

**Enhancing Spectrally Selective Response of W/WAIN/WAlON/Al₂O₃ –Based
Nanostructured Multilayer Absorber Coating through Graded Optical Constants**

**Atasi Dan ^a, Arup Biswas ^b, Piyali Sarkar ^b, Sanjay Kashyap ^c, Kamanio Chattopadhyay
^{c, d}, Harish C. Barshilia ^{e, *}, Bikramjit Basu ^{a, d, *}**

^a Materials Research Centre, Indian Institute of Science, Bangalore 560 012, India

^b Spectroscopy Division, Bhabha Atomic Research Centre, Mumbai 400085, India

^c Materials Engineering, Indian Institute of Science, Bangalore 560 012, India

^d Interdisciplinary Centre for Energy Research, Indian Institute of Science, Bangalore 560
012, India

^e Nanomaterials Research Laboratory, Surface Engineering Division, CSIR-National
Aerospace Laboratories, HAL Airport Road, Kodihalli, Bangalore 560 017, India

Abstract

In the field of concentrating solar power (CSP) technologies, multilayer absorber coatings are widely being investigated. The spectral properties of selective coatings can be tailored by carefully adjusting the composition and thickness of each layer. Based on the extensive analysis using the transmission electron microscopy (TEM), phase modulated spectroscopic ellipsometry along with computational analysis, we demonstrate how we can engineer the optical constants (refractive index and extinction coefficient) of individual layer to successfully achieve the spectrally selective properties in W/WAIN/WAlON/Al₂O₃ –based multilayer absorber coating. This coating exhibits a high absorptance of 0.958 and a low emittance of 0.08. The spectroscopic ellipsometry study confirmed the variation in metallic and optical properties of single layer of WAIN, WAlON and Al₂O₃ films, deposited on stainless steel substrates. This study also revealed the presence of intermediate layers of 26%

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WAIN - 74% WAION at WAIN/WAION interface and 60% WAION - 40% Al₂O₃ at WAION/Al₂O₃ interface. The Tauc - Lorentz dispersion model was very effective to interpret the ellipsometry data of single layers of WAIN and Al₂O₃, while Cauchy absorbent model was useful for WAION coating. Bruggeman effective medium approximation was used to describe the optical functions of intermediate layers. Investigation on optical constants reveals that the refractive index and extinction coefficient of each layer decrease from substrate to surface. The computational predictions of the reflectance properties corroborate well with the experimental results. In summary, the careful engineering on the optical properties of W/WAIN/WAION/Al₂O₃ structure enables it to be an exceptional spectrally selective absorber coating.

Keywords: Spectrally selective coating, Transmission electron microscopy, Ellipsometry, optical constants

*** Corresponding Authors:**

Email: harish@nal.res.in (Harish C. Barshilia)

bikram@mrc.iisc.ernet (Bikramjit Basu)

1. Introduction

It is well known that the interaction of electromagnetic radiation with a material is described in terms of optical constants (refractive index, extinction coefficient, permittivity, etc.) [1]. The optical constants of solar selective coatings have attracted considerable interest since they constitute a major role in the spectrally selective absorber for photothermal conversion in concentrated solar power systems [2, 3]. The photo thermal conversion of solar energy requires an efficient solar selective absorber coating, which has a maximum absorptance ($\alpha \geq 0.95$) in solar irradiation region (0.25 - 2.5 μm) and minimum emittance ($\varepsilon \leq 0.05$) in IR region (2.5 - 25 μm) [4, 5]. In order to understand the physical mechanism of

1 solar selectivity in an absorber coating, an extensive knowledge of optical constants over a
2 wide range of wavelength is essentially important. The optical constants do not only help to
3 determine the efficiency of a solar thermal systems, but also serve the role as an additional
4 tool for optimization in designing the absorber coating in future. In recent years, several
5 investigations are reported to understand the effect of optical constants. The role of refractive
6 index and extinction co-efficient on reflectance properties of each layer have been
7 established. Ellipsometry is widely used to determine the refractive index and extinction co-
8 efficient of each layer [6, 7]. For example, Selvakumar et al. [8] performed the ellipsometric
9 characterization on $\text{HfO}_x/\text{Mo}/\text{HfO}_2$ –based solar selective coating and found the metallic
10 character of Mo layer, while dielectric behaviour has been observed in HfO_x and HfO_2 layers.
11 An investigation using spectroscopic ellipsometry by Juang et al. [9] demonstrated that the
12 property of stainless steel can change from metal to dielectric, if deposited in a nitrogen
13 environment. Soum-Glaude et al. [10] analysed the spectral performance of SiC(N)H coating
14 with the help of ellipsometric measurements while Subasri et al. [11] confirmed the
15 fabrication of graded index structure of Ag- $\text{TiO}_2/\text{TiO}_2/\text{SiO}_2$ absorber coating.

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37 In order to advance the optical engineering of the thin film and to comprehend the
38 light trapping phenomenon, different simulation approaches are adopted and applied for
39 single and multilayer coatings. Irrespective of the approach and coating structures, most of
40 the simulation procedures require the known optical constants as input. In addition, a number
41 of other parameters such as the number of layers, their order and thicknesses are also
42 required. This aspect has been reported to a larger extent. Farooq et al. [12] have simulated
43 the optical properties of a multilayer V: Al_2O_3 coating with a high absorptance of 0.98 and a
44 low emittance of less than 0.07 using a computer model. They also validated the
45 computational findings with experimental results. Modelling of two multilayer stacks (Mo,
46 TiO_2 , MgF_2 and W, TiO_2 , MgF_2) have been performed by Sergeant et al. [13]. They predicted

1 high solar absorptance ($> 94\%$), while thermal emittance was low ($< 7\%$) at 720 K. Nejati et
2 al. [14] have theoretically investigated the optical properties of absorber coatings by changing
3 the number of cermet layers with different ceramic and metallic components.
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8 In our previous work [15, 16], we have reported the spectrally selective properties (α
9 $= 0.958$, $\varepsilon = 0.08$) of W/WAIN/WAlON/Al₂O₃ -based solar absorber coating, which was
10 deposited on stainless steel substrate by reactive DC and RF magnetron sputtering. The
11 coating also possessed a high angular absorptance over a wide range of incidence angles from
12 18° - 58° [17].
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21 In the present study, we have unravelled the mechanism of the superior selectivity of
22 W/WAIN/WAlON/Al₂O₃ -based absorber coating. We have examined and analysed each
23 layer of the coating systematically using transmission electron microscopy (TEM). The
24 optical constants of all the layers were evaluated using spectroscopic ellipsometry data. The
25 reflectance spectra of the coatings were simulated with commercially available SCOUT
26 software by modelling the multilayer absorber stack. The obtained results and subsequent
27 analysis enable appropriate explanation for the origin of spectrally selective properties of
28 W/WAIN/WAlON/Al₂O₃ coating.
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41 **2. Experimental**

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44 W/WAIN/WAlON/Al₂O₃ multilayer coating has been deposited on stainless steel (35 mm
45 X 35 mm X 2 mm) and Si substrates by reactive DC and RF magnetron sputtering.
46 Mechanically polished and chemically cleaned substrates were kept in the sputtering chamber
47 which was pumped to a base pressure of 8.5×10^{-6} mbar. High purity ($> 99.9\%$) W, Al and
48 Al₂O₃ targets were used for deposition. Reactive DC sputtering of W and Al targets was
49 carried out in order to deposit WAIN and WAlON layers in Ar + N₂ and Ar + N₂ + O₂,
50 respectively. The Al₂O₃ layer was deposited by RF sputtering in Ar + O₂ environment. Proper
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1 optimization of target power, deposition time and gas flow rate resulted in desired selective
2 coating with maximum solar absorptance and minimum thermal emittance. Gas flow was
3 controlled by electronic mass flow controllers and the substrates were continuously rotated
4 during deposition. The deposition parameters have been demonstrated in detail elsewhere
5 [15].
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11 Detailed microstructural and chemical characterization of all the layers were carried out
12 using FEI make TITAN G² 60-300kV TEM/STEM. For this study, we prepared the cross-
13 sectional TEM samples using thinning of samples by dimpling, followed by ion milling
14 (Gatan make PIPS). High-resolution transmission electron microscopy (HR-TEM), and
15 selected area electron diffraction (SAED) studies were also performed to acquire further
16 information. The thickness of the single layer WAIN, WAION and Al₂O₃, deposited for
17 longer duration on Si substrates were measured by FESEM. The surface roughness of films
18 fabricated on stainless steels were examined using AFM (Bruker).
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32 The ellipsometric data were collected using a spectroscopic phase modulated ellipsometer
33 (model UVISEL™ 460, ISA JOBIN-YVON SPEX) in the wavelength range of 300 – 800 nm
34 at an incidence angle of 70°. The data analysis was carried out using DeltaPsi2 Software. A
35 Perkin-Elmer Lambda 950 spectrophotometer equipped with an integrating sphere of
36 diameter 150 mm were used in the wavelength interval 0.3 – 2.5 μm to measure diffuse
37 reflectance of the coatings. The experimental reflectance spectra were fitted with the SCOUT
38 software. In order to facilitate the simulation procedure, we used optical constants obtained
39 from ellipsometry study and angle of incidence as input.
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52 **3. Results**

53 **3.1. Microstructural Properties**

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1 First, we shall present the microstructural details of the investigated multilayer coating.
2 TEM investigation of the cross-sectional absorber reveals the thickness of individual layer of
3 W, WAIN, WAION, and Al₂O₃ to be ~125 nm, ~40 nm, ~40 nm and ~62 nm, respectively. A
4 ~ 4 nm thin silicon oxide layer could also be observed on Si substrate. Dark field TEM
5 micrograph of Fig. 1 (a), acquired using STEM dark-field detector, clearly shows the growth
6 of all the four layers. The compositions of each of the four layers were determined by
7 carrying out line scans across the layers. The concentration profiles of each element are
8 shown in Fig. 1 (b) and the corresponding traces of the beam is shown by the red line in the
9 TEM micrograph of Fig. 1 (a). Each layer is clearly distinguishable in terms of variation in
10 elemental concentration, as marked in Fig. 1 (b). Selected area electron diffraction (SAED)
11 pattern acquired from the substrate (Fig. 1 (c)) can be indexed in terms of [101] zone axis of
12 Si. Fig. 1 (d) shows the dark-field TEM image along with SAED pattern in the inset. The
13 SAED can be indexed in terms of [001] zone axis of bcc W. The dark-field image is acquired
14 using (020) reflection of bcc W. The SAED pattern acquired from the grain is shown by the
15 arrow. This evidence confirms the crystalline nature of W layer. At few places in the dark-
16 field image, a number of fine nanocrystals are also illuminated in WAIN and Al₂O₃ layers.
17 Such observations indicate the nanocrystalline nature of these layers. Diffuse spotty ring in
18 the diffraction pattern and the dark-field image in Fig. 1 (e) also support such observations.
19 Most of the spotty rings can be indexed as the reflections of hexagonal α -Al₂O₃. The dark-
20 field image corresponds to (202) reflection of α -Al₂O₃. The uniform contrast of the WAION
21 layer suggests the possible amorphous nature of this layer. To further support the above
22 results, we have carried out high-resolution transmission electron microscopy (HRTEM) of
23 interfaces (details are in supplementary information, Fig. S1).

