

See discussions, stats, and author profiles for this publication at: <https://www.researchgate.net/publication/280035781>

Fuzzy Based Optimization of Thrust Force and Torque during Drilling of Natural Hybrid Composites

Article in Applied Mechanics and Materials · April 2015

DOI: 10.4028/www.scientific.net/AMM.787.265

CITATIONS

16

READS

95

4 authors, including:



R. Vinayagamorthy

Sri Chandrasekharendra Saraswathi Viswa Mahavidyalaya University

43 PUBLICATIONS 699 CITATIONS

SEE PROFILE

Some of the authors of this publication are also working on these related projects:



Influence of fiber surface modifications on the mechanical behavior of Vetiveria zizanioides reinforced polymer composites [View project](#)

Fuzzy based optimization of thrust force and torque during drilling of natural hybrid composites

R Vinayagamorthy^{1, a*}, N Rajeswari^{2, b}, S. Sivanarasimha^{3, c}
and K. Balasubramanian^{4, d}

¹ Research Scholar, Department of Mechanical Engineering, Dr. M.G.R Educational and Research Institute University, Maduravoyal, Chennai- 600095, India.

² Professor, Department of Mechanical Engineering, Veltech Multitech Dr. Rangarajan Dr. Sakunthala Engineering College, Chennai - 600062, India.

³ B.E Student of Mechanical Engineering, SCSVMV University, Enathur, Kancheepuram – 631561, India.

⁴ Principal, Vel Tech Engineering College, Chennai - 600062, India

^{a*} vmmailbox@rediffmail.com, ^b raji_bala2010@ymail.com, ^c sivanarasimha92@gmail.com, ^d bala_manu2002@yahoo.co.in.

Key words: natural composite, optimization, machinability

Abstract: This investigation was done to study machinability during drilling on sandwich laminates. Vetiver and jute were used as natural fibers and glass was used as synthetic fibers in vinyl ester matrix in the form of laminates by varying the fiber content in each laminate. The laminates were drilled during which spindle speed, spindle feed rate, tool point angle and sample laminate were modified using D-optimal design technique. During drilling of each hole, thrust force and torque developed were noted as outputs. The outputs were optimized to observe best drilling conditions. A fuzzy model was created and its predictions for trial conditions were noted. A comparison between trial values, regression values and fuzzy values was made. Confirmatory trials were made for optimum set of runs and outputs were again noted. The percentage of error between the model, confirmatory trials and fuzzy were found to be meagre and hence concluded that the optimization was satisfactory.

Introduction

During ultrasonic drilling on glass fiber epoxy plastics, it was reported that hole surface roughness increases when power rating and grain size were increased. Also, maximum hole surface roughness was observed at entrance side than at exit side [1]. In another research, sandwich laminates were prepared by using sisal and glass as reinforcements in vinyl ester matrix. Drilling experiments on the developed samples reported that feed rate has the predominant influence on the delamination [2]. A drilling study was done on medium density fiber boards and concluded that feed rate and drill size are predominantly affecting the thrust force and this happened due to increase in shear area at high feed and drill size conditions [3]. A research work has been carried out on milling of jute fibers composites and concluded that thrust force and torque were majorly affected by input factors like spindle speed, spindle feed rate and depth of cut [4]. In present investigation, sandwich laminates were prepared by using natural as well as synthetic reinforcements. The laminates were subjected to a drilling in accordance with D-optimal design technique. Two outputs namely thrust force and torque developed were noted and optimized.

Experimental

Composite laminates were made by using hand layup technique in the size of 350 x 350 x 12 mm. Vetiver was pre-treated in sodium hydroxide in order to remove the cellulosic substances. After this treatment, the fibers were heated in furnace in order to enhance its bonding ability with resin [5]. The proportions of vetiver, jute and glass were varied and maintained as 34 % put together whereas the resin content was maintained as 66 % in all laminates. Laminate I was made with 17 % of vetiver and 17 % of jute, Laminate II was made with 13 % of vetiver, 13 % of jute and 8 % of glass and laminate III was made with 10 % of vetiver, 10 % of jute and 14 % of glass.

