

# Overlap-based Vocabulary Generation Improves Cross-lingual Transfer Among Related Languages

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## Abstract

Pre-trained multilingual language models such as mBERT and XLM-R have demonstrated great potential for zero-shot cross-lingual transfer to low web-resource languages (LRL). However, due to limited model capacity, the large difference in the sizes of available monolingual corpora between high web-resource languages (HRL) and LRLs does not provide enough scope of co-embedding the LRL with the HRL, thereby affecting the downstream task performance of LRLs. In this paper, we argue that *relatedness* among languages in a language family along the dimension of lexical overlap may be leveraged to overcome some of the corpora limitations of LRLs. We propose **Overlap BPE (OBPE)**, a simple yet effective modification to the BPE vocabulary generation algorithm which enhances overlap across related languages. Through extensive experiments on multiple NLP tasks and datasets, we observe that OBPE generates a vocabulary that increases the representation of LRLs via tokens shared with HRLs. This results in improved zero-shot transfer from related HRLs to LRLs without reducing HRL representation and accuracy. Unlike previous studies that dismissed the importance of token-overlap, we show that in the low-resource related language setting, token overlap matters. Synthetically reducing the overlap to zero can cause as much as a four-fold drop in zero-shot transfer accuracy.

## 1 Introduction

Zero-shot cross-lingual transfer is the ability of a model to learn from labeled data in one language and transfer the learning to another language without any labeled data. Transformer (Vaswani et al., 2017) based multilingual models pre-trained on unlabeled data from multiple languages are the state-of-the-art means for cross-lingual transfer (Ruder

et al., 2019; Devlin et al., 2019a). While pre-training based cross-lingual transfer holds great promise for low web-resource languages (LRLs), such techniques are found to be more effective for transfer within high web-resource languages (HRLs) (Wu and Dredze, 2020).

Vocabulary generation is an important step in multilingual model training, where vocabulary size directly impacts model capacity. Usually, the vocabulary is generated from a union of HRL and LRL data. This often results in under-allocation of vocabulary bandwidth to LRLs, as LRL data is significantly smaller in size compared to HRL. This under-allocation of model capacity results in lower LRL performance (Wu and Dredze, 2020), as mentioned previously. In response, prior research has explored development of region-specific models (Antoun et al.; Khanuja et al., 2021), generating vocabulary specific to language clusters (Chung et al., 2020), and exploring relatedness among languages to build better LMs for LRLs (Khemchandani et al., 2021). However, none of these methods have utilized relatedness among languages for better vocabulary generation during multilingual pre-training.

In this paper, we hypothesize that exploiting language relatedness can result in an overall more effective vocabulary, which is also better representative of LRLs. Closely related languages (e.g., languages belonging to a single family) have common origins for words with similar meanings. We show some examples across three different families of related languages in Table 10. Morphological inflections of the root word lead to lexically overlapping tokens across languages. Learning representations for such subwords in lexically overlapping words shared across HRL and its related LRLs can enable better transfer of supervision from HRL to LRLs. During Masked Language Modelling (MLM) pre-training (Devlin et al., 2019a), the shared tokens can serve as anchors in learning contextual representations of neighboring tokens. However, choos-

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Language and Token frequencies	English: <b>University</b> (10), versity (6); German: <b>Universitäten</b> (2); Dutch: <b>Universiteit</b> (1); Western Frisian: <b>Universiteiten</b> (1)
Starting Vocab	Uni, versit, U,n,i,v,e,r,s,i,t,y,a
BPE Vocab	versity, Uni, versit, U,n,i,v,e,r,s,i,t,y,a
OBPE Vocab	<b>Universit</b> , Uni, versit, U,n,i,v,e,r,s,i,t,y,a

Table 1: First row shows lexically overlapping tokens in four different languages with their corpus frequencies (in brackets), with English (En) as the High Web-Resource Language (HRL). From a starting vocabulary shown in the second row, BPE merges tokens based on greater overall frequency, adding new vocabulary item *versity* as it has the highest overall frequency (16). OBPE instead adds *Universit* since it also rewards cross-lingual overlap, even though *Universit* has lower overall frequency (15).

ing the correct granularity of sharing automatically is tricky. On one extreme, we can choose a vocabulary which favours longer units frequent in HRL without regard for sharing, thereby leading to better semantic representation of the tokens but no cross-lingual transfer. On the other extreme, we can choose character-level vocabulary (Ma et al., 2020), where every token is shared across languages but have no semantic significance.

Given text from a mix of high and low Web-resource languages (HRL and LRL, respectively), Byte Pair Encoding (BPE) (Sennrich et al., 2016) and its variants like Wordpiece (Schuster and Nakajima, 2012) and Sentencepiece (Kudo and Richardson, 2018) prefer frequent tokens, most of those from the HRLs. This would cause most long HRL tokens to get included, leaving only a limited budget of short tokens for the LRL. Any sub-token level overlap between HRL and LRL could get lost in this process. In a zero-shot setting, since available supervision is HRL based, this creates a bottleneck when transferring supervision from HRL to LRLs. Oversampling LRLs is a common strategy to offset this imbalance but that hurts HRL performance as shown in (Conneau et al., 2020a).

In this paper, we propose Overlap BPE (OBPE). OBPE chooses a vocabulary by giving token overlap among HRL and LRLs a primary consideration. OBPE prefers vocabulary units which are shared across multiple languages, while also encoding the input corpora compactly. Thus, OBPE tries to balance the trade-off between cross-lingual subword sharing and the need for robust representation of individual languages in the vocabulary. This re-

sults in a more balanced vocabulary, resulting in improved performance for LRLs without hurting HRL accuracy. Table 1 shows an example to highlight this difference between OBPE and BPE.

Recently K et al. (2020); Conneau et al. (2020b) concluded that token overlap is unimportant for cross-lingual transfer. However, they studied language pairs where either both languages had a large corpus, or where the languages were not sufficiently related. We focus on related languages within a family and observe drastic drop in zero-shot accuracy when we synthetically reduce the overlap to zero (58% F1 drops to 17% for NER, 71% drops to 30% for text classification).

This paper offers the following contributions

- We present OBPE, a simple yet effective modification to the popular BPE algorithm to promote overlap between LRLs and a related HRL during vocabulary generation. OBPE uses a generalized mean based formulation to quantify token overlap among languages.
- We evaluate OBPE on twelve languages across three related families, and show consistent improvement in zero-shot transfer over state-of-the-art baselines on four NLP tasks. We analyse the reasons behind the gains obtained by OBPE and show that OBPE increases the percentage of LRL tokens in the vocabulary without reducing HRL tokens. This is unlike over-sampling strategies where increasing one reduces the other.
- Through controlled experiments on the amount of token overlap on a related HRL-LRL pair, we show that token overlap is extremely important in the low-resource, related language setting. Recent literature which conclude that token overlap is unimportant may have overlooked this important setting.