3.2. Spectroscopic Ellipsometry Analysis

3.2.1 Optical Functions of Single Layer Coatings

1 An analysis of selective properties of a multilayer film requires a knowledge on the
2 optical properties of individual layer. In order to obtain the optical properties of individual
3 layer, single layer of WAlN, WAlON and Al₂O₃ were fabricated independently on stainless
4 steel and Si substrates for longer duration. Before starting the ellipsometric study, it was
5 necessary to acquire information about the thickness of each **single layer** coating. Hence, the
6 individual coating on Si substrate was investigated using FESEM for the cross-sectional
7 thickness measurements. The thicknesses of the coatings are found to be ~ 433, 716 and 300
8 nm for WAlN, WAlON and Al₂O₃ films, respectively (Supplementary information; Fig. S2.).
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20 In spectroscopic ellipsometry, the main principle is to measure the changes in the state of
21 the polarization of a monochromatic beam upon reflection at an optical boundary. The
22 changes are expressed as Ψ and Δ of each layer, which correspond to changes in amplitude
23 ratio and phase of s- and p- polarised light, respectively. Ψ and Δ are related by the complex
24 reflection ratio (ρ), i.e., the ratio of the Fresnel reflection coefficients for s- and p-polarized
25 light [18]:
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$$35 \rho = \frac{r_p}{r_s} = \tan(\Psi) \exp(i\Delta) = \frac{\frac{E_{rp}}{E_{ip}}}{\frac{E_{rs}}{E_{is}}} \quad (1)$$

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41 where E_{rp} and E_{rs} are the reflected electric fields for s- and p- polarized light, respectively,
42 and E_{ip} and E_{is} are the respective incident electric fields.
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46 The optical constants can be determined by considering a proposed physical model
47 corresponding to each sample which can be generated based on appropriate generalised
48 oscillator for the optical dispersion. Eventually curve fitting of the obtained data from the
49 proposed model can be carried out with the experimental Ψ and Δ data, acquired from
50 ellipsometry. **The goal is to minimize the mean square function using a regression algorithm**
51 **for the ellipsometry equation** [19]:
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$$\chi = \left\{ \frac{1}{2N-M} \sum_{i=1}^N \left[\left(\frac{\Psi_i^{mod} - \Psi_i^{expt}}{\sigma_{\Psi,i}^{expt}} \right)^2 + \left(\frac{\Delta_i^{mod} - \Delta_i^{expt}}{\sigma_{\Delta,i}^{expt}} \right)^2 \right] \right\}^{1/2} \quad (2)$$

where N is the number of measured Ψ and Δ pairs, M is the total number of variable parameters, and σ is the standard deviations. The superscript ‘mod’ means the theoretical calculations and the ‘expt’ means the experimental data.

The fitting of the experimentally measured ellipsometric parameter (Ψ and Δ) with theoretically generated parameters were performed using the following approaches:

- a) A single layer homogeneous model of thin film was constructed with a realistic dispersion model of refractive index (n) and extinction coefficient (k).
- b) The optical properties (n and k) of substrate were taken from separate ellipsometric measurement of bare substrate.
- c) The dispersion modelling of the optical properties of WAION layers was performed using Cauchy absorbent dispersion relation due to amorphous nature of the sample. The Cauchy absorbent dispersion relation can be expressed as,

$$n(\lambda) = A + \frac{B}{\lambda^2} + \frac{C}{\lambda^4} \quad (3)$$

$$k(\lambda) = D + \frac{E}{\lambda^2} + \frac{F}{\lambda^4} \quad (4)$$

where λ is the wavelength, A, B, C, D, E and F are the fit parameters. A represents the long wavelength asymptotic refractive index value. B and C influence the slope and amplitude of the refractive index curve. B dominates the curvature for the medium wavelength, while C is responsible for the spectrum at shorter wavelengths. The characteristics of D, E and F are similar to A, B and C respectively.

(d) We preferred using a Tauc–Lorentz (TL) oscillator model for WAIN and Al₂O₃ coating as some nanograins are visible in these layers (see S1 (d)). TL model is very effective in characterization of nanocrystalline and amorphous materials [20]. It is relevant to mention that the complex dielectric function for a material can often be expressed using such simple oscillator model. This model provides the expression for ϵ_2 , the imaginary part of the dielectric function. The model can be obtained by multiplying the Tauc expression for ϵ_2 near the band edge by the imaginary part of the complex dielectric function of a single Lorentz oscillator [21]:

$$\begin{aligned} \epsilon_2 &= \frac{AE_o\Gamma(E-E_g)^2}{[(E-E_g)^2 + \Gamma^2 E^2]^2} \frac{1}{E}; E > E_g \\ \epsilon_2 &= 0; E < E_g \end{aligned} \quad (5)$$

where E_o is the peak transition energy, E_g is the optical band gap energy, Γ is the broadening parameter, and A is the optical transition matrix elements. The real part of the dielectric function ϵ_1 is given by Kramers-Krönig transformation (KKT)

$$\epsilon_1 = \epsilon_{\alpha,UV} + \frac{2}{\pi} P \int_{E_b}^{\infty} \frac{\xi \epsilon_2(\xi)}{\xi^2 - E^2} d\xi \quad (6)$$

where $\epsilon_{\alpha,UV}$ is high frequency dielectric constant and P is denoting the principal values of the integrals. This integral could be solved in the closed form, which is shown elsewhere [21, 22].

These proposed physical models have been curve fitted with experimentally measured Ψ and Δ data of WAIN, WAION and Al₂O₃ samples through χ^2 minimisation (metric of good fitting) process. The maximum number of iteration allowed is 100 and the criteria for convergence used is $\delta\chi^2 = 0.000001$. Clearly, the fitted Ψ and Δ , marked by solid lines are in good agreement to the measured data, represented by open symbols in Figs. 2 (a - c). The respective single layer structures used to perform the modelling have also been presented

1 along with $\Psi - \Delta$ spectrum. However, the oscillations in the full wavelength range of 300 –
2 800 nm in Figs. 2 (b) and 2 (c) indicate interference phenomenon representing the semi-
3 transparent/transparent behaviour of WAION and Al₂O₃. In contrast, the absence of such
4 oscillation in Fig. 2 (a) is indicative of strongly absorbing property of WAIN. Such behaviour
5 can also be predicted from the reflectance spectra of each single layer coating in the
6 wavelength range of 300 - 2500 nm (see supplementary information, Fig. S3.). The optical
7 constants, refractive index (n) and extinction coefficient (k) of the individual layer have also
8 been extracted from the best fitting results of Cauchy absorbent dispersion relation and TL
9 model and plotted as a function of wavelength in Figs. 3 (a) and 3 (b). It can be noted that
10 the refractive index of WAIN increases with wavelength, which is a characteristic response of
11 metallic film. In case of WAION, the refractive index slowly decreases with wavelength and
12 does not show much variation after 600 nm, which can be considered as an evidence of
13 semiconducting nature of WAION [23, 24]. Al₂O₃ has almost a constant refractive index
14 throughout the wavelength range. The decrease of the k in WAIN and WAION film depicts
15 the existence of interband transition. The 'k' value of Al₂O₃ is zero as expected for a
16 dielectric material (see Fig. 3 (b)) [25]. Such excellent optical behaviour makes Al₂O₃ a very
17 good option for anti-reflection layer. The best fitting parameters for all the layers have been
18 presented in Tables 1 and 2.

19 The optical absorption co-efficient defines how far can electromagnetic radiation of a
20 particular wavelength can penetrate a material. This can be calculated in terms of wavelength
21 and the optical extinction co-efficient by the following equation

$$\alpha = \frac{4\pi k}{\lambda} \quad (7)$$

22 Absorption coefficient of WAIN, shown in Fig. 4 (a) is appreciably higher than that of
23 WAION and Al₂O₃. Such observation indicates that WAIN absorbs photons very efficiently
24 than other two films, which is also evident from the variation of penetration depth as a

function of wavelength in Fig. 4 (b). The penetration depth provides useful information on the thickness of the material involved in the interaction with light [26]. As seen in Fig. 4 (b), the penetration depth in WAIN film is almost zero, which physically signifies that the solar radiation is trapped in the film while for WAION layer, the penetration depth increases drastically with wavelength. This indicates the solar radiation can penetrate the WAION film intensely before getting absorbed. These results also suggest that WAIN is the main absorbing layer of the multilayer structure, while WAION acts as semi-transparent layer.

The optical constants (n and k) are related to complex dielectric constant by the following expression, $\varepsilon = \varepsilon_1 + i\varepsilon_2$, where $\varepsilon = N^2$ and the complex refractive index, $N = n + ik$. Hence, $\varepsilon_1 = n^2 - k^2$ and $\varepsilon_2 = 2nk$ [27]. Figs. 4 (c) and 4 (d) represent the real and imaginary part of ε as a function of incident photon energy. The imaginary part of the dielectric constant is directly related to the conductivity, which can be observed from the equation below.

$$\varepsilon = \varepsilon_1 + i\varepsilon_2 = \varepsilon_1 + i \frac{\sigma\omega}{\varepsilon_0} \quad (8)$$

Therefore, more the value of ε_2 , more conducting the material will be. Hence, the large ε_2 of WAIN in Fig. 4 (d) suggests the conducting i.e. metallic property of that layer. The imaginary part of dielectric function is also associated with the dissipation and thus it is responsible for the absorption. It is well known that the higher the imaginary part of the complex dielectric constant, better the wave absorption effect. Therefore, the high value of ε_2 is responsible for the maximum absorption of solar energy in WAIN. The lower ε_2 values for WAION and Al_2O_3 film represent the transmitting behaviour of these layers. All these findings from dielectric constant data validate the observations found in the previous observations related to optical constants, absorption coefficients and penetration depths of all the layers.