Drilling operations were done by using computer numerical machining center. Four high speed steel drill tools of 10 mm diameter were purchased and their point angles were modified to 60° , 90° , 120° and 150° . A Kistler make force dynamometer was used to measure the thrust force and torque during drilling. Speed, feed rate and point angle were selected as 4-level numerical input factors and sample laminate was selected as a 3-level categorical input factor. Thus, selected model was a D-optimal model with mixed levels. The identification of input factors was based on the previous literatures done in the field of drilling [6-8]. The numerical values for speed (n) were assigned as 500 rpm, 1000 rpm, 1500 rpm and 2000 rpm, feed rate (f) were assigned as 0.1 mm/rev, 0.2 mm/rev, 0.3 mm/rev and 0.4 mm/rev, point angle were assigned as mentioned earlier. The categorical factor for sample laminate (D) was assigned as I, II and III levels.

Table 3. Experimental trial runs and measured outputs

| Run | Speed (rpm) | Feed (mm/rev) | Point angle (degree) | laminate | Experimental | | Regression | | Fuzzy | |
|-----|-------------|---------------|----------------------|----------|--------------------|---------------|--------------------|---------------|--------------------|---------------|
| | | | | | Thrust force F (N) | Torque T (Nm) | Thrust force F (N) | Torque T (Nm) | Thrust force F (N) | Torque T (Nm) |
| 1 | 500 | 0.2 | 60 | III | 102.1 | 6.27 | 103.2 | 6.83 | 100.6 | 6.3 |
| 2 | 500 | 0.1 | 60 | II | 90.3 | 5.21 | 89.45 | 5.45 | 91.2 | 5.3 |
| 3 | 1000 | 0.4 | 150 | I | 94.8 | 4.72 | 95.1 | 4.66 | 95.3 | 4.8 |
| 4 | 1000 | 0.1 | 120 | II | 94.1 | 4.9 | 94 | 5.03 | 93.5 | 5 |
| 5 | 2000 | 0.1 | 90 | III | 99.3 | 5.73 | 99.18 | 6.1 | 98.8 | 5.2 |
| 6 | 2000 | 0.3 | 90 | I | 86.3 | 4.94 | 85.27 | 5.8 | 86.1 | 5.1 |
| 7 | 500 | 0.4 | 150 | III | 120.4 | 6.49 | 121.2 | 5.58 | 121 | 6.5 |
| 8 | 1500 | 0.1 | 60 | I | 82.7 | 4.32 | 83.91 | 4.23 | 83.1 | 4.2 |
| 9 | 500 | 0.3 | 150 | II | 99.3 | 4.11 | 100.1 | 4.1 | 99 | 4.2 |
| 10 | 2000 | 0.1 | 150 | I | 89.5 | 4.81 | 90.2 | 5.08 | 88.9 | 5 |
| 11 | 2000 | 0.4 | 60 | III | 111.4 | 7.08 | 110.5 | 7.1 | 110.7 | 7.1 |
| 12 | 2000 | 0.4 | 150 | II | 105.5 | 5.6 | 106.11 | 5.67 | 105.9 | 5.2 |
| 13 | 2000 | 0.1 | 60 | II | 91.6 | 5.19 | 90.51 | 5.2 | 92.9 | 5.2 |
| 14 | 500 | 0.1 | 120 | I | 88.7 | 4.02 | 89 | 4.04 | 87.2 | 4 |
| 15 | 2000 | 0.2 | 150 | III | 109 | 6.02 | 109.2 | 6.05 | 108.7 | 6 |
| 16 | 500 | 0.1 | 150 | III | 107.6 | 5.48 | 108.02 | 5.1 | 106.9 | 5.5 |
| 17 | 500 | 0.4 | 60 | II | 102.5 | 5.89 | 103.6 | 5.23 | 103.1 | 5.4 |
| 18 | 500 | 0.4 | 60 | I | 90.9 | 5.1 | 90.76 | 5 | 91 | 5 |
| 19 | 1500 | 0.3 | 60 | II | 96.3 | 5.48 | 95.89 | 5.11 | 97.2 | 5.1 |
| 20 | 1000 | 0.4 | 90 | III | 114.5 | 6.7 | 114.19 | 6.79 | 113.2 | 6.2 |
| 21 | 2000 | 0.3 | 150 | I | 90.4 | 4.56 | 89.2 | 4.34 | 91 | 4.4 |
| 22 | 2000 | 0.2 | 120 | II | 91.5 | 5.39 | 92.34 | 5.33 | 92 | 5.3 |
| 23 | 2000 | 0.4 | 120 | III | 115.3 | 6.54 | 114.27 | 6.31 | 114.7 | 6.3 |
| 24 | 500 | 0.1 | 120 | I | 87.2 | 4.01 | 86.4 | 4 | 86.7 | 4 |
| 25 | 2000 | 0.4 | 150 | II | 106.4 | 5.5 | 106.82 | 5.6 | 106 | 5.1 |
| 26 | 500 | 0.4 | 60 | I | 91.5 | 4.18 | 90.12 | 4.19 | 92 | 4.2 |
| 27 | 500 | 0.1 | 150 | III | 108.3 | 5.5 | 108.45 | 5.56 | 107.6 | 5.6 |
| 28 | 2000 | 0.4 | 60 | III | 110.3 | 7.1 | 110.22 | 7.14 | 110.5 | 7.2 |