The source code for our experiments is available at <https://github.com/Vaidehi99/OBPE>.

## 2 Related Work

Transformer-based multilingual language models such as mBERT (Devlin et al., 2019b) and XLM-R (Conneau et al., 2020a) are now established as the de-facto method for zero-shot cross-lingual transferability, and thus hold promise for low resource domains. However, recent studies have indicated that even the current state-of-the-art models such as XLM-R (Large) do not yield reasonable transfer performance across low resource target languages

with limited data (Wu and Dredze, 2020). This has led to a surge of interest in enhancing cross-lingual transfer of multilingual models to the low-resource setting. We categorize existing work based on the stage of the pre-training pipeline where it is relevant:

**Input Data** In the data creation stage, Conneau et al. (2020a) propose over-sampling of LRL documents to improve LRL representation in the vocabulary and pre-training steps. Khemchandani et al. (2021) specifically target related languages and propose transliteration of LRL documents to the script of related HRL for greater lexical overlap. We deploy both these tricks in this paper.

**Tokenization** Rust et al. (2021) study that even the tokenization step could have a crucial impact on performance accrued to each language in a multilingual models. They propose the use of dedicated tokenizer for each language instead of the automatically generated multilingual mBERT tokenizer. However, they continue to use the default mBERT vocabulary generator.

**Vocabulary Generation** Sennrich et al. (2016) highlighted the importance of subword tokens in the vocabulary and proposed use of the BPE algorithm (Gage, 1994) for efficiently growing such a vocabulary incrementally. Variants like Wordpiece (Schuster and Nakajima, 2012) and Sentencepiece (Kudo and Richardson, 2018) either build on top of BPE or follow a very similar process. Kudo (2018) is a variant method that chooses tokens based on unigram LM score. We obtained better results with BPE and continued with that. All these BPE variants incrementally add subwords based on overall frequency in the combined corpus, and they all ignore language boundaries. Chung et al. (2020) observed that such a combined approach could under-represent several languages, and proposed instead to separately create vocabularies for clusters of related languages and take a union of each cluster-specific vocabulary. However, within each cluster they continue to use the default vocabulary generator. Our approach can be used as a drop-in replacement to further enhance the quality of the cluster-specific vocabulary that they obtain. Wang et al. (2019); Gao et al. (2020) propose a soft-decoupled encoding approach for exploiting subword overlap between LRLs and HRLs. However, their focus is NMT models and does not easily integrate in existing multilingual models such as mBERT. (Maronikolakis et al., 2021) targets tok-

enization compatibility based purely on vocabulary size and does not focus on choosing the tokens that go in the vocabulary.

**Pre-Training and Adaptation** Several previous works have proposed to include additional alignment loss between parallel (Cao et al., 2020) or pseudo-parallel (Khemchandani et al., 2021) sentences to co-embed HRLs and LRLs. Another approach is to design language-specific Adapter layers (Pfeiffer et al., 2020a,b; Artetxe et al., 2020; Üstün et al., 2020) that can be easily fine-tuned for each new language. Pfeiffer et al. (2021) leverages the pre-trained embeddings of lexically overlapping tokens between the vocabulary of pre-trained model and that of unseen target language to initialize the corresponding embeddings of target language. However, they did not attempt to increase the fraction of such tokens in the vocabulary.

We are not aware of any prior work that explicitly promotes overlapping tokens between LRLs and HRLs in the vocabulary of multilingual models.

### 3 Overlap-based Vocabulary Generation

We are given monolingual data  $D_1, \dots, D_n$  in a set of  $n$  languages  $\mathcal{L} = \{L_1, \dots, L_n\}$  and a vocabulary budget  $V$ . Our goal is to generate a vocabulary  $\mathcal{V}$  that when used to tokenize each  $D_i$  in a multilingual model would provide cross-lingual transfer to LRLs from related HRLs. We use  $\mathcal{L}_{\text{LRL}}$  to denote the subset of the  $n$  languages that are low-resource, the remaining languages  $\mathcal{L} - \mathcal{L}_{\text{LRL}}$  are denoted as the set  $\mathcal{L}_{\text{HRL}}$  of high resource languages.

Existing methods of vocabulary creation start with a union  $D$  of monolingual data  $D_1, \dots, D_n$ , and choose a vocabulary  $\mathcal{V}$  that most compactly represents  $D$ . We first present an overview of BPE, a popular algorithm for vocabulary generation.

#### 3.1 Background: BPE

Byte Pair Encoding (BPE) (Gage, 1994) is a simple data compression technique that chooses a vocabulary  $\mathcal{V}$  that minimizes total size of  $D = \cup_i D_i$  when encoded using  $\mathcal{V}$ .

$$\mathcal{V} = \operatorname{argmin}_{S:|S|=V} \sum_{i=1}^n |\operatorname{encode}(D_i, S)| \quad (1)$$

The size of the encoding  $|\operatorname{encode}(D_i, S)|$  can be alternately expressed as the sum of frequency of tokens in  $S$  when  $D_i$  is tokenized using  $S$ . This motivates the following efficient greedy algorithm to implement the above optimization (Sennrich et al.,

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**Algorithm 1** Overlap based BPE (OBPE)

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for  $i \in \{1, 2, \dots, n\}$  do
  Split words in  $D_i$  into characters  $C_i$  with a special
  marker after every word
end for
 $\mathcal{V} = \cup_{i=1}^n C_i$ 
while  $|\mathcal{V}| < V$  do
  Update token and pair frequency on  $\{D_i\}, \mathcal{V}$ 
  Add to  $\mathcal{V}$  token  $k$  formed by merging pairs  $u, v \in \mathcal{V}$ 
  with the largest value of
  
$$(1 - \alpha) \sum_j f_{kj} + \alpha \sum_{i \in \mathcal{L}_{\text{LRL}}} \max_{h \in \mathcal{L}_{\text{HRL}}} \left( \frac{f_{ki}^p + f_{kh}^p}{2} \right)^{\frac{1}{p}}$$

end while
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2016). Let  $f_{ki}$  denote the frequency of a candidate token  $k$  in the corpus  $D_i$  of language  $L_i$ . The BPE algorithm grows  $\mathcal{V}$  incrementally. Initially,  $\mathcal{V}$  comprises of characters in  $D$ . Then, until  $|\mathcal{V}| \leq V$ , it chooses the token  $k$  obtained by merging two existing tokens in  $\mathcal{V}$  for which the frequency in  $D$  is maximum.

$$\mathcal{V} = \mathcal{V} \cup \operatorname{argmax}_{k=[u,v]:u,v \in \mathcal{V}} \sum_i f_{ki} \quad (2)$$

A limitation of BPE on multilingual data is that tokens that appear largely in low-resource  $D_i$  may not get added to  $\mathcal{V}$ , leading to sentences in  $L_i$  being over-tokenized. For a low resource language, the available monolingual data  $D_i$  is often orders of magnitude smaller than another high-resource language. Models like mBERT and XLM-R address this limitation by over-sampling documents of low-resource languages. However, over-sampling LRLs might compromise learned representation of HRLs where task-specific labeled data is available. We propose an alternative strategy of vocabulary generation called OBPE that seeks to maximize transfer from HRL to LRL.