3.2.2. Optical Functions of Multilayer Coatings

The optical design of multilayer coatings was performed using the optical constants of single layers, evaluated using Cauchy absorbent dispersion model and TL model. It is important to mention here that W layer possess pure metallic character with a high refractive index ($n = 3.83$), which has been well reported in literature [28, 29]. Moreover, W layer does not have any role in increasing the absorption of solar radiation in W/WAIN/WAlON/Al₂O₃ stack. Therefore, initially, we considered the basic layer-by-layer structure of WAIN/WAlON and WAIN/WAlON/Al₂O₃ and made an attempt to fit the experimental ellipsometric data of these samples deposited on SS substrate. However, we were unable to fit the experimental data with the theoretical predicted spectra. This may be due to the fact that the layer-by-layer stack is oversimplified. Hence, simple Cauchy absorbent and TL dispersion model cannot solely explain the optical response of such complicated structure. When we are moving from single layer to multilayer stack, we must take into account the collective optical behaviour of neighbouring layer and their effect on each other. Therefore, we consider a multilayer model, where the presence of intermixed layers was assumed in the middle of two layers. The intermediate layer in between WAIN and WAlON, WAIN-WAlON has been considered as a mixture of WAIN and WAlON phases. On the other hand, WAlON-Al₂O₃ is an intermixing layer in between WAlON and Al₂O₃ films. Due to complexity of the interfacial layer properties, researchers have often used Bruggeman effective-medium approximation (EMA)[30] model to obtain the optical properties of a two mixed material such as,

$$f_A \frac{\varepsilon_A - \varepsilon^{BR}}{\varepsilon_A + 2\varepsilon^{BR}} + (1 - f_A) \frac{\varepsilon_B - \varepsilon^{BR}}{\varepsilon_B + 2\varepsilon^{BR}} = 0 \quad (9)$$

where ε^{BR} is the average dielectric function of the composite in Bruggeman approximations, ε_A and ε_B indicate the dielectric function phase A and phase B, respectively.

The filling factor f_A is the volume fraction occupied by phase A.

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However, EMA model is very sensitive to the surface morphologies. The surface roughness can significantly influence the fitting using EMA model. The surface roughnesses of layer by layer coatings are notably small ($\sim 1 - 2$ nm) (Supplementary information, Fig. S4.). Therefore, the effect of the surface roughness has been neglected.

The variation of Ψ and Δ for WAIN/WAIN-WAION/WAION and WAIN/WAIN-WAION/WAION/WAION- $\text{Al}_2\text{O}_3/\text{Al}_2\text{O}_3$ coatings on SS substrates in the wavelength range of 300 - 800 nm have been shown in Figs. 5 (a) and 5 (b). The experimental and analytically predicted data are in well agreement with each other, which gives more confidence to the model used (see insets of Figs. 5 (a) and 5 (b)). The best fit results have been chosen by optimising simultaneously the composition of intermediate layers. The intermixed layer in between WAIN and WAION contains 26% WAIN and 74% WAION, while the layer in between WAION and Al_2O_3 is a mixture of 40% WAION and 60% Al_2O_3 . The EMA model has been utilized to generate the optical constants of the intermixed layers by weighting the optical constants of their components. We have also presented the wavelength dependence of n and k in Figs. 6 (a) and 6 (b). Interestingly, the optical constants (n and k) systematically decrease from WAIN (bottom layer) to Al_2O_3 (top layer). The optical constants of all the layers at 550 nm have been summarized in Table 3.

3.3. Optical Simulation

We have performed computational studies based on optical constants of the individual layer to predict reflectance properties in 300 – 2500 nm wavelength range. The simulated spectra using SCOUT software was fitted with the measured reflectance spectra by adjusting the optical constants of the individual layer. Optical constants of all the layers including the substrate, obtained from spectroscopic ellipsometry measurement have been introduced during simulation to calculate the reflectance. Figs. 7 (a) and 7 (b) show that the simulated and the experimental spectra do not agree well with each other as we did not consider the

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presence of intermediate layers (WAIN - WAION and WAION - Al₂O₃). However, Figs. 7 (c - e) illustrate best fitted simulated and reflectance spectra, where the optical constants of all the five layers (WAIN, WAIN-WAION, WAION, WAION-Al₂O₃ and Al₂O₃) acquired from ellipsometry study, were used to conduct computational analysis for the multilayer stack with two intermediate layers. Hence, the formation of the intermediate layer is also validated by the computational study. It can also be observed that in case of the coatings without the intermixed layers (Figs. 7 (a) and 7 (b)), the reflectance minima of all the spectra appear in the lower wavelength side, whereas the reflectance spectra of the thin films (Figs. 7 (c - e)) simulated by introducing the middle layers indicate a shift in the reflectance minima towards higher wavelength. It causes the reduction of the reflectance in the solar spectrum, thus increasing the absorptance of the coating. This study also confirms the accuracy of the optical constants, which were used to simulate the reflectance spectra. Therefore, it should be mentioned that the simulation in the present study can be considered to be an innovative reverse engineering procedure, which is extremely effective to verify the optical constants of the candidate layers, originated from ellipsometry.

4. Discussion

The most significance outcome of the present work has been to establish the rationale behind the remarkable spectrally selective properties of W/WAIN/WAION/Al₂O₃ with the help of spectroscopic ellipsometry measurements and computational analysis. In the following, we shall describe the correlation between architecture of the coating and optical constants as well as underlying physical mechanism of solar energy absorption.

4.1. Correlation between Optical Properties of Tandem Absorber and Multilayer Architecture

4.1.1. Gradation in Refractive Index

1 The investigation on the single and multilayer coating has demonstrated specific
2 dependence of optical constants (n and k) of all the layers on the wavelength. According to
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4 the previous study of our group, WAIN/WAlON/Al₂O₃ has a very high absorptance of 0.958
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6 in the solar spectrum. As the optical constants play an important role to design an efficient
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8 spectrally selective coating, it can be predicted that the appropriate stacking of these layers
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10 have offered such remarkable solar absorptance in the solar wavelength range. The successful
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12 fabrication of WAIN/WAlON/Al₂O₃ coating is directly related to the optical constants,
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14 particularly refractive index of each layer. A small difference in the refractive index may lead
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16 to a drastic change in the selective performance of the coating. Our study confirms that
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18 WAIN has a strongly absorbing property, while Al₂O₃ layer is transparent due to its dielectric
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20 nature. It is also evident from Fig. 6 (a) that WAIN/WAlON/Al₂O₃ is a graded film, where
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22 the refractive index of the individual layer is different from those of neighbouring layer. Also,
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24 the refractive indices of the coating decrease form substrate to surface.
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31 The most exciting finding of this work is the existence of the intermediate layers.
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33 There is no sharp boundary among WAIN, WAlON and Al₂O₃ layers. These layers are
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35 connected by two intermediate layers of 26% WAIN - 74% WAlON and 60% WAlON - 40%
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37 Al₂O₃. Fig. 6 (a) indicates that the refractive index of 26% WAIN - 74% WAlON layer lies in
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39 between the refractive indices of WAIN and WAlON, while 60% WAlON - 40% Al₂O₃ layer
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41 also shows intermediate value of refractive index following the analogy of the previous
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43 junction layer. The appropriate modelling to capture the reflectance properties of the
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45 multilayer stack was the major challenge of this work. This was accomplished by introducing
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47 the interfacial layers and optimizing appropriate volume fraction of the components in the
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49 interfacial layers. In particular, the analysis using EMA model enabled us to understand that
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51 the formation of these two additional intermediate layers makes the film highly graded. This
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53 kind of variation in refractive index makes the three-layer stack effectively five layer stack. It
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1 is noteworthy to mention that the high absorptance and the gradation in refractive indices are
2 highly correlated with each other. Therefore, it can be interpreted that the approach of
3 decreasing refractive index from the base layer to surface of a multilayer coating is an
4 unavoidable restriction for a solar selective absorber coating. The gradation of refractive
5 index has been introduced by varying the gas flow of N_2 and O_2 as the refractive index of any
6 layer is strongly dependent of the composition. The integration of N and O atoms in W and
7 Al matrix changes the electronic configuration, chemical states and film properties. Bartzsch
8 et al.[31] demonstrated the nonlinear dependency of the refractive index on the oxygen
9 content. They reported a decrease in refractive index with an increase in oxygen component
10 in $Si_xO_yN_z$ film. Borges et al.[32] were also able to tailor the optical properties of AlN_xO_y
11 film by changing $N_2 + O_2$ reactive gas mixture. Therefore, it is expected that the successive
12 deposition of all the layers in different reactive gas environment resulted in the formation of
13 an optically graded film. On the other hand, the refractive index of a coating is directly
14 related to the metallic property of the coating. The refractive index of the coating increases
15 with an increase in metallic property. This can also be supported from the extinction
16 coefficient (k) of each layer. One can notice in Fig. 6 (b) that WAIN has the maximum value
17 of k and for Al_2O_3 , $k = 0$. It is well known that materials with lower value of k are dielectric,
18 while those with higher value of k shows metallic property.

4.1.2. Compositional Variation

46 The decrease of the metallic property can be explained in the following way. W layer
47 on stainless steel substrate is a pure metal and a source of free electrons. It is relevant to state
48 that W layer serves the role of an infrared reflector to reduce the thermal heat loss from the
49 coating i.e. emittance of the coating. Therefore, W/WAIN/WAlON/ Al_2O_3 coating has a very
50 low thermal emittance of 0.08. It also acts as a diffusion barrier to protect the film from
51 degradation at high temperature. However, during deposition of WAIN layer, nitrogen gas is