Error between Experimental and Regression: F = 0.81%, T = 0.73 %,
Error between Experimental and Fuzzy: F = 0.7%, T = 0.6%

Design of Experiment

This research work utilizes D-optimal model for design and optimization. D-optimal model would be effectively used when the output is influenced by a mixture of numerical and categorical factors. It also effectively optimizes the output influenced by input factors with unequal levels. Analysis of variance was used to study the predominance of input factors on the output. The experimental trials followed and observed outputs were shown in Table 3.

Discussions

Thrust force (F). The combined ANOVA analysis was shown in Table 4. The F-values of model and lack of fit show that the model is significant. Adequacy of the model was verified by the closeness of R^2 and adj R^2 values. As they are very closer, the model was adequate for predicting the outputs. The contribution values as presented shows that the sample laminate, feed rate and tool angle were majorly influencing the thrust force. A maximum contribution of 55.24 % was noticed with sample laminate. This clearly shows that the proportions of fibers in laminate plays a vital role in deciding the thrust force.

Table 4. Consolidated ANOVA Table

| Entity/Factor | Square sum | DOF | Mean square | F-value | p-value | Contribution % | R ² | Adj-R ² | Adequate precision (AP) |
|------------------|------------|-----|-------------|---------|---------|-----------------|----------------|--------------------|-------------------------|
| Thrust Force (F) | | | | | | | | | |
| Model | 2803.5 | 17 | 164.91 | 115.6 | <0.0001 | Significant | 0.995 | 0.986 | 38.5 |
| Speed (n) | 6.12 | 1 | 6.12 | 4.29 | 0.0651 | 0.22 | | | |
| Feed (f) | 408.03 | 1 | 408.03 | 286.2 | <0.0001 | 14.5 | | | |
| Tool angle (α) | 130.82 | 1 | 130.82 | 91.77 | <0.0001 | 4.64 | | | |
| Work (D) | 1556.5 | 2 | 778.22 | 545.8 | <0.0001 | 55.24 | | | |
| Lack of fit | 11.7 | 5 | 2.34 | 4.57 | 0.0605 | - | | | |
| Pure error | 2.56 | 5 | 0.51 | - | - | No | | | |
| Total | 2817.7 | 27 | - | - | - | - | | | |
| Torque (T) | | | | | | | | | |
| Model | 20.82 | 17 | 1.22 | 13.16 | <0.0001 | Significant | 0.95 | 0.9 | 12.2 |
| Speed (n) | 0.73 | 1 | 0.73 | 7.88 | 0.0185 | 3.35 | | | |
| Feed (f) | 2.02 | 1 | 2.02 | 21.7 | 0.0009 | 9.29 | | | |
| Tool angle (α) | 0.82 | 1 | 0.82 | 8.84 | 0.014 | 3.77 | | | |
| Work (D) | 12.04 | 2 | 6.02 | 64.64 | <0.0001 | 55.35 | | | |
| Lack of Fit | 0.5 | 5 | 0.1 | 1.17 | 0.433 | - | | | |
| Pure error | 0.43 | 5 | 0.086 | - | - | No Significance | | | |
| Total | 21.75 | 27 | - | - | - | - | | | |