### 3.2 Our Proposal: OBPE

The key idea in OBPE is to maximize the overlap between an LRL and a closely related HRL while simultaneously encoding the input corpora compactly as in BPE. When labeled data  $D_h^T$  for a task  $T$  is available in an HRL  $L_h$ , then a multilingual model fine-tuned with  $D_h^T$  is likely to transfer better to a related LRL  $L_i$  when  $L_i$  and  $L_h$  share several tokens in common. Thus, the objective that OBPE

seeks to optimize when creating a vocabulary is:

$$\mathcal{V} = \operatorname{argmin}_{S:|S|=V} \left[ (1 - \alpha) \sum_{i=1}^n |\operatorname{encode}(D_i, S)| - \alpha \sum_{i \in \mathcal{L}_{\text{LRL}}} \max_{j \in \mathcal{L}_{\text{HRL}}} \operatorname{overlap}(L_i, L_j, S) \right] \quad (3)$$

where  $0 \leq \alpha \leq 1$  determines importance of the two terms. The first term in the objective compactly represents the total corpus, as in BPE’s (Eq (1)). The second term additionally biases towards vocabulary with greater overlap of each LRL to one HRL where we expect task-specific labeled data to be present. There are several ways in which we can measure the overlap between two languages with respect to a current vocabulary. First, we encode each of  $D_i$  and  $D_j$  using the vocabulary  $S$ , which then yields a multiset of tokens in each corpus. Inspired by the literature on fair allocation (Barman et al., 2021), we explore a continuously parameterized function that expresses overlap between two languages’ encoding as a generalized mean function as follows:

$$\operatorname{overlap}(L_i, L_h, S) = \sum_{k \in S} \left( \frac{f_{ki}^p + f_{kh}^p}{2} \right)^{\frac{1}{p}}, \quad p \leq 1 \quad (4)$$

where  $f_{ki}$  denotes the frequency of token  $k$  when  $D_i$  is encoded with  $S$ . For different values of  $p$ , we get different tradeoffs between fairness to each language and overall goodness. When  $p = -\infty$ , generalized mean reduces to the minimum function, and we get the most egalitarian allocation. However, this ignores the larger of the two frequencies. When  $p = 1$ , we get a simple average which is what the first term in Equation (3) already covers. For  $p = 0, -1$ , we get the geometric and harmonic means respectively. Due to smaller size of LRL monolingual data, the frequency of a token which is shared across languages is likely to be much higher in HRL monolingual data as compared to that in LRL monolingual data, Hence, setting  $p$  to large negative values will increase the weight given to LRLs and thus increase overlap. We will present an exploration of the effect of  $p$  on zero-shot transfer in the experiment section.

The greedy version of the above objective that controls the candidate vocabulary item to be in-



Family	HRL	LRLs	Number of HRL Docs	
			BALANCED	SKEWED
West Germanic	English (en)	German (de), Dutch (nl), Western Frisian (fy)	0.16M	1.00M
Romance	French (fr)	Spanish (es), Portuguese (pt), Italian (it)	0.16M	0.50M
Indo-Aryan	Hindi (hi)	Marathi (mr), Punjabi (pa), Gujarati (gu)	0.16M	0.16M

Table 2: Twelve Languages *simulated* as HRLs and LRLs across with two different corpus distribution: BALANCED and SKEWED. Number of documents in languages simulated as LRLs is 20K.

ducted in each iteration of OBPE is thus:

$$\mathcal{V} = \mathcal{V} \cup \underset{k=[u,v]:u,v \in \mathcal{V}}{\operatorname{argmax}} (1 - \alpha) \sum_j f_{kj} + \alpha \sum_{i \in \mathcal{L}_{\text{LRL}}} \max_{h \in \mathcal{L}_{\text{HRL}}} \left( \frac{f_{ki}^p + f_{kh}^p}{2} \right)^{\frac{1}{p}} \quad (5)$$

The data structure maintained by BPE to efficiently conduct such merges can be applied with little changes to the OBPE algorithm. The only difference is that we need to separately maintain the frequency in each language in addition to overall frequency. Since the time and resources used to create the vocabulary is significantly smaller than the model pre-training time, this additional overhead to the pre-training step is negligible.

## 4 Experiments

We evaluate by measuring the efficacy of zero-shot transfer from the HRL on four different tasks: named entity recognition (NER), part of speech tagging (POS), text classification (TC), and Cross-lingual Natural Language Inference (XNLI). Through our experiments, we evaluate the following questions:

1. Is OBPE more effective than BPE for zero-shot transfer? (Section 4.2)
2. What is the effect of token overlap on overall accuracy? (Section 4.3)
3. How does increased LRL representation in the vocabulary impact accuracy? (Section 4.4)

We report additional ablation and analysis experiments in Section 4.5.

### 4.1 Setup

**Pre-training Data and Languages** As our pre-training dataset  $\{D_i\}$ , we use the Wikipedia dumps of all the languages as used in mBERT. We pre-train with 12 languages grouped into three families of four related languages as shown in Table 2. In each family, we simulate as HRL the most populous language, and call the remaining as LRLs. The number of documents for languages simulated as

Dataset split	Lang	Number of sentences			
		NER	POS	TC	XNLI
Train:HRL	hi	5.0	53.0	25.0	
	en	10.5	18.0	10.0	393.0
	fr	7.5	16.5	10.0	393.0
Validation:HRL	hi	1.0	3.0	4.0	
	en	6.0	4.0	10.0	2.5
	fr	4.0	2.0	10.0	2.5
Test data	hi	0.2	12.0	7.0	
	en	6.0	4.6	10.0	5.0
	fr	4.0	4.1	10	5.0
	mr	0.8	9.5	6.5	-
	pa	0.2	13.4	7.9	-
	gu	0.3	14.0	8.0	-
	de	12.0	19.3	10.0	5.0
	nl	8.0	1.0	-	-
	fy	0.8	-	-	-
	es	5.0	3.1	10.0	5.0
	pt	4.0	2.5	-	-
	it	5.0	3.4	-	-

Table 3: Task-specific data sizes. Number of sentences in thousands.