1 impinged for reactive sputtering. In view of the microstructural properties, the W atoms can
2 accommodate nitrogen atoms of smaller size with a distortion in the lattice, which leads to
3 nanocrystalline nature of the film. Due to electronegative nature, N atoms acquire electrons at
4 the expense of W and Al atoms and it acts as an attractive pole of free electrons supplied by
5 W and Al. As a result, the conductivity of WAlN layer decreases to some extent compared to
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7 pure W metallic layer on stainless steel substrate. It has been observed by Soto et al. [33] that
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9 in low pressure of nitrogen, a component of WAlN film, WN_x exhibits metallic property. In a
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11 separate study [34], it has also been reported that WN_x has the lowest electrical resistivity
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13 among other transition metal nitrides. Even though the formation of semiconducting AlN
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15 takes place during sputtering, the metallic character is predominant due to the presence of
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17 WN_x as well as metallic Al in WAlN layer. Moreover, the higher value of complex dielectric
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19 constant of WAlN is correlated to the increased metallic property (see Fig. 4 (d)). During the
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21 fabrication of WAlON layer, the gas mixture of N_2 and O_2 is fed into the sputtering chamber.
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23 For the combined concentration of N and O atoms, it becomes impossible for these atoms to
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25 fit into W or Al atoms and the layer becomes completely amorphous. It is important to
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27 mention that the oxynitrides in this layer, WO_xN_y or AlO_xN_y are very attractive systems
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29 because optical properties of the constituent materials (Al, W, WO_x , Al_2O_3 , WN_x , AlN, etc)
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31 can be tuned to achieve the required performance. A few studies [35, 36] have been focused
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33 on the optical properties of transition metal oxynitrides, particularly WO_xN_y compared to that
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35 of transition metal oxides or nitrides. It is worthwhile to state that W exhibits a stronger
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37 affinity to oxygen than nitrogen. Also, from the thermodynamic considerations, the formation
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39 of tungsten oxide is strongly favoured over the formation of tungsten nitride or NO, because
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41 the heat of formation for WO_3 and WO_2 is -842.9 kJ/mol [37] and -589.7 kJ/mol [38],
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43 respectively. Such values are much lower than corresponding values for W_2N (-22 kJ/mol)
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45 [39], WN (-15 kJ/mol) [40], and NO (-91.3 kJ/mol) [41]. Therefore, it is expected that a large
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portion of WAION layer will be occupied by WO_3 and WO_2 phases. Moreover, Gillet et al. [42] suggested that the conductivity of WO_3 is related to non-stoichiometry, which originates from oxygen vacancies. In a separate study [43], it has been reported that amorphous WO_3 thin film has a band gap of 3.4 eV, while heat treated crystalline film possess a smaller band gap of 2.6 eV. Li et al. [44] also demonstrated that WO_3 , a wide band n-type semiconductor with a conductivity of 3.5×10^{-11} S/cm, acts as insulator (1.6×10^{-8} S/cm) before annealing due to amorphous nature. As WO_xN_y system is composed of WO_3 , WO_2 , WO_x , WN , etc. phases, AlO_xN_y system in WAION layer similarly may consist of substoichiometric AlO_x and AlN_y as well as stoichiometric Al_2O_3 and AlN . The band gap and conductivity of these materials can also be associated with the difference in ionicity between metal-O and metal-N bonds. As both these bonds present simultaneously in WAION layer, these lead to the localisation of most of the free electrons in W and Al. Considering all these aspects, it can be commented that WAION has a lower metallic property than WAIN. On the surface, the anti-reflecting layer is purely non-conducting as it contains Al_2O_3 , a highly insulating material ($E_g \sim 3.64$ eV) consisted of mixed ionic and covalent bonding and a large band gap energy [45]. Hence, the descending order of metallic component from substrate to surface has been elucidated intensely.

4.2. Solar Energy Absorption Mechanism in Multilayer Stack

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Now, we will try to explain the possible absorption mechanism, which is responsible for such an outstanding spectral selectivity of W/WAIN/WAION/ Al_2O_3 coating. An incident electromagnetic wave, while interacting with a material undergoes reflection, absorption and transmission. It is well known that it is difficult to achieve the highest spectral selectivity by a single layer due to huge amount of surface reflection. When light travels through the interface between two media with different refractive index (n_1 and n_2), the reflected light intensity at normal incidence can be expressed as,

$$R = \left[\frac{n_1 - n_2}{n_1 + n_2} \right]^2 \quad (10)$$

The above equation predicts that a strong reflection takes place, when the solar radiation tries to enter the main absorbing WAIN layer that typically have both a high real and imaginary part of the refractive index compared to air. In order to reduce the energy loss, it was essential to fabricate Al_2O_3 as an antireflection layer, which has a low refractive index. This simple concept of AR coating only works well for a limited range of wavelength and angle of incidence. A wide band and angularity independent reduction in the light reflection was achieved by depositing the semi-transparent WAION layer in between WAIN and Al_2O_3 layers.

A coating with low metallic property and optical constants will allow the sunlight to transmit to the next layer. The light-matter interaction will be stronger in WAIN due to higher metallic properties. These claims can also be validated by the absorption co-efficient and penetration depth of WAIN layer (see Figs. 4 (a) and 4 (b)). Even though absorption is very high in WAIN, some portion of the sunlight will be reflected back to 26% WAIN – 74% WAION layer from WAIN layer. According to ray optics, if two emerging reflected electromagnetic waves from WAIN and 26% WAIN – 74% WAION layers are out of phase by 180° , they lead to an extinction of solar radiation due to destructive interference. Consequently, the absorptance increases drastically. The reflectance spectra of the samples in Figs. 7 (c - e) depict that the reflectance is effectively reduced by adding each additional layer, which signifies the enhancement in solar absorptance. The presence of two interference minima at 360 and 1293 nm can be observed in the reflectance spectrum of SS/W/WAIN/WAION, while the appearance of a wider minimum occupying wavelength of 870 – 1345 nm along with a sharp minimum at 356 nm can be distinctly noticed in the reflectance spectrum of SS/W/WAIN/WAION/ Al_2O_3 . Therefore, the occurrence of

1 destructive interference in the presently studied coating can be believed to be of great
2 significance to boost the solar absorptance in solar spectrum.
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5 Another interesting approach to capture the solar radiation is through total internal
6 reflection (TIR), caused by the refractive index contrast between the neighbouring layers. The
7 solar rays scatter in different direction during interaction with the nanocrystallines in WAIN
8 layer. If the rays fail to fall within the escape cone, described by the critical angle[46],
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10 $\theta_c = \text{arcSin}\left(\frac{n_{26\% \text{ WAIN}-74\% \text{ WAION}}}{n_{\text{WAIN}}}\right)$, the rays will be totally internally reflected backed to
11
12 WAIN layer. The reflection of the rays for other layers is analogous to WAIN layer. The
13 multiple reflections of the rays increase the possibility of light-matter interaction and the
14 absorptance increases remarkably. Moreover, nanocomposite structure of WAIN layer,
15 embedded in amorphous matrix is very effective for intrinsic absorption of solar radiation.
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17 The high value of extinction coefficient of WAIN accounts for the strong absorption in solar
18 wavelength range.
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32 In summary, the specific design of W/WAIN/WAION/Al₂O₃ with a gradient in the
33 refractive index (n) and extinction coefficient (k) gradually from substrate to surface enabled
34 the coating to have outstanding solar radiation absorption ability ($\alpha = 0.958$) with a minimum
35 heat loss into the surrounding ($\varepsilon = 0.08$). Three optical phenomena; i.e., interference
36 mechanism, total internal reflection and intrinsic absorption have major contributions to boost
37 solar absorptance significantly.
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47 It is also important to mention that the thermal, structural and chemical stability are
48 the most essential criteria for a coating to be a potential high temperature spectrally selective
49 surface. In our recent study, we have reported that W/WAIN/WAION/Al₂O₃ coating was
50 stable at 350 and 500 °C in air for 500 and 150 hrs, respectively without showing any
51 significant change in the selective performance [17, 47]. The structural and chemical
52 characterizations of the as-deposited and annealed coatings also suggested the outstanding
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stability of the different components present in the coating at high temperature. Hence, it can

be stated that the presently studied coating undoubtedly have the potential to emerge as a spectrally selective solar absorber coating for solar thermal power systems.

5. Conclusions

In the present work, the microstructural study, phase modulated ellipsometric analysis together with computational analysis using SCOUT software have revealed the reasons behind the outstanding selective properties of W/WAIN/WAlON/Al₂O₃ –based solar selective absorber coating fabricated using magnetron sputtering. The key findings are as follows:

- a) TEM analysis confirms the crystalline nature of W layer. The existence of very fine nanocrystals in WAIN and Al₂O₃ layers was recorded together with amorphous nature of WAlON layer.
- b) Based on the critical analysis of the phase modulated ellipsometry data using Cauchy absorbent dispersion model, Tauc-Lorentz and Bruggeman effective medium approximation model, the gradation in optical constants (n and k) across the tandem architecture was established. During the analysis of the spectroscopic ellipsometry data, it has been perceived that the presence of two additional layers of 26% WAIN - 74% WAlON at WAIN/WAlON interface and 60% WAlON - 40% Al₂O₃ at WAlON/Al₂O₃ interface can allow one to effectively establish good corroboration between experimentally measured and model based predicted data. Bruggeman effective medium approximation works very well in parameterizing the refractive index and extinction coefficient of the intermediate layers.

1 c) The computational analysis using the extracted optical constants from
2 ellipsometry study establishes a good correlation between simulated and measured
3 reflectance spectra of the multilayer coating.
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7 Overall, the combined study of fine scale microstructural analysis, ellipsometric
8 measurements and the simulation work provide us effective guidelines to understand the solar
9 selective properties of W/WAIN/WAlON/Al₂O₃ absorber coatings.
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Table 1: Best fit ellipsometric parameters of TL dispersion model for WAIN and Al₂O₃ single layer coating on SS substrate

Coating	Parameters of TL dispersion model				
	E _g (eV)	ε _∞	A	E ₀ (eV)	C
WAIN	0.036	0.278	358.01	21.57	233.39
Al ₂ O ₃	6.71	1.15	99.44	11.15	0.26

Table 2: Best fit ellipsometric parameters of Cauchy absorbent model for WAION single layer coating on SS substrate

Coating	Parameters of Cauchy absorbent model					
	A	B	C	D	E	F
WAION	1.86	1.64	1.59	1146.34	-0.40	0.830

Table 3: The optical constants (n and k at 550 nm) of all the layers

Layer	Optical constants at 550 nm	
	Refractive index (n)	Extinction coefficient (k)
WAIN	2.971	1.299
WAIN-WAION	2.188	0.255
WAION	1.940	0.007
WAION-Al ₂ O ₃	1.806	0.004
Al ₂ O ₃	1.614	0