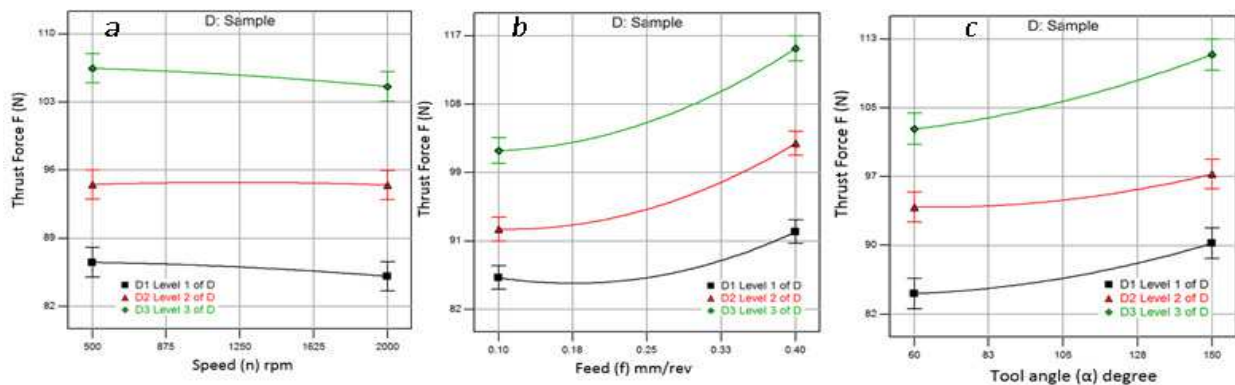


Figure 1: Interaction plots (a) F vs n (b) F vs f (b) F vs α and

Interaction plots for thrust force were presented in Fig. 1. Fig 1a clearly shows that speed has no much importance on thrust force as there was a meagre variation of thrust when speed was varied. When feed rate was increased, thrust force also increases for laminates II and III whereas for laminate I, thrust force shows slight decrease until 0.15 mm/rev thereafter there found to be an increase in thrust force. This increase in thrust force may be of the fact that at high feed rates, the rate of penetration of tool on laminate increases. This creates high thrust force on the laminate surface. When tool angle was increased, the area of contact of the tool with laminate surface increases thus boosting thrust force. The observed behaviors were quite common in all laminates but, laminate I show a minimum thrust force than laminate II and III. This clearly indicates that the presence of glass reinforcement raises the thrust force considerably [9]. Hence, laminate I was suitable for drilling under minimum thrust force.

Torque (T). The F-values of model and lack of fit shows that the model is significant from Table 4. As R² and adj R² values are very closer, the model was adequate for predicting the outputs. The contribution values as presented shows that all the input factors were majorly influencing the torque. The laminates contribution of 55.35 % shows that the reinforcement content in laminate plays a vital role in deciding the torque. Interaction plots for torque were shown in Fig. 2. Fig. 2a shows that increase in spindle speed increases the torque value for laminate I and II whereas laminate III show a constant torque value. Fig 2b shows that, increase in feed rate increases the torque value after a value nearer to 0.15 mm/rev. Fig 2c also shows that, increase in tool angle decreases the torque rapidly for laminates II and III whereas for laminate I there was only a meagre

decrease in torque. A comparison between the laminates clearly infers that laminate I shows minimum torque under all conditions. Thus it may be concluded that natural reinforcements namely vetiver and jute as a replacement for glass made positive effect on machinability. A second order regression equations for outputs were developed and presented in Table 5.