LRLs is set to 20K. For the HRLs, we consider two corpus distributions:

- BALANCED : all three HRLs get 160K documents each
- SKEWED : English gets one million, French half million, and Hindi 160K documents

We evaluate twelve-language models in each of these settings, and present results for separate four language models per family in Table 12 in the Appendix. For the Indo-Aryan languages set, the monolingual data of Punjabi and Gujarati is transliterated to Devanagari, the script of Hindi and Marathi. We use libindic’s indictrans library (Bhat et al., 2015) for transliteration. Languages in the other two sets do not require transliteration as they have a common script. Thus, all four languages in each set are in the same script so their lexical overlap can be leveraged.

**Pre-Training Details** To ensure that LRLs are not under-represented, we over-sample using exponentially smoothed weighting similar to multilingual BERT (Devlin et al., 2019b) with exponentiation

factor 0.7. We perform MLM pretraining on a BERT base model with 110M parameters from scratch. We generate a vocabulary of size of 30k. We chose batch size as 2048, learning rate as  $3e-5$  and maximum sequence length as 128. Pre-training of BERT was done with duplication factor 5 for for 64k iterations for HRLs. For all LRLs, duplication factor was 20 and training was done for 24K iterations. MLM pre-training was done on Google v3-8 Cloud TPUs where 10K iterations required 2.1 TPU hours.

**Task-specific Data** We evaluate on four downstream tasks: (1) NER: data from WikiANN (Pan et al., 2017) and XTREME (Hu et al., 2020), (2) XNLI: data from (Conneau et al., 2018), (3) POS: data from XTREME (Hu et al., 2020) and TDIL<sup>1</sup>, and (4) Text Classification (TC): data from TDIL and XGLUE (Liang et al., 2020). We downsampled the TDIL data for each language to make them class-balanced. The POS tagset for Indo-Aryan languages used was the BIS Tagset (Sardesai et al., 2012). Table 3 presents a summary. The test set to compute LRL perplexity was formed by sampling 10K sentences from Samanantar corpus (Ramesh et al., 2021) for Indic languages and from Tatoeba corpus<sup>2</sup> for other languages. The perplexity reported for a language is the average of sentence perplexity over all the sentences sampled from that language’s corpus.

**Task-specific fine-tuning details** We perform task-specific fine-tuning of pre-trained BERT on the task-specific training data of HRL and evaluate on all languages in the same family. Here we used learning-rate  $2e-5$  and batch size 32, with training duration as 16 epochs for NER, 8 epochs for POS and 3200 iterations for Text Classification and XNLI. The models were evaluated on a separate validation dataset of the HRL and the model with the minimum validation loss, maximum F1-score, accuracy and minimum validation loss was selected for final evaluation for XNLI, NER, POS and Text Classification respectively. All fine-tuning experiments were performed on Google Colaboratory. The results reported for all the experiments are an average of 3 independent runs.

## 4.2 Effectiveness of OBPE

We evaluate the impact of OBPE on improving zero-shot transfer from HRLs to LRLs within the

<sup>1</sup>Technology Development for Indian Languages (TDIL), <https://www.tdil-dc.in>

<sup>2</sup>Tatoeba, <https://tatoeba.org>

same family across four different tasks. We compare with four existing methods that represent different methods of vocabulary creation and allocation of budget across languages:

### Methods compared

1. **BPE** (Sennrich et al., 2016), the existing default method of vocabulary generation.
2. **Clustered vocabulary (CV)** (Chung et al., 2020) Since the paper uses a SentencePiece unigram for vocabulary, we followed the same approach for this comparison. We allocate each family equal number of vocabulary tokens which is  $V/3$ .
3. **BPE-dropout (BPE-dp)** (Provilkov et al., 2020) uses the vocabulary generated by BPE but tokenizes the text using a dropout rate of 0.1. This allows the training of tokens that are subsumed by larger tokens in the vocabulary.
4. **Compatibility of Tokenizations (Tok-Comp)** (Maronikolakis et al., 2021) uses a method to select meaningful vocabulary sizes in an automated manner for all language using compression rates. Since their best performances are found, when the compression rates are similar, we choose a size for each language corresponding to compression rate of 0.5. The tokenizer used in this method is WordPiece. .
5. **OBPE** (Ours) with default  $\alpha = 0.5, p = -\infty$ . We also do ablation on these.

In Table 4 we observe that across all four tasks, zero-shot LRL accuracy improves compared to BPE. For example, the average accuracy on XNLI for the LRL languages improves from 55.6 to 58.1 just by changing the set of tokens in the vocabulary. These gains are obtained without compromising HRL performance on the tasks. The Clustered Vocabulary (CV) approach is much worse than BPE. These experiments are on the Balanced-12 model. In the supplementary section, we report the results on the Skewed-12 (Table 5) and Balanced-4 models (Table 12) and show similar gains even with these models. In this table, we averaged the gains over nine LRLs, and in the Supplementary Table 14 we show consistent gains for individual languages.

In addition to improving zero-shot transfer from HRLs to LRLs on downstream tasks, OBPE also leads to better intrinsic representation of LRLs. We validate that by measuring the pseudo-perplexity (Salazar et al., 2020) of a test set of LRL sentences. We find that average perplexity of LRL

Method	LRL Performance ( $\uparrow$ )				HRL Performance ( $\uparrow$ )			
	NER	TC	XNLI	POS	NER	TC	XNLI	POS
BPE (Sennrich et al., 2016)	64.48	65.52	52.07	84.64	83.26	<b>82.07</b>	62.71	<b>95.20</b>
BPE-dp (Provilkov et al., 2020)	63.92	64.15	52.66	84.75	81.73	81.07	63.74	94.61
CV (Chung et al., 2020)	59.58	61.91	49.30	81.68	81.15	80.93	64.51	94.47
TokComp (Maronikolakis et al., 2021)	63.79	65.77	53.94	<b>85.49</b>	82.43	80.93	66.10	94.86
OBPE (This paper)	<b>65.72</b>	<b>68.02</b>	<b>54.03</b>	85.26	<b>83.98</b>	81.91	<b>66.27</b>	95.09

Table 4: Zero-shot performance of models in the Balanced-12 setting trained on 9 LRL and 3 HRL languages. Performance is measured on four tasks: NER (F1), Text Classification (Accuracy), POS (Accuracy), and XNLI (Accuracy). For all metrics, higher is better ( $\uparrow$ ). Zero-shot transfer to LRL improves without hurting HRL accuracy. P-value of paired-t-test between BPE and OBPE LRL gains has values 0.01, 0.04, 0.02, 0.01 for each of the 4 tasks establishing statistical significance. Detailed results for each language is presented in Table 14. Section 4.2 has further discussion.