Figure

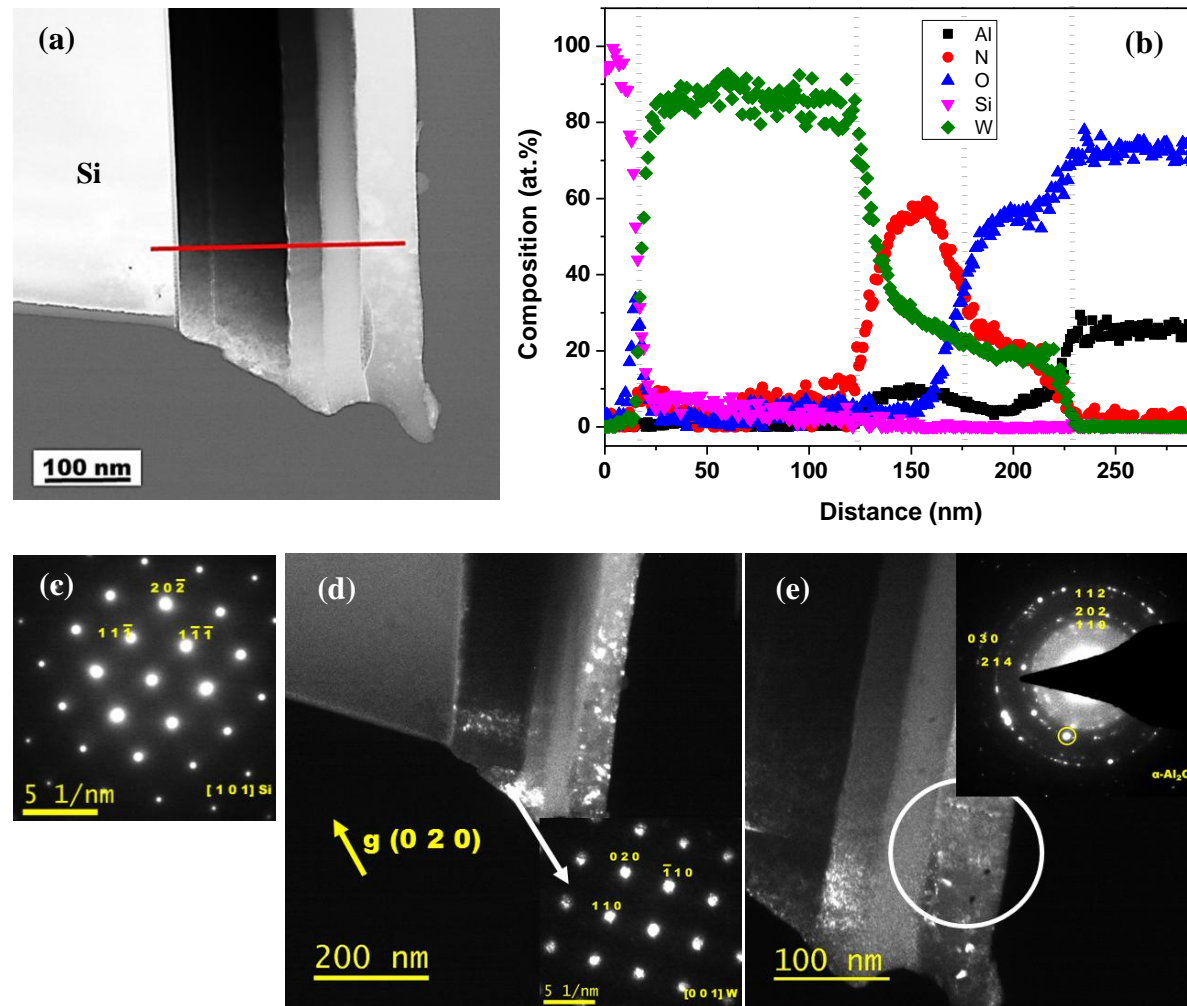
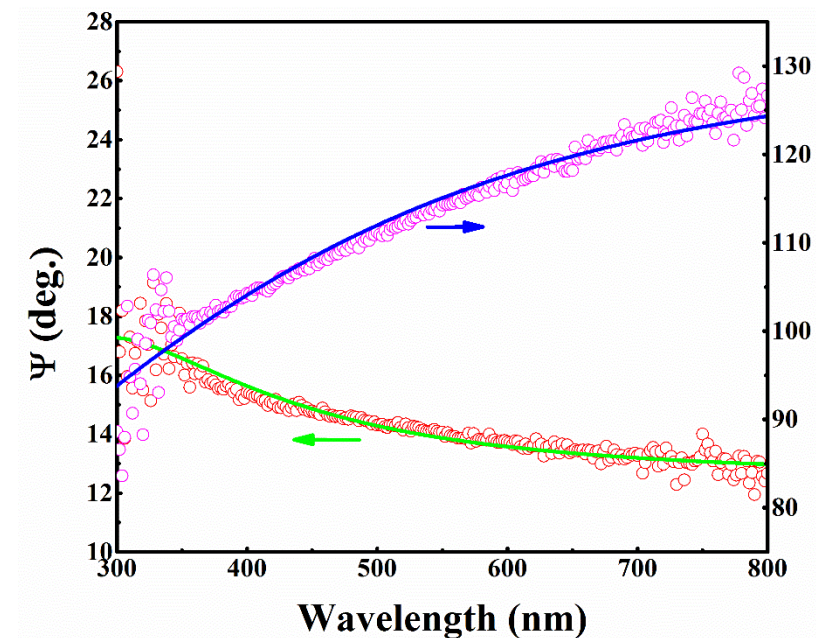
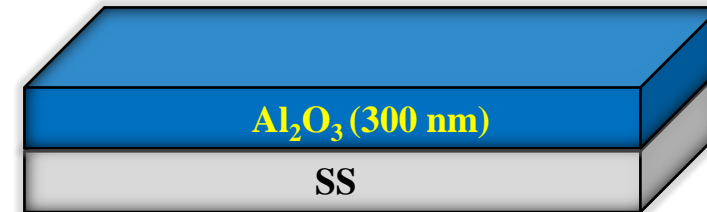
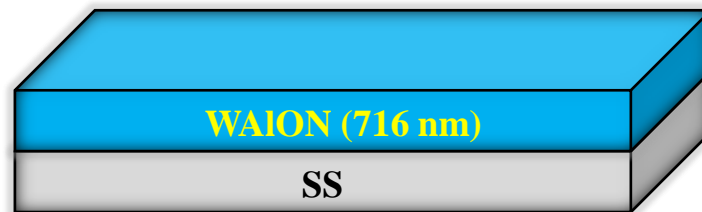
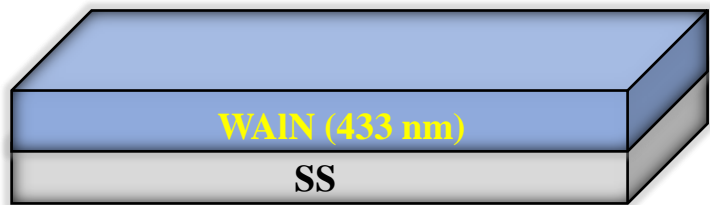
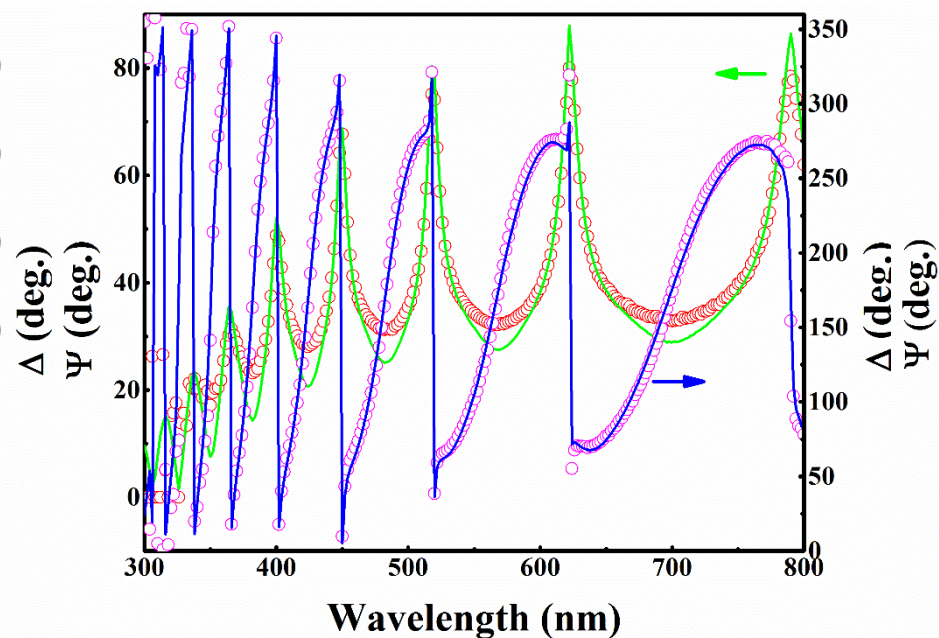


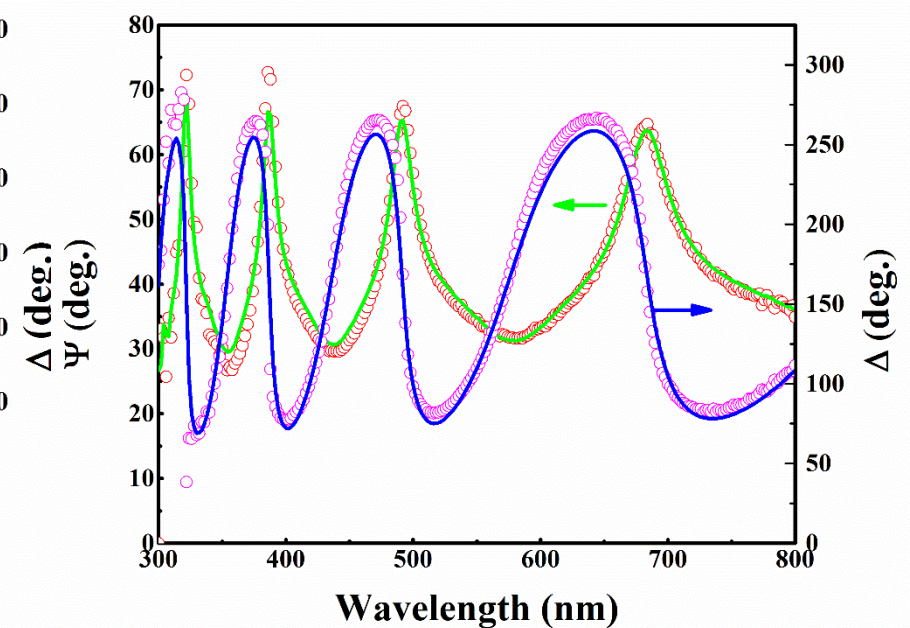
Fig. 1. (a) STEM dark-field image (cross-sectional view) of W/WAlN/WAlON/Al₂O₃ thin layers deposited on single crystal Si substrate, (b) concentration profiles of elements present in all four layers acquired using STEM-EDS detector from a region marked in the image with the red color line. (c) SAD pattern acquired from the substrate indexed in terms of [101] zone axis of Si, (d) dark-field showing the illuminated crystalline grains present in W layer and very fine nanograins in WAlN and Al₂O₃ layers and a SAD pattern acquired from a region marked by white arrow which can be indexed in terms of [001] zone axis of bcc W. (e) dark-field image with a SAD pattern as inset acquired from a region marked by white circle and spotty rings can be indexed with the reflection of hexagonal α -Al₂O₃.