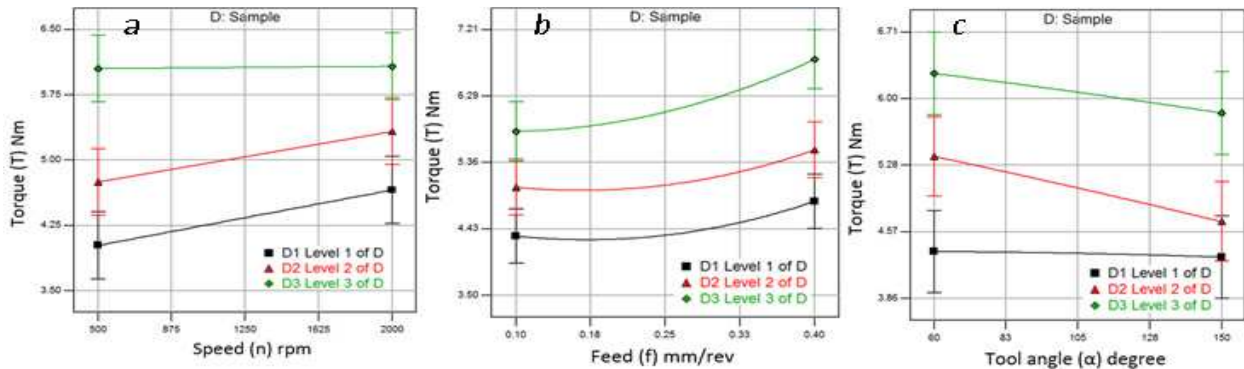


Figure 2: Interaction plots(a) Tvs n (b) Tvs f (b) Tvs α and

Table 5. Table of regression equations

| Response | Equation |
|------------|--|
| Thrust (F) | $F_I = 88.23 - 7.2E-4n - 36.68f - 0.042\alpha + 4.42E-4nf + 6.9E-6n\alpha - 0.057f\alpha - 4.26E-7n^2 + 129f^2 + 5.24E-4\alpha^2$ |
| | $F_{II} = 94.11 + 2E-4n - 22.8f - 0.063\alpha + 4.42E-4nf + 6.9E-6n\alpha - 0.057f\alpha - 4.26E-7n^2 + 129f^2 + 5.24E-4\alpha^2$ |
| | $F_{III} = 99.51 - 1.01E-3n - 15.8f - 0.012\alpha + 4.42E-4nf + 6.9E-6n\alpha - 0.057f\alpha - 4.26E-7n^2 + 129f^2 + 5.24E-4\alpha^2$ |
| Torque (T) | $T_I = 4.3 - 5.6E-5n - 2.38f - 1.16E-3\alpha + 2.51E-4nf + 4.02E-6n\alpha - 0.0134f\alpha - 2E-9n^2 + 10.25f^2 + 5.26E-6\alpha^2$ |
| | $T_{II} = 5.76 - 9.28E-5n - 2.25f - 8.24E-3\alpha + 2.51E-4nf + 4.02E-6n\alpha - 0.0134f\alpha - 2E-9n^2 + 10.25f^2 + 5.26E-6\alpha^2$ |
| | $T_{III} = 6.52 - 4.64E-4n - 0.64f - 5.2E-3\alpha + 2.51E-4nf + 4.02E-6n\alpha - 0.0134f\alpha - 2E-9n^2 + 10.25f^2 + 5.26E-6\alpha^2$ |

Optimization

A multiple optimization technique was done with an objective of minimizing the outputs. The optimization technique was carried out on the basis of desirability approach. Using this approach, there found to be more than one optimum condition. These conditions would be selected based on the desirability values which are closer to unity. A set of seven optimum conditions were taken and confirmatory trials have been conducted for these conditions.

Fuzzy modelling

Fuzzy modeling starts with fuzzification process during which membership functions were created for input and output factors. A triangular type membership function [10] was made by taking three values namely low, medium and high as shown in Fig. 3. The next step was the defuzzification process in which membership functions were reduced in to a most representative value. During this stage, set of rules containing IF-THEN statements were framed based on the runs shown in Table 5. Fuzzy gives a prediction plot from which output responses could be predicted for input values. The developed model was validated by comparing the D-optimal values with confirmatory trials and with fuzzy predictions. The error between each analysis was calculated and shown Fig. 4. These error were found to be minimum for both thrust force and torque. Hence, the optimization was found to be highly satisfactory.