Method	LRL Performance ( $\uparrow$ )				HRL Performance ( $\uparrow$ )			
	NER	TC	XNLI	POS	NER	TC	XNLI	POS
BPE (Sennrich et al., 2016)	52.91	51.68	48.57	74.79	81.78	80.04	64.96	95.03
CV (Chung et al., 2020)	52.73	54.40	44.28	76.70	79.84	77.74	57.18	94.60
OBPE (This paper)	<b>55.09</b>	<b>55.37</b>	<b>50.01</b>	<b>75.05</b>	<b>82.94</b>	<b>80.31</b>	<b>65.57</b>	<b>95.09</b>

Table 5: Zero-shot performance of models in the Skewed-12 setting of Table 2 on same four tasks as Table 4. OBPE shows gains here too. Detailed numbers in Table 11 of Supplementary. Section 4.2 has further discussion.

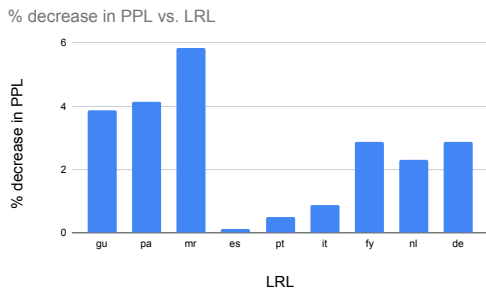


Figure 1: Percentage reduction in Pseudo perplexity (Salazar et al., 2020) for different LRLs as we go from BPE to OBPE vocabulary. (Section 4.2)

sentences drops by 2.6% when we go from the BPE to OBPE vocabulary. More details on this experiment appear in Figure 1.

In order to investigate the reasons behind the OBPE gains, we first inspected the percentage of tokens in the vocabulary that belong to LRLs, HRLs, and in their overlap. We find that with OBPE both LRL tokens and overlapping tokens increase. Either of these could have led to the observed gains. We analyze the effect of each of these factors in the following two sections.

### 4.3 Effect of Token Overlap

We present the impact of token overlap via two sets of experiments: first, a controlled setup where we

	en-es	
	High (es: 1 GB)	Low: (es: 20K)
NER	-1.4	-11.7
XNLI	0.7	-1.3
	hi-mr	
	High (mr: 110K)	Low (mr: 20K)
NER	-12.2	-41.6
TC	-2.7	-41.3
POS	-6.6	-7.8

Table 6: Drop in Accuracy of Zero-shot transfer when we synthetically reduce token overlap to zero. Transfer is from English (en) as HRL to Spanish (es) and from Hindi (hi) as HRL to Marathi (mr) in two settings: (1) High where es, mr have sizes comparable to the HRL and (2) Low where their sizes are only 20K. Token overlap is important in the low-resource and related language setting (Section 4.3)

synthetically vary the fraction of overlap and second where we measure correlation between overlap and gains of OBPE on the data as-is.

For the controlled setup we follow (K et al., 2020) for synthetically controlling the amount of overlap between HRL and LRL. We trained a bilingual model between Hindi (HRL 160K) and Marathi (LRL 20K) — two closely related languages in the Indo-Aryan family. To find the set of overlapping tokens between Hindi and Marathi, we first run OBPE on Hindi-Marathi language pair to generate a vocabulary and label all tokens present

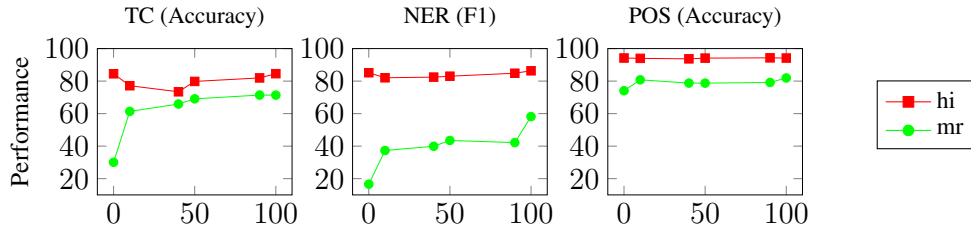


Figure 2: Zero-shot performance vs Overlap of models trained on unicode shifted HRL data to simulate increasing overlap between HRL (SynthHindi) and LRL (mr). Performance is measured on three tasks: Text Classification (Accuracy), NER (F1) and POS (Accuracy). On TC and NER observe the huge drop in LRL accuracy as we decrease overlap from 100 down to 0. Further discussions in Section 4.3.

in both languages as *overlapping tokens*. We then incrementally sample 10%, 40%, 50%, 90% of the tokens from this set. We shift the Unicode of the entire Hindi monolingual data except the set of sampled tokens so that there are no overlapping tokens between Hindi (hi) and Marathi (mr) monolingual data other than the sampled tokens. Let us call this Hindi data **SynthHindi**. We then run OBPE on SynthHindi-Marathi language pair to generate a vocabulary to pretrain the model. The task-specific Hindi data is also converted to SynthHindi during fine-tuning and testing of the model.

Figure 2 shows results with increasing overlap. We observe increasing gains in LRL accuracy as we go from no overlap to full overlap on all three tasks. NER accuracy increases from 17% to 58% for the LRL (mr) even while the HRL (hi) accuracy stays unchanged. For TC we observe similar gains. For POS, even without token overlap, we get good cross-lingual transfer because POS tags are more driven by structural similarity, and Hindi and Marathi follow similar structure.

Our results contradict the conclusions of (K et al., 2020) which claimed that token overlap is unimportant for cross-lingual transfer. However, there are two key differences with our setting: (1) unlike (K et al., 2020), we explore low-resource settings, and (2) except for English-Spanish, the other language pairs they considered are not linguistically related. To explain the importance of both these factors, in Table 6 we present accuracy of English-Spanish in a simulated low-resource setting where we sample 20K Spanish documents and 160K English documents. Also, we repeat our Hindi-Marathi experiments where Marathi is not low-resource. We observe that (1) Spanish as LRL benefits significantly on overlap with English. (2) Marathi gains from token overlap with Hindi even in the high resource setting.

Thus, we conclude that as long as languages are related, token overlap is important and the benefit from overlap is higher in the low resource setting.

**Overlap Vs Gain: Real data setup** We further substantiate our hypothesis that the shared tokens across languages favoured by OBPE enable transfer of supervision from HRL to LRL via statistics on real-data. In Table 9 we show the Pearson product-moment correlation coefficient between overlap gain and performance gain within LRLs of the same family and task. We get a high positive correlation coefficient, with an average of 0.644.

#### 4.4 Effect of Increased LRL representation

We next investigate the impact of increased representation of LRL tokens in the vocabulary. OBPE increases LRL representation by favoring overlapping tokens, but LRL tokens can also be increased by just over-sampling LRL documents. We train another BALANCED12 model but with further over-sampling LRLs with exponentiation factor of 0.5 instead of 0.7. We observe in Figure 8 that this increases LRL fraction but reduces HRL tokens in the vocabulary. Table 7 also shows the comparison of zero-shot transfer accuracy with over-sampled BPE against over-sampled OBPE. We find that OBPE even with default exponentiation factor achieves highest LRL gains, whereas aggressively over-sampled BPE hurts HRL accuracy. Within the same sampling setting, OBPE is better than corresponding BPE.