(a)

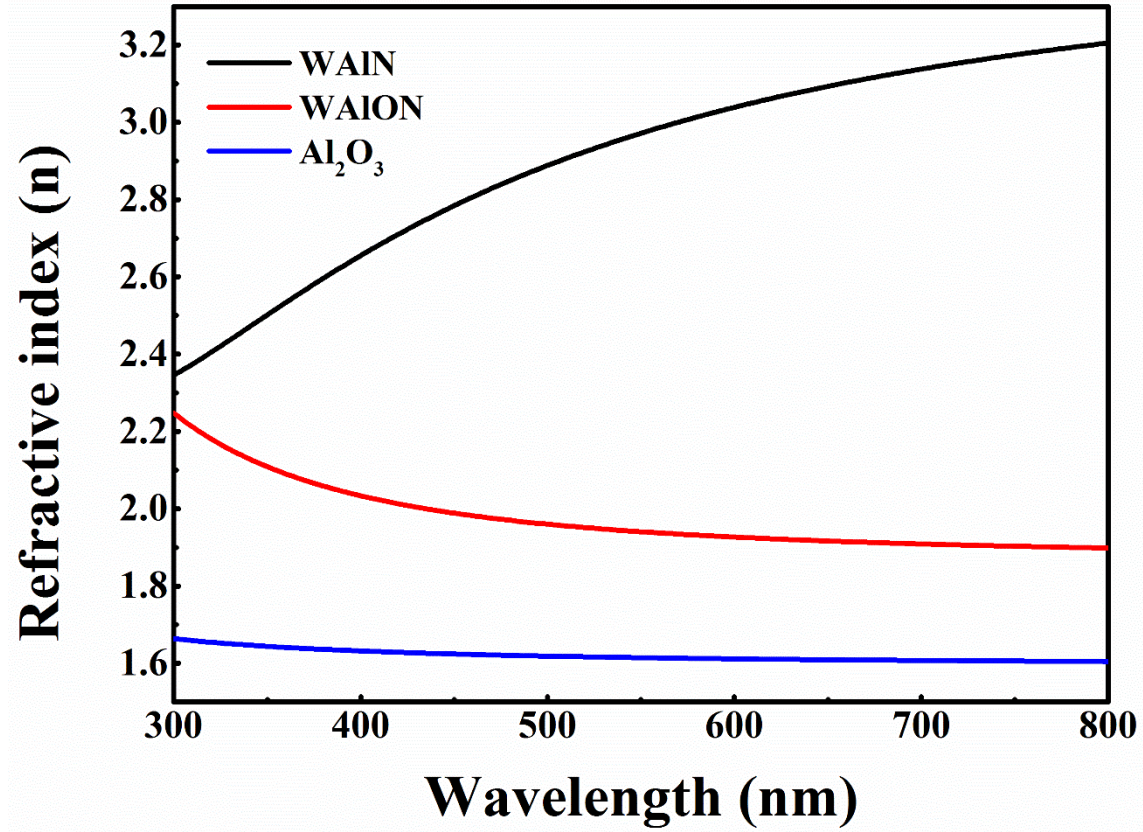


(b)

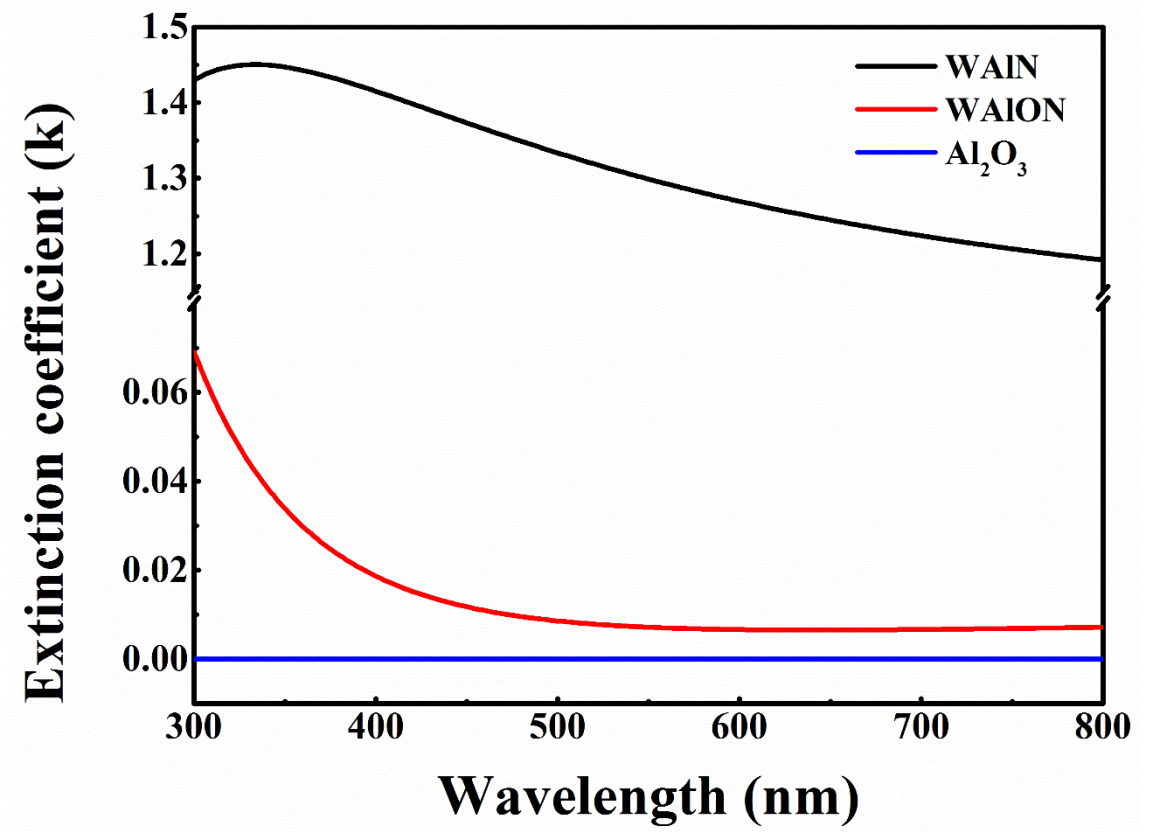


(c)

Fig. 2. Phase modulated ellipsometry spectra for (a) WAIN, (b) WAION, and (c) Al_2O_3 single layer thin film on SS substrates deposited for prolonged duration, along with their respective models shown in the schematics above the graphs. The open symbols (o) represent experimental data, while the solid lines (-) are obtained from the fitting procedure. Thickness of individual layer is also mentioned.

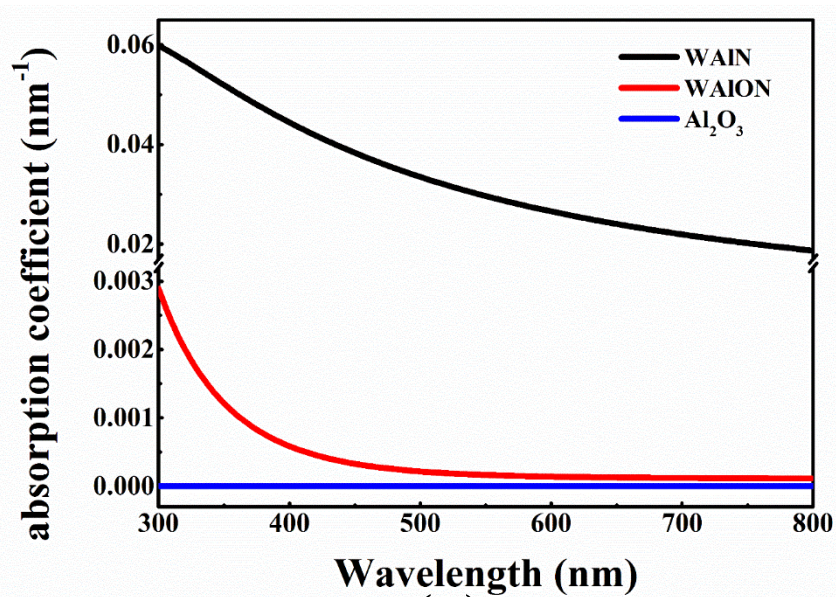


(a)

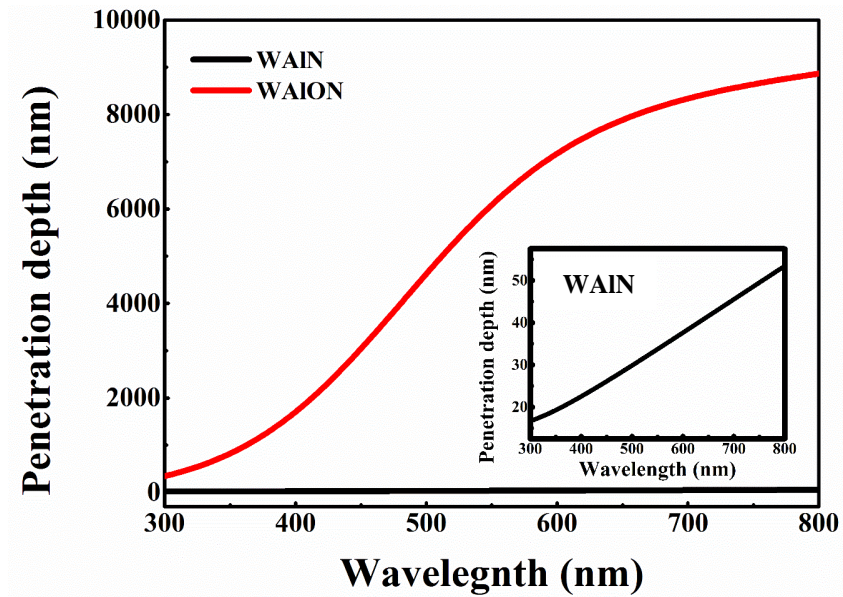


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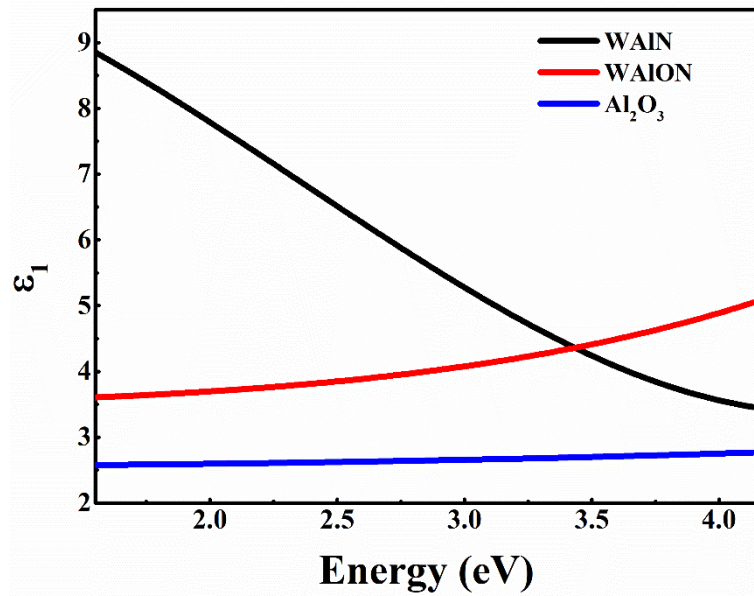
Fig. 3. Variation of (a) refractive index and (b) extinction coefficient with wavelength for WAIN, WAION and Al₂O₃ single layer coatings on SS substrates, as shown in Fig. 2.



