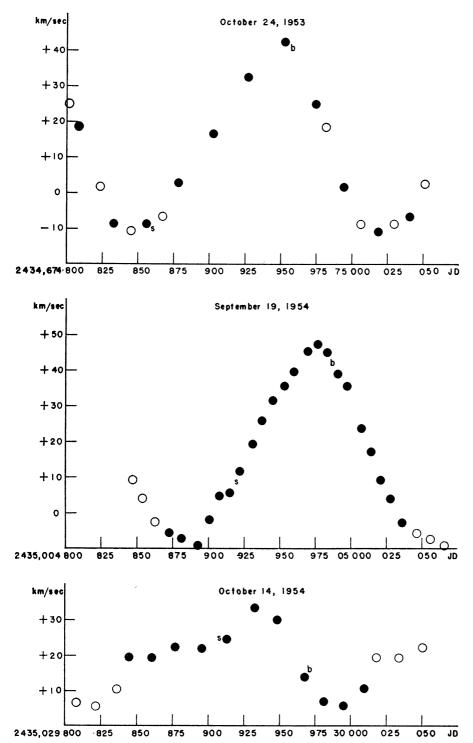


Fig. 1b—Individual radial velocities of ν Eridani

TABLE 2
OBSERVED RADIAL VELOCITIES

Plate	JD 243+	Phase (Days)	Velocity (Km/Sec)	Plate	JD 243+	Phase (Days)	Velocity (Km/Sec)
Cd	4674 808	0 035	+18 5	Cd	5064 926	0 083	+ 1 0
	833 856	060 083	- 8 7 - 8 7		933 941	090 098	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	878	106	+27		952	109	+72
	903	130	+16.7		960	117	+12 1
	927	154	+32 3		968	125	+16 6
	953 975	006 028	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		976 984	133 141	+196 + 237
	997	050	+16		996	154	$+25 \ 3$
	4675 019	072	-10 8		5065 006	163	+28 7
	041	094	- 6 5		016	173	+28 2
	5004 873 882	069 078	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		846 854	156 164	+21 2 +23.8
	892	089	-91		869	005	+25.8 +25.0
	901	097	- 20		879	015	+23 5
	908	105	+ 4 6		888	024	$+20\ 2$
	915 922	112	+ 5 5		895 904	$\begin{array}{c} 031 \\ 040 \end{array}$	+17 4
	931	119 128	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		911	$040 \\ 047$	$\begin{array}{c c} +11 & 9 \\ +8 & 9 \end{array}$
	938	134	$+25\ 7$		919	055	+ 6 9
	945	141	+31 5		926	062	+ 5 1
	953	149	+35 6		934	070	+ 4 4
	960 969	156 166	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		942 949	078 085	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	976	173	+47  4		960	096	+47
	983	006	$+45 \ 2$		969	105	+50
	990	013	+39 1		976	112	+ 8 2
	997 5005 008	020 031	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		983 991	119 127	+ 9 3 + 8 9
	015	031	+17.1		999	135	+12 5
	021	044	+92		5066 007	143	+16 2
	028	051	+ 3 9		015	151	+19 5
C	036 5029 845	059 082	$\begin{array}{c c} -28 \\ +193 \end{array}$		5084 682 690	088 096	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
$LS_2$	860	097	+19.3		697	103	+16 8
	877	114	$+22\ 2$		705	111	+13 5
	896	133	+21 8		712	118	+10 8
	913 933	150 170	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		720 727	126 133	$+129 \\ +111$
	949	012	+299		734	140	$+12^{\circ}2$
	967	030	+13 8		742	148	+15 8
	981	044	+ 6 8		749	155	+19 4
	995 5030 010	058 073	$\begin{array}{c c} + 5 & 7 \\ +10 & 3 \end{array}$		760 768	166 000	+22 2
$_{2}S_{1}$	5036 826	046	+67		775	007	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	840	060	+ 58		782	014	+18 6
	861	081	+80		789	021	+17 0
	876 890	096 110	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		795 801	$\begin{array}{c} 027 \\ 033 \end{array}$	+16 2
	905	125	+ 68		807	039	$\begin{array}{c c} +15 & 8 \\ +17 & 0 \end{array}$
	922	142	+14 7		812	044	+17.2
	942	162	$+26\ 4$		818	050	+17 5
	960	006	+28 7		825	057	+17 8
	978 991	024 037	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		833 839	065 071	+20 1  +20 3
	5037 005	051	+71		845	077	+18 8
Cd	5064 866	023	+250		851	083	+16 3
	875	032	+23 6		858	090	+15.2
	883 892	040 049	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		865 872	097 103	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	892 899	056	+187 +96		881	113	+117 + 96
	910	067	+ 3 7		890	122	+ 62
	918	0 075	+ 2 5		899	0 131	+84

TABLE 3

THE OBSERVED AND CALCULATED MAXIMA AND MINIMA
(Minimum = 2423709.816 + 0.1735089E; Maximum = 2433965.857 + 0 1735089E)