#### 4.5 Ablation study

We conducted experiments for different values of  $p$  that controls the amount of overlap in the generalized mean function (Equation (5)). Figure 3 and Table 14 show the results for various  $p$ . Setting  $p = 1$  gives the original BPE algorithm. Setting  $p = 0, -1$  gives geometric and harmonic mean respectively, setting  $p = -\infty$  gives minimum. We



Method	LRL Performance ( $\uparrow$ )				HRL Performance ( $\uparrow$ )			
	NER	TC	XNLI	POS	NER	TC	XNLI	POS
BPE	64.5	65.5	52.1	84.6	83.3	<b>82.1</b>	62.7	<b>95.2</b>
+overSample	64.4	67.6	52.1	84.6	82.4	82.0	62.0	95.2
OBPE	<b>65.7</b>	<b>68.0</b>	<b>54.0</b>	<b>85.3</b>	<b>84.0</b>	81.9	<b>66.3</b>	95.1
+overSample	64.6	67.9	53.5	85.1	82.7	81.7	65.7	94.8

Table 7: Zero-shot performance of models in the same setting as Table 4 but comparing default sampling with oversampling (exponentiation factor  $S=0.5$ ). Note, even if BPE\_overSample improves LRL somewhat, it causes HRL to drop. OBPE with default sampling is best for both LRLs and HRLs. Also OBPE\_overSampled is better than BPE\_overSampled (Section 4.4).

Lang family	Task	Pearson Correlation
Indo-Aryan	NER	0.835
	POS	0.690
West Germanic	NER	0.387
	POS	0.348
Romance	NER	0.946
	POS	0.595

Table 9: Correlation coefficient between performance gain and overlap gain within languages in a family for various tasks. (Section 4.3).

compare the task-specific results for different values of  $p$  as shown in Table 14 and find that the gains we obtain are highest in the  $p = -\infty$  (minimum) setting (Figure 3).

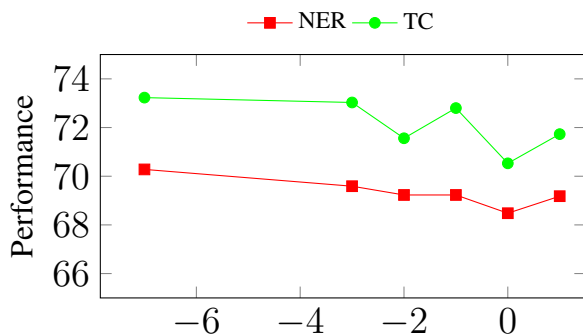


Figure 3: Zero-shot LRL performance of models in the same setting as Table 4 for different values of  $p$  evaluated on NER and Text Classification. Best results at  $p = -\infty$ . (Section 4.5)

We also experiment with  $\alpha = 0.7$ , and find that for most languages the results were not better than our default  $\alpha = 0.5$ .

## 5 Conclusion

In this paper, we address the problem of cross-lingual transfer from HRLs to LRLs by exploiting

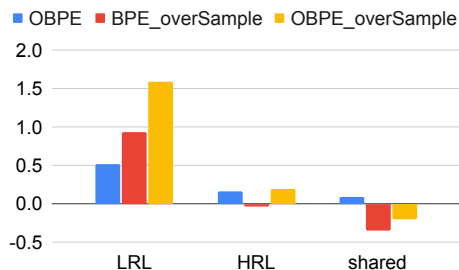


Table 8: Percentage rise over BPE in representation of LRL, HRL and Shared (percentage of tokens shared between HRL and LRL weighted by frequency) in vocabulary generated by OBPE and BPE\_overSample and OBPE\_overSample (Section 4.4).

relatedness among them. We focus on lexical overlap during the vocabulary generation stage of multilingual pre-training. We propose Overlap BPE (OBPE), a simple yet effective modification to the BPE algorithm, which chooses a vocabulary that maximizes overlap across languages. OBPE encodes input corpora compactly while also balancing the trade-off between cross-lingual subword sharing and language-specific vocabularies. We focus on three sets of closely related languages from diverse language families. Our experiments provide evidence that OBPE is effective in leveraging overlap across related languages to improve LRL performance. In contrast to prior work, through controlled experiments on the amount of token overlap between two related HRL-LRL language pairs, we establish that token overlap is important when a LRL is paired with a related HRL.

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## A Appendix

### A.1 Examples of Token Overlap within Language Families

Table 10 shows examples of overlapping tokens within three different language families, and Figure 4 shows a real example of how OBPE chooses shared tokens.

### A.2 Limitations

- Our approach is expected to improve cross-lingual transfer from HRL to LRL only when the HRL and LRL are related linguistically since it relies on the presence of lexically overlapping tokens
- It requires the transliteration of LRL data to the script of its related HRL if LRL does not have the same script.

### A.3 Potential risks

Language models may amplify bias in data and also introduce new ones. Multilingual models explored in the paper are not immune to such issues. Detecting such biases and mitigating them is a topic of ongoing research. We are hopeful that our focus on better representation of LRLs in the vocabulary is a step towards more inclusive models.

	Tokens
Hindi	नियुक्ति(Niyukti), नियुक्त(Niyukta)
Punjabi	नियुकत(Niyukata), नियुकतीਆ(Niyukatiaa), नियुकती(Niyukati)
Marathi	नियुक्ति(Niyukti), नियुक्त(Niyukta)
Gujarati	नियुक्ति(Niyukti), नियुक्त(Niyukta)
BPE vocab	नियुक्ति(Niyukti), नियुक्त(Niyukta)
OBPE vocab	नियुक्ति(Niyukti), नियुक्त(Niyukta), नियुक्(Niyuk)

Figure 4: Similar meaning words with shared root forms across related Indo-Aryan languages. BPE vocabulary does not capture the tokens corresponding to Punjabi as it is a LRL and will thus tokenize Niyukata into multiple tokens which do not capture its meaning whereas Niyukata when tokenized by OBPE tokenizer will contain Niyuk which captures most of the meaning of the token Niyukata whose representation will be learnt when pretraining using Punjabi monolingual data

### A.4 Replicability

BERT configuration parameters used in our experiments are as follows:

```
"attention_probs_dropout_prob": 0.1, "hidden_act": "gelu", "hidden_dropout_prob": 0.1, "hidden_size": 768, "initializer_range": 0.02, "intermediate_size": 3072, "max_position_embeddings": 512, "num_attention_heads": 12, "num_hidden_layers": 12, "type_vocab_size": 2, "vocab_size": 30000
```

All the task-specific fine-tuning experiments are done using GPUs on Google Colaboratory where each fine-tuning experiment requires 2 GPU hours.