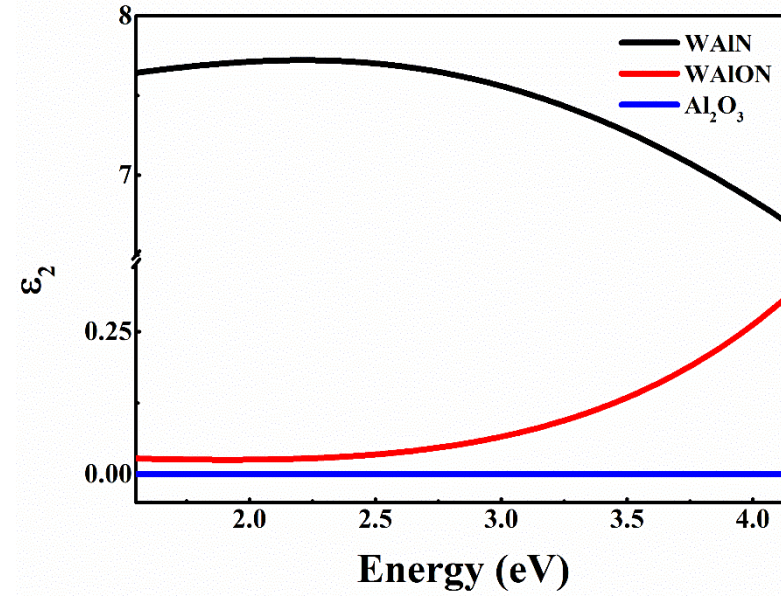
(a)



(b)

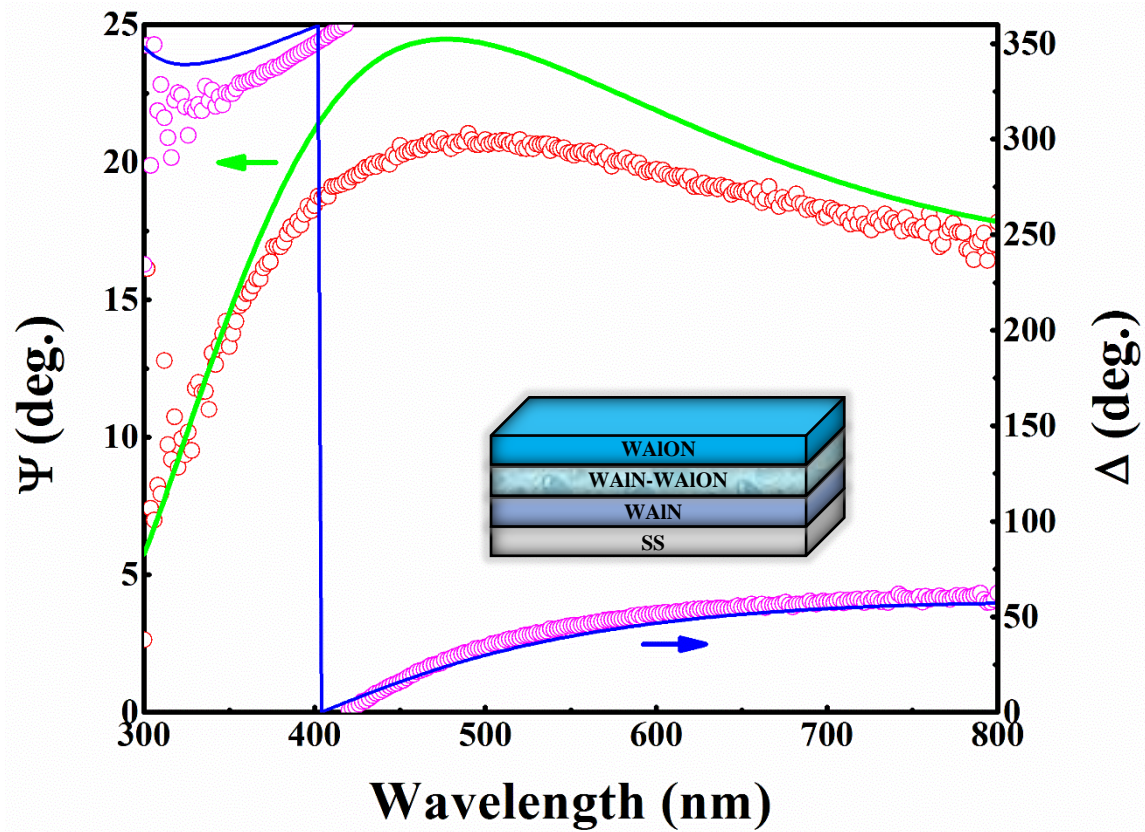


(c)

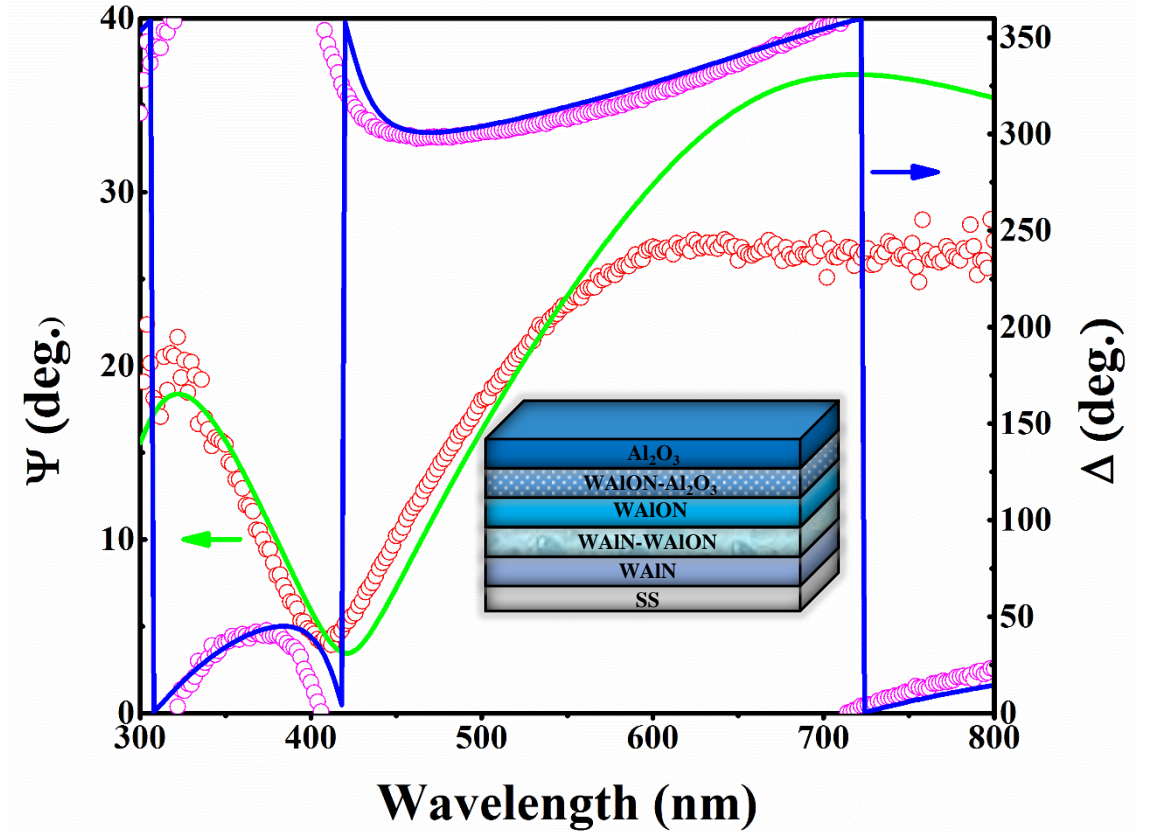


(d)

Fig. 4. (a) Absorption coefficient, (b) penetration depth (The inset shows the penetration depth of WAIN separately), (c) real (ϵ_1), and (d) imaginary (ϵ_2) part of the dielectric constants as function of wavelength for single layer coatings deposited on SS substrates, as shown in Fig. 2.



(a)



(b)

Fig. 5. Experimental (symbols) and fitted (solid lines) ellipsometric data for (a) WAIN/WAIN-WAION/WAION and (b) WAIN/WAIN-WAION/WAION-WAION- Al_2O_3 / Al_2O_3 layers on SS substrate; Insets show schematic representation of proposed structures used to perform the fitting.