DATE	E	Observed JD	CALCULATED JD	Dif					
		Minimum							
Oct. 24, 1953	\[ \begin{cases} 63196 \\ 63197 \end{cases} \]	2434674 846 2434675 020	2434674 884 2434675 058	$-38 \times 10^{-3} \\ -38$					
Sept 19, 1954	\[ \begin{aligned} \ 65098 \\ 65099 \end{aligned}	2435004 888 2435005 061	2435004 898 2435005 072	-10 -11					
Oct. 14, 1954	\{ 65242 \ 65243	2435029 815 2435029 991	2435029 884 2435030 057	69 66					
Oct 21, 1954 Nov. 18, 1954 Nov. 19, 1954 Dec. 8, 1954	∫65282 (65283 65444 65450 ∫65558 (65559	2435036 840 2435037 015 2435064 929 2435065 949 2435084 720 2435084 893	2435036 824 2435036 998 2435064 932 2435065 974 2435084 712 2435084 886	+16 +17 - 3 -25 + 8 + 7					
	Maximum								
Oct. 24, 1953 Sept 19, 1954 Oct. 14, 1954 Oct. 21, 1954 Nov 18, 1954	4087 5989 6133 6173 56334 6335	2434674 947 2435004 977 2435029 937 2435036 954 2435064 843 2435065 015	2434674 988 2435005 002 2435029 987 2435036 927 2435064 862 2435065 036	-41 -25 -50 +27 -19 -21					
Nov. 19, 1954 Dec. 8, 1954	\[ \begin{cases} 6340 \\ 6341 \\ 6449 \end{cases} \]	2435065 864 2435066 040 2435084 768	2435065 903 2435066 077 2435084 816	-39 -37 -48					

TABLE 4
OBSERVED 2K

Date	Observed 2K (Km/Sec)	(O-C) (Maximum) (Days)	Phase (Days)	Date	Observed 2K (Km/Sec)	(O-C) (Maximum) (Days)	Phase (Days)
Oct. 24, 1953 Sept. 19, 1954 Oct 14, 1954 Oct. 21, 1954	54 5 57 0 29 2 24 0	$ \begin{array}{c} -41 \times 10^{-3} \\ -25 \\ -50 \\ +27 \end{array} $	4 7 6 6 3 7 3 7	Nov 18, 1954 Nov. 19, 1954 Dec 8, 1954	29 7 21 4 14 6	$ \begin{array}{r} -20 \times 10^{-3} \\ -38 \\ -48 \end{array} $	3 7 4 8 2 6

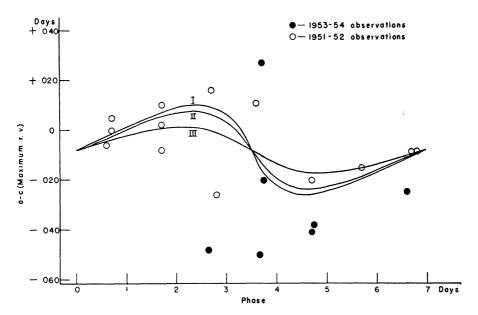


Fig 2 —Differences (O – C) for maximum radial velocity I,  $K_1 = 15.0$  km/sec,  $K_2 = 24.5$  km/sec; II,  $K_1 = 10.6$  km/sec,  $K_2 = 20.2$  km/sec; III,  $K_1 = 8.0$  km/sec,  $K_2 = 24.5$  km/sec.

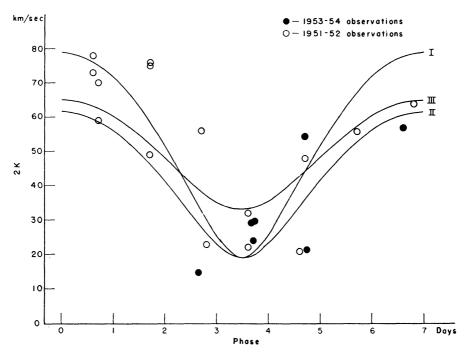


Fig. 3 —Observed and theoretical values of 2K I,  $K_1 = 150$  km/sec,  $K_2 = 245$  km/sec; II,  $K_1 = 106$  km/sec,  $K_2 = 20.2$  km/sec; III,  $K_1 = 80$  km/sec,  $K_2 = 24.5$  km/sec.

viously in BW Vulpeculae and  $\sigma$  Scorpii. But this is impossible for two reasons: (a) The computed maximum, uncorrected for the value of the initial epoch, is 0.816; after correction this becomes 0.808: both values fall upon the flat portion, while in BW Vulpeculae the computed maximum always *preceded* the "stillstand." (b) The phenomenon of double maxima and minima is pronounced only when the total range in velocity is small; in  $\sigma$  Scorpii the "stillstand" is most pronounced when the range is large.

We are undoubtedly concerned with another periodicity similar to those discovered by T. Walraven (1955) in AI Velorum. The present material is insufficient to examine this third period in detail. But on three nights we can estimate its value as follows: interval between two minima, October 14, 1954, 0.063 day; interval between two minima, October 21, 1954, 0.063 day; interval between two maxima, December 8, 1954, 0.067 day. We therefore suggest that there may be a period  $P_3 = 0.064$  day, with an amplitude of  $K_3 = 5$  km/sec.

## REFERENCES

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