

Available online at www.sciencedirect.com



PHYSICS LETTERS B

Physics Letters B 555 (2003) 33-42

www.elsevier.com/locate/npe

Neutrino decay confronts the SNO data

Abhijit Bandyopadhyay a, Sandhya Choubey b, Srubabati Goswami c

^a Theory Group, Saha Institute of Nuclear Physics, 1/AF, Bidhannagar, Calcutta 700 064, India
 ^b Department of Physics and Astronomy, University of Southampton, Highfield, Southampton S017 1BJ, UK
 ^c Harish-Chandra Research Institute, Chhatnag Road, Jhusi, Allahabad 211 019, India

Received 20 September 2002; received in revised form 8 January 2003; accepted 9 January 2003

Editor: P.V. Landshoff

Abstract

We investigate the status of the neutrino decay solution to the solar neutrino problem in the context of the recent results from Sudbury Neutrino Observatory (SNO). We present the results of global χ^2 -analysis for both two and three generation cases with one of the mass states being allowed to decay and include the effect of both decay and mixing. We find that the Large Mixing Angle (LMA) region which is the currently favoured solution of the solar neutrino problem is affected significantly by decay. We present the allowed areas in the Δm^2 -tan² θ plane for different allowed values of α and examine how these areas change with the inclusion of decay. We obtain bounds on the decay constant α in this region which implies a rest frame life time $\tau_0/m_2 > 8.7 \times 10^{-5}$ s/eV for the unstable neutrino state. We conclude that the arrival of the neutral current results from SNO further disfavors the neutrino decay solution to the solar neutrino problem leaving a very small window for the decay constant α which could still be allowed.

© 2003 Elsevier Science B.V. Open access under CC BY license.

1. Introduction

The comparison of the SNO charged current (CC) measurements with their neutral current (NC) rate establishes oscillations to active neutrino flavor at the 5.3σ level [1]. The inclusion of Super-Kamiokande (SK) electron scattering (ES) rate [2] with SNO confirms transitions to active flavors at more than 5.5σ level. In other words SNO rules out the possibility of having a purely sterile component in the solar neutrino beam at the 5.5σ level. However, presence of sterile components in the beam is not entirely ruled out. Transition to *mixed* states is still allowed with < 32% (65%) sterile mixture at the 1σ (2σ) level [3–5]. One of the scenarios in which one can have a final sterile state is neutrino decay. The aim of this Letter is to investigate the status of the neutrino decay solution to the solar neutrino problem with the incorporation of the SNO data. We deal with both two generation and three generation cases. For the latter we consider three flavor mixing between ν_e , ν_μ and ν_τ with mass eigenstates ν_1 , ν_2 and ν_3 with the assumed mass hierarchy as $m_1^2 < m_2^2 < m_3^2$. The lightest neutrino mass state is assumed to have

E-mail addresses: abhi@theory.saha.ernet.in (A. Bandyopadhyay), sandhya@hep.phys.soton.ac.uk (S. Choubey), sruba@mri.ernet.in (S. Goswami).

States which are a mixture of active as well as sterile components.

lifetime much greater than the Sun–Earth transit time and hence can be taken as stable. Whereas the heavier mass states v_2 and v_3 may be unstable. But the CHOOZ data [6] constrains the mixing matrix element U_{e3} to a very small value which implies very small mixture of the v_3 state to the v_e state produced in Sun. So the instability of the v_3 state has hardly any effect on solar neutrino survival probability, and to study the effect of decay on solar neutrinos for simplicity we can consider only the second mass state v_2 to be unstable.

There are two kinds of models of non-radiative decays of neutrinos:

- If neutrinos are Dirac particles one has the decay channel $v_2 \to \bar{v}_{1R} + \phi$, where \bar{v}_{1R} is a right handed singlet and ϕ is an iso-singlet scaler [7]. Thus all the final state particles are sterile.
- If neutrinos are Majorana particles, the decay mode is $v_2 \to \bar{v}_1 + J$, where \bar{v}_1 interacts as a \bar{v}_e with a probability $|U_{e1}|^2$ and J is a Majoron [8].

In both scenarios the rest frame lifetime of v_2 is given by [9]

$$\tau_0 = \frac{16\pi}{g^2} \frac{m_2 (1 + m_1/m_2)^{-2}}{\Delta m^2},\tag{1}$$

where g is the coupling constant and Δm^2 (= $m_2^2 - m_1^2$) is the mass squared difference between the states involved in the decay process. If a neutrino of energy E decays while traversing a distance L then the decay term $\exp(-\alpha L/E)$ gives the fraction of neutrinos that decay. α is the decay constant and is related to τ_0 as $\alpha = m_2/\tau_0$.

For the Sun–Earth distance of 1.5×10^{11} m, and for a typical neutrino energy of 10 MeV one starts getting appreciable decay for $\alpha \sim 10^{-12}$ eV². For lower values of α the exp($-\alpha L/E$) term goes to 1 signifying no decay while for $\alpha > 10^{-10}$ eV² the exponential term goes to zero signifying complete decay of the unstable neutrinos. Assuming $m_2 \gg m_1$ Eq. (1) can be written as

$$g^2 \Delta m^2 \sim 16\pi \alpha. \tag{2}$$

If we now incorporate the bound $g^2 < 4.5 \times 10^{-5}$ as obtained from K decay modes [10] we get the bound $\Delta m^2 > 10^6 \alpha$. This gives the range $\Delta m^2 \gtrsim 10^{-6}$ eV² for which we can have appreciable decay.

Neutrino decay in the context of the solar neutrino problem has been considered earlier in [7,8,11] and more recently in [12–14]. After the declaration of the SNO CC data last year [15], bounds on the decay constant α have been obtained from the data on total rates [16] as well as from SK spectrum data [17]. However, with the declaration of the recent SNO neutral current results [1] we expect to have a better handle on the sterile admixture in the solar neutrino beam and hence tighter constraints on the decay constant α . The statistical analysis for the two-generation oscillation