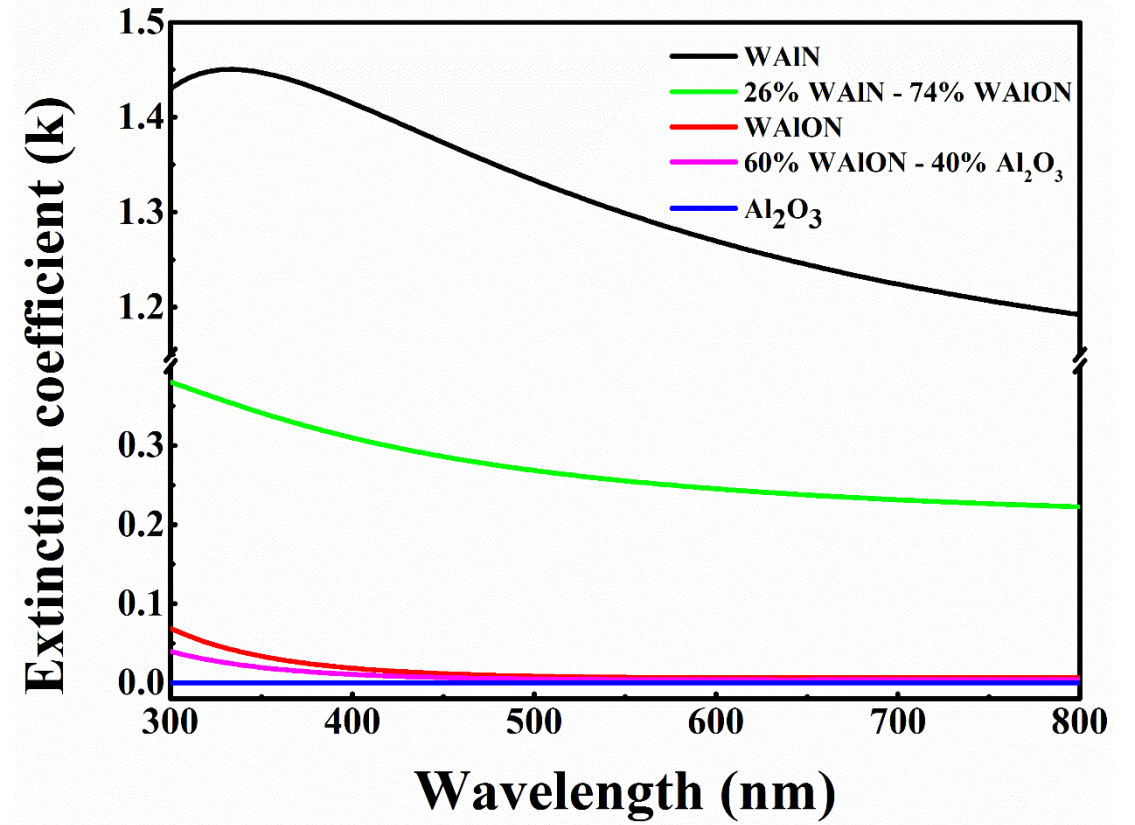
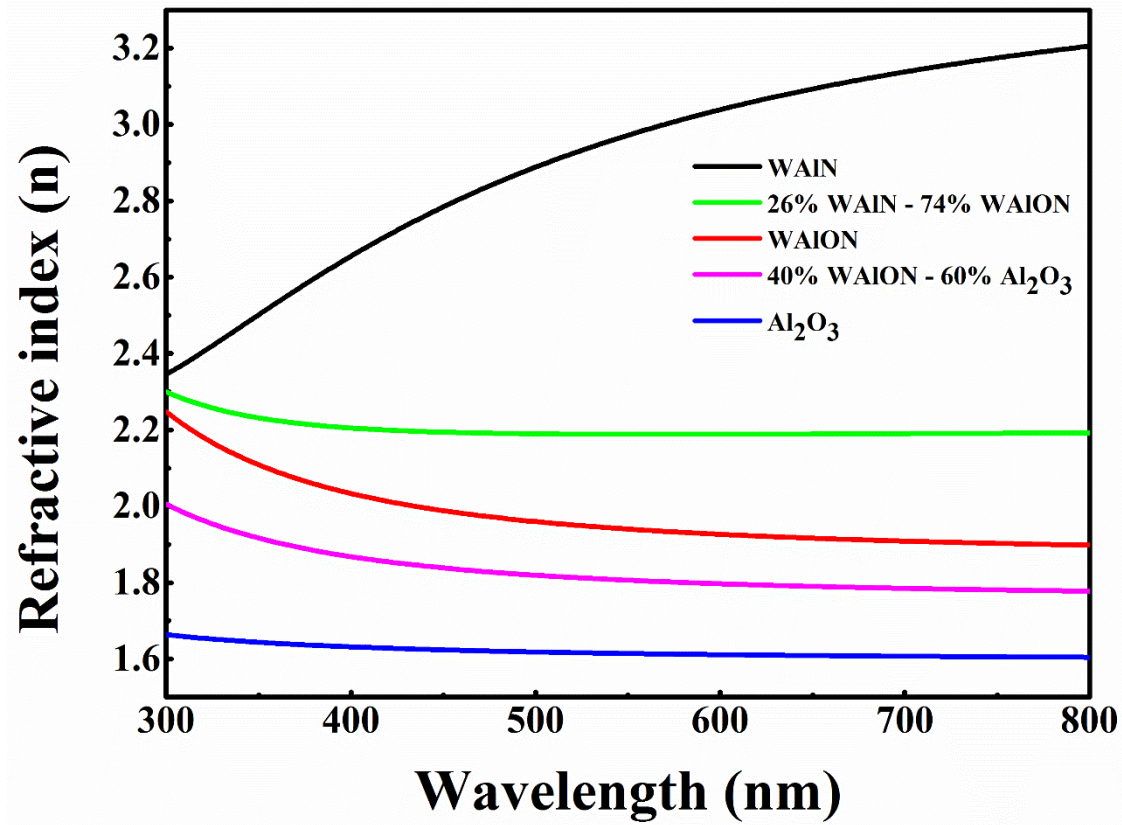
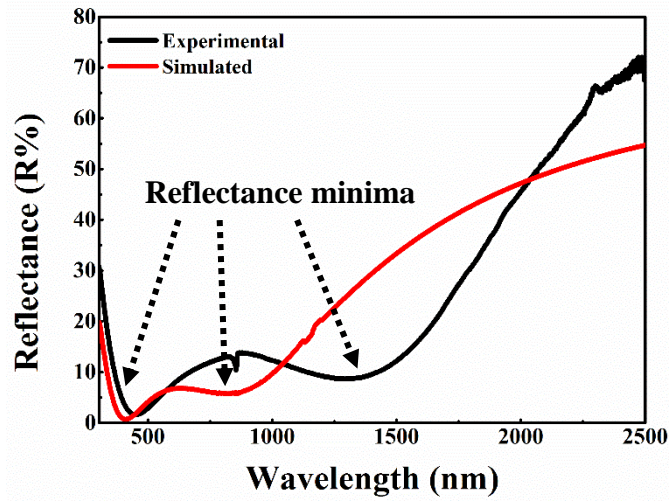
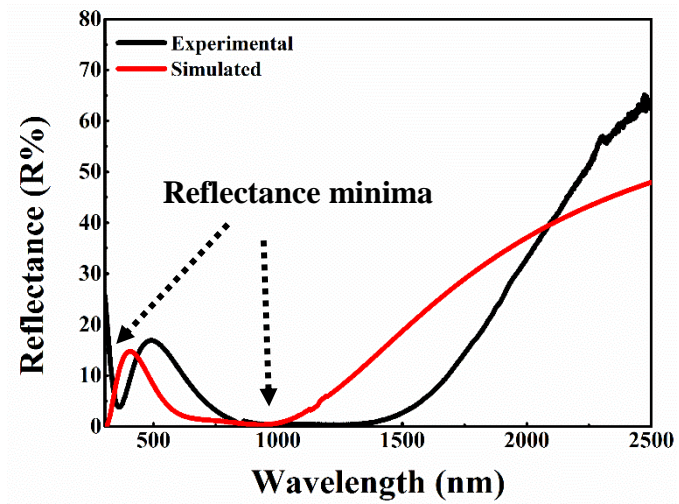


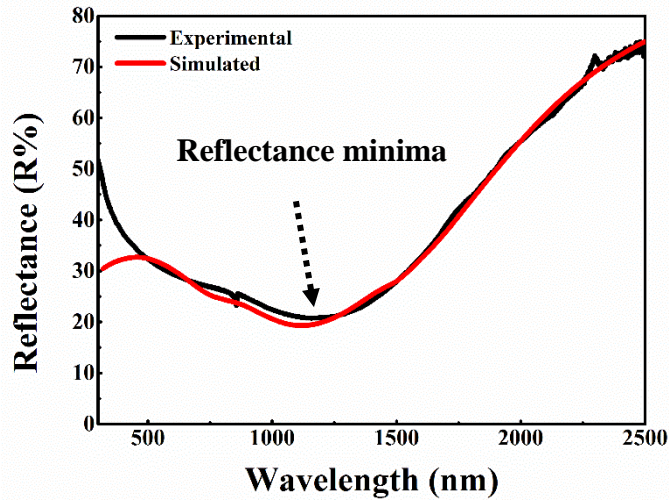
Fig. 6. (a) Refractive index (n) and (b) extinction coefficient of individual layer of multilayer stack (see inset in Fig. 5(b)).



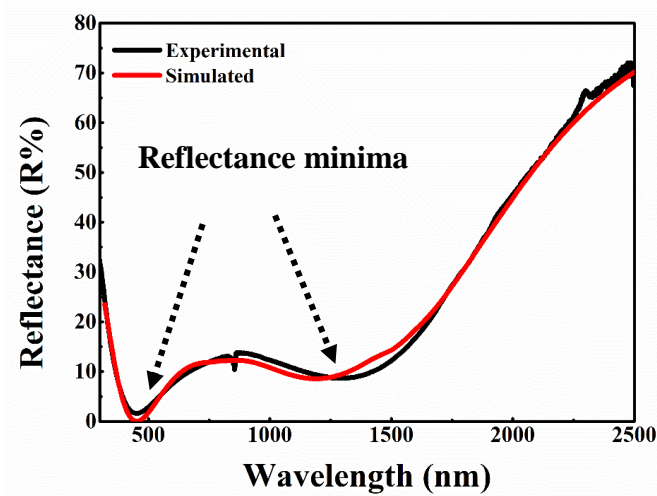
(a)



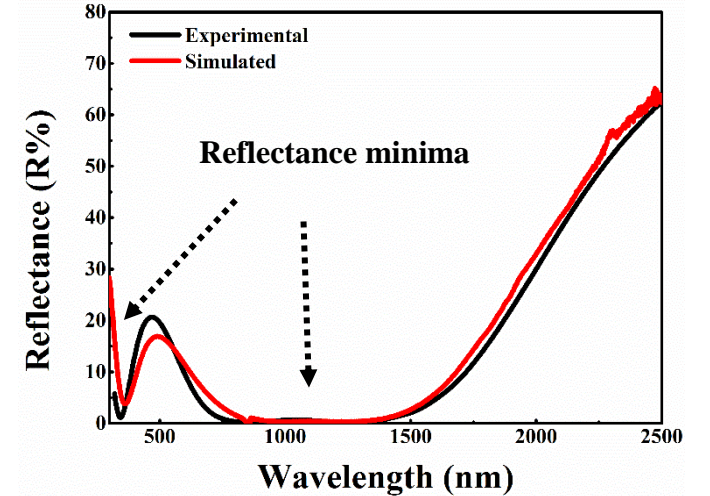
(b)



(c)



(d)



(e)

Fig. 7. Experimental (black) and simulated (red) reflectance spectra of (a) SS/WAIN/WAlON, (b) SS/WAIN/WAlON/Al₂O₃, (c) SS/WAIN, (d) SS/WAIN/WAIN-WAlON/WAlON, and (e) SS/WAIN/WAIN-WAlON/WAlON/WAlON-Al₂O₃/Al₂O₃ coatings in solar wavelength range.