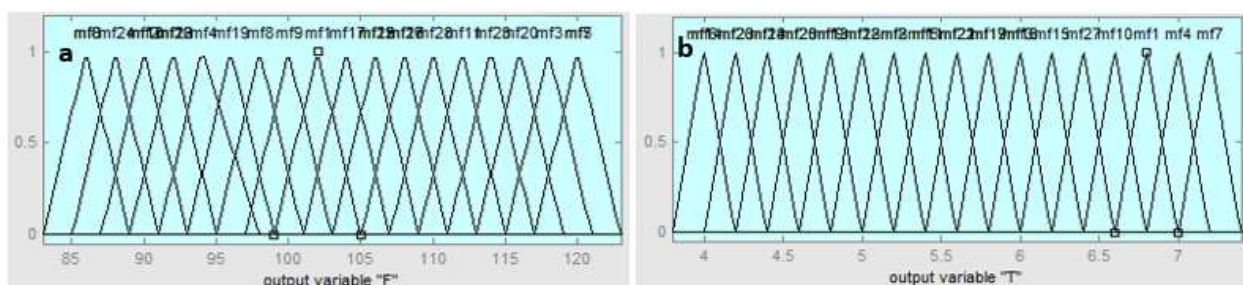


Figure. 3 Membership plot for (a) Thrust force (b) Torque

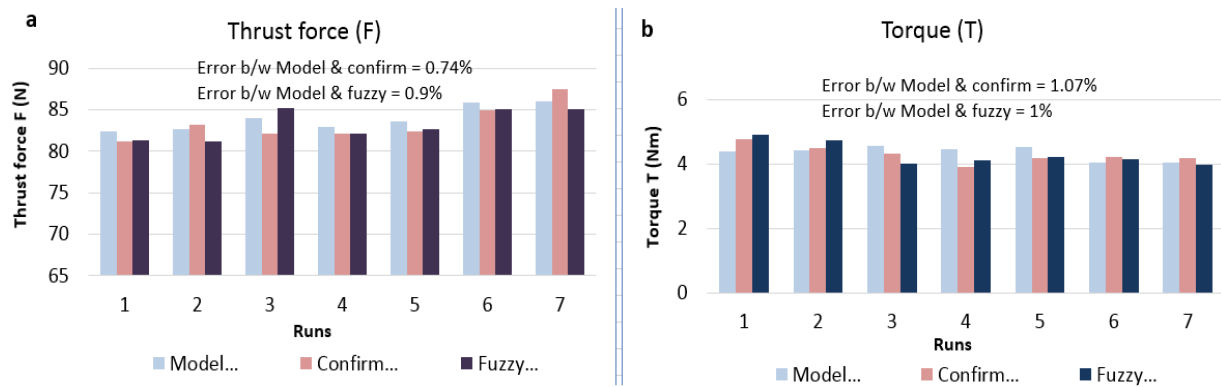


Figure 4: Comparison between Model, Confirmatory and Fuzzy models (a) Thrust (b) Torque

Conclusion

1. Sample laminate, feed rate and point angle were found to have major contribution on thrust force. All factors have major influence on torque.
2. There found to be a highest contribution of 55 % for sample laminate with thrust force and torque. This shows that the natural reinforcement content plays a vital role in deciding the thrust force and torque. Inclusion of glass fibers creates development of thrust force and torque. Hence, sample I containing only natural fibers improved machinability.
3. The developed model shows good agreement with confirmatory runs and fuzzy values. Hence the optimization is highly satisfactory.

References

- [1] Kishore Debnath, Inder deep Singh, Akshay Dvivedi, Evaluation of surface roughness during rotary mode ultrasonic drilling of glass/epoxy composite laminates, *J. Prod. Eng.* 17(2014) 16-20.
- [2] S. Velumani, P. Navaneethakrishnan, S. Jayabal, R. Ramprasath, Regression modelling and optimization of cutting parameters through Nelder-Mead simplex search and CCFD during drilling of sisl-glass/vimyl ester composites, *Int. J. Mach. Mach. Mater.* 14(2013) 1-23.
- [3] S. Prakash, K. Palanikumar, A. Krishnamoorthy, Thrust force evaluation in drilling medium density fibre boards using design of experiments, *Int. J. Adv. Manuf. Technol.* 25 (2012) 95-112.
- [4] R. Vinayagamoorthy, N. Rajeswari, Analysis of cutting forces during milling of natural fibered composites using Fuzzy logic, *Int. J. Compos. Mater. Manuf.* 2 (2012) 15-21.
- [5] R. Vinayagamoorthy, N. Rajeswari, Mechanical performance studies on *Vetiveria zizanioides*/Jute/glass fiber-reinforced hybrid polymeric composites, *J. Reinf. Plast. Compos.* 33 (2014) 81-92.
- [6] S. Jayabal, U. Natarajan, U. Sekar, Regression modeling and optimization of machinability behavior of glass-coir-polyester hybrid composite using factorial design methodology, *Int. J. Adv. Manuf. Technol.* 55(2011) 263-273.
- [7] S. Jayabal, U. Natarajan, Optimization of thrust force, torque, and tool wear in drilling of coir fiber-reinforced composites using Nelder-Mead and genetic algorithm methods, *Int. J. Adv. Manuf. Technol.* 51 (2010) 371-381.
- [8] Birhan Işık, Ergün Ekici, Experimental investigations of damage analysis in drilling of woven glass fiber-reinforced plastic composites. *Int. J. Adv. Manuf. Technol.* 49 (2010) 861-869.
- [9] K. Mohamed Kaleemulla, B. Siddeswarappa, Effect of fibre content and laminate thickness on the drilling behavior of GSFRRP composites under varied drill geometries, *Int. J. Mach. Mach. Mater.* 10(2011) 222-234.
- [10] T. Rajasekaran, K. Palanikumar and B. K. Vinayagam, Application of fuzzy logic for modeling surface roughness in turning CFRP composites using CBN tool, *J. Prod. Eng. Res.* 5(2011) 191-199.