### A.5 License

Tatoeba data, GLUE data, Wikipedia dumps use the Creative Commons licenses. TDIL data used for Indic languages uses Research license type and Xtreme dataset uses Apache License 2.0. To the best of our knowledge, the use of scientific artifacts in this work is consistent with their intended use.



Indo-Aryan	Hindi: <a href="#">Vaapariyo</a> , Marathi: <a href="#">Vaapartat</a> , Punjabi: <a href="#">Vaaparan</a> , Gujarati: <a href="#">Vaaparvana</a> Hindi: <a href="#">Jaate</a> , Marathi: <a href="#">Jaoon</a> , Punjabi: <a href="#">Jaana</a> , Gujarati: <a href="#">Jaao</a>
West-Germanic	English: <a href="#">Category</a> , German: <a href="#">Kategorie</a> , Dutch: <a href="#">Categorie</a> , Western Frisian: <a href="#">Kategory</a> English: <a href="#">University</a> , German: <a href="#">Universitaten</a> , Dutch: <a href="#">Universiteit</a> , Western Frisian: <a href="#">Universiteiten</a>
Romance	French: <a href="#">Association</a> , Spanish: <a href="#">Asociacion</a> , Portuguese: <a href="#">Associacao</a> , Italian: <a href="#">Associazione</a> French: <a href="#">Certifie</a> , Spanish: <a href="#">Certificar</a> , Portuguese: <a href="#">Certificado</a> , Italian: <a href="#">Certificato</a>

Table 10: Lexically overlapping tokens with similar meanings across four languages in each of three families. OBPE, our proposed method, exploits such meaning-preserving overlap among related languages to induce vocabulary for multilingual learning.

Lang	hi	mr	pa	gu	en	de	nl	fy	fr	es	pt	it	LRL	HRL
	HRL				HRL				HRL				avg	avg
NER														
BPE	83.66	45.03	25.85	24.25	75.94	52.42	62.83	62.63	85.75	70.53	68.34	64.34	52.91	81.78
CV	83.83	47.67	32.69	33.43	72.35	46.89	55.13	57.88	83.34	71.78	66.45	62.61	52.73	79.84
OBPE	85.92	47.55	26.05	32.79	77.15	52.72	62.87	65.55	85.76	73.35	70.25	64.69	55.09	82.94
TC														
BPE	75.8	51.46	49.88	51.9	88.27	49.5			76.05	55.64			51.68	80.04
CV	76.46	54.37	55.49	56.33	81.94	51.5			74.81	54.31			54.40	77.74
OBPE	76.58	55.38	53.98	54.06	88.3	57.85			76.06	55.59			55.37	80.31
POS														
BPE	93.96	74.84	59.34	65.87	94.81	69.18	74.96		96.33	86.66	84.67	82.81	74.79	95.03
CV	93.67	77.68	71.28	75.81	94.1	67.68	72.75		96.04	84.33	82.44	81.65	76.70	94.60
OBPE	94.11	75.46	58.84	68.5	94.94	68.1	75.18		96.22	86.54	84.3	83.46	75.05	95.09
XNLI														
BPE					67.05	45.51			62.87	51.62			48.57	64.96
CV					54.87	39.87			59.48	48.68			44.28	57.18
OBPE					67.71	47.33			63.43	52.69			50.01	65.57

Table 11: Zero-shot performance of models in the Skewed-12 setting trained on 9 LRL and 3 HRL languages. Performance is measured on four tasks: NER (F1), Text Classification (Accuracy), POS (Accuracy), and XNLI (Accuracy). For all metrics, higher is better . Zero-shot transfer to LRL improves without hurting HRL accuracy. Averages results across HRLs and LRLs are presented in Table 5. OBPE shows gains here too. Section 4.2 has further discussion.

## A.6 Data bias

We have used standard Wikipedia corpus, and there have been some studies on bias in such corpus.(Hube, 2017)

Lang	hi HRL	mr	pa	gu	en HRL	de	nl	fy	fr HRL	es	pt	it	LRL avg	HRL avg
NER														
BPE	85.49	54.88	75.35	40.5	74.99	53.16	62.91	66.54	84.24	70.14	70.2	63.86	61.95	81.57
OBPE( $\alpha = 0.5$ )	86.59	59.23	76.15	41.84	74.74	56.95	63.19	67.92	83.73	69.99	69.76	64.91	63.33	81.69
OBPE( $\alpha = 0.7$ )	85.99	59.54	75.59	41.37	75.36	54.6	63.43	66.86	83.95	71.77	69.27	66.29	63.19	81.77
TC														
bpe	83.97	68.01	74.24	77.1	88.2	57.6			77.45	53.45			66.08	83.21
OBPE( $\alpha = 0.5$ )	83	71.78	75.21	78.28	88.28	62.41			76.88	54.19			68.37	82.72
OBPE( $\alpha = 0.7$ )	83.56	69.3	74.84	77.09	87.93	57.9			77.11	57.84			67.39	82.87
POS														
bpe	94.14	81.7	86.57	86.86	94.5	69.2	80.39		95.79	88.62	84.8	85.74	82.99	94.81
OBPE( $\alpha = 0.5$ )	94.18	82.79	86.63	86.5	94.6	70.53	79.49		95.94	88.79	86.62	86.41	83.47	94.91
OBPE( $\alpha = 0.7$ )	94.1	81.56	87.04	86.55	94.38	70.67	79.99		96.17	89.8	87.77	86.19	83.70	94.88
XNLI														
bpe					65.79	48.3			63.21	54.93			51.62	64.50
OBPE( $\alpha = 0.5$ )					66.77	50.84			66.77	53.27			52.06	66.77
OBPE( $\alpha = 0.7$ )					66.37	48.54			63.57	54.85			51.70	64.97

Table 12: Zero-shot performance of three different models each trained on 3 LRLs and 1 HRL in the respective families 2 in the BALANCED-4 setting . Performance is measured on four tasks: NER (F1), Text Classification (Accuracy), POS (Accuracy), and XNLI (Accuracy). For all metrics, higher is better . Zero-shot transfer to LRL improves without hurting HRL accuracy. OBPE shows gains here too. Languages in Romance family show some improvements in  $\alpha = 0.7$  setting as compared to  $\alpha = 0.5$ . (Section sec:ablation)

	% overlap retained	En-Es				Hi-Mr			
		High		Low		High		Low	
		es	en	es	hi	mr	hi	mr	
NER	100	72.3	75.1	63.4	85.9	55.6	86.3	58.2	
	0	70.9	67.7	51.7	82.7	43.4	85.1	16.6	
TC	100		88.2	63.7	84.4	75.1	84.6	71.4	
	0		82.6	53.8	78.9	72.4	84.5	30.1	
POS	100		94.7	82.9	94.2	83.3	94.2	81.9	
	0		92.8	60.4	94.0	76.7	94.2	74.1	
XNLI	100	61.9	66.6	55.2					
	0	62.6	61.5	53.9					

Table 13: Accuracy of Zero-shot transfer from English (En) as HRL to Spanish (Es) and from Hindi(Hi) as HRL to Marathi(Mr) in two settings: (1) High where Es,Mr have sizes comparable to the HRL and (2) Low where their sizes are only 20K. As the percentage of overlapping tokens retained is decreased from 100% to 0%, the accuracy drops but the drop is higher in the low-resource setting. Task-specific accuracy numbers in first column(En-Es-High-es) have been taken from (K et al., 2020). Table 6 contains the reduction in accuracy on decreasing overlap from 100% to 0 % i.e. the difference between the rows corresponding to 100% and 0%

Lang	hi	mr	pa	gu	en	de	nl	fy	fr	es	pt	it	avg
Method(p)	NER												
OBPE(1)=BPE	86.57	59.71	69.71	41.89	77.42	60.14	67.87	69.73	85.79	72.96	71.02	67.31	69.18
OBPE(0)	87.29	61.86	67.21	41.46	76.08	59.50	67.30	66.86	86.02	69.80	70.89	67.54	68.48
OBPE(-1)	86.67	64.19	72.38	39.93	77.17	58.25	67.09	69.86	85.83	72.99	70.43	66.02	69.23
OBPE(-2)	86.17	60.91	67.30	44.43	76.47	59.66	67.13	70.03	85.25	75.02	71.82	66.53	69.23
OBPE(-3)	87.14	62.68	72.25	44.73	77.24	61.41	67.38	69.87	86.15	69.82	71.06	65.37	69.59
OBPE(-∞)	87.09	62.96	72.17	44.25	77.93	60.44	68.65	70.23	86.92	74.14	72.55	66.05	70.28
BPE-dp	85.54	62.64	71.46	39.75	75.51	59.29	67.76	70.42	84.15	67.43	68.82	67.74	68.38
TokComp	86.43	61.12	72.82	45.88	76.57	55.25	65.28	67.85	84.22	71.04	68.87	66.00	68.44
CV	84.27	55.66	43.37	50.19	74.99	53.51	65.36	65.39	84.20	73.05	66.16	63.49	64.97
Bsamp	84.68	59.73	67.31	40.62	76.76	61.34	67.29	71.80	85.89	73.71	71.20	66.69	68.92
Osamp	84.71	63.22	67.82	42.03	77.83	62.35	68.08	71.59	85.50	69.16	70.06	66.70	69.09
	TC												
OBPE(1)=BPE	80.35	61.45	69.00	72.32	88.63	62.27			77.23	62.58			71.73
OBPE(0)	80.11	64.07	68.26	70.48	87.61	54.96			76.53	62.23			70.53
OBPE(-1)	80.00	64.37	69.10	72.10	87.89	66.25			77.33	65.36			72.80
OBPE(-2)	79.21	64.83	68.58	70.41	88.17	65.76			76.78	58.71			71.56
OBPE(-3)	81.00	62.79	68.17	73.20	89.38	68.34			77.50	63.84			73.03
OBPE(-∞)	80.68	68.90	70.03	72.14	87.92	66.05			77.14	63.00			73.23
BPE-dp	79.68	63.45	69.43	70.36	87.39	59.75			76.15	57.76			70.50
TokComp	82.06	67.17	70.42	72.48	88.02	58.47			77.22	60.29			72.02
CV	79.90	61.33	65.68	68.96	87.98	55.79			74.92	57.79			69.04
Bsamp	81.00	65.29	70.97	72.30	88.05	66.11			76.92	63.51			73.02
Osamp	80.11	66.08	70.11	72.38	88.39	66.25			76.57	64.58			73.06
	POS												
OBPE(1)=BPE	94.22	79.60	86.83	86.21	94.91	77.70	82.00		96.47	89.74	87.79	87.27	87.52
OBPE(0)	94.13	76.26	86.53	85.03	94.85	76.09	82.48		96.31	88.78	87.01	86.62	86.74
OBPE(-1)	94.20	79.13	86.23	85.14	94.87	78.22	82.56		96.32	89.62	87.25	87.27	87.34
OBPE(-2)	93.98	81.07	86.54	85.86	94.68	76.80	82.08		96.23	89.14	86.31	86.45	87.19
OBPE(-3)	94.31	79.55	86.67	86.65	95.03	76.34	83.63		96.30	89.97	87.76	88.00	87.66
OBPE(-∞)	94.18	81.55	87.01	86.76	94.98	79.28	82.38		96.40	90.04	88.01	88.21	87.94
BPE-dp	93.26	80.03	86.31	85.23	94.49	77.90	83.07		96.10	90.01	87.84	87.63	87.44
TokComp	93.99	80.38	86.75	86.79	94.79	79.50	84.91		95.80	89.87	87.05	88.70	88.05
CV	93.12	74.82	84.62	81.56	94.28	74.74	79.41		96.01	87.51	85.52	85.27	85.17
Bsamp	94.3	77.81	86.35	85.68	94.93	77.2	82.94		96.34	89.93	88.05	88.54	87.46
Osamp	94.01	81.22	86.66	86.36	94.35	76.99	82.93		96.04	89.75	88.24	88.43	87.73
	XNLI												
OBPE(1)=BPE					64.35	50.36			61.06	53.77			57.39
OBPE(0)					64.33	49.06			59.96	54.71			57.02
OBPE(-1)					64.35	48.62			61.40	53.51			56.97
OBPE(-2)					65.05	50.36			64.45	55.31			58.79
OBPE(-3)					67.86	50.64			64.85	57.11			60.11
OBPE(-∞)					67.41	50.76			65.13	57.29			60.15
BPE-dp					64.31	50.16			63.17	55.17			58.20
TokComp					67.98	53.05			64.21	54.83			60.02
CV					65.19	47.43			63.83	51.16			56.90
Bsamp					63.41	51.02			60.58	53.09			57.03
Osamp					67.13	50.38			64.25	56.64			59.60

Table 14: Zero-shot performance of models in the Balanced-12 setting trained on 9 LRL and 3 HRL languages. Performance is measured on four tasks: NER (F1), Text Classification (Accuracy), POS (Accuracy), and XNLI (Accuracy). For all metrics, higher is better. Zero-shot transfer to LRL improves without hurting HRL accuracy. Averages results across HRLs and LRLs are presented in Table 4. Section 4.2 has further discussion. Table 4 contains the values corresponding to rows BPE, BPE-dp, CV, TokComp, OBPE(-∞) averaged over LRLs and HRLs, Table 7 contains the values corresponding to rows Bsamp, Osamp averaged over LRLs and HRLs, Figure 3 plots the rows corresponding to varying p values. (Section 4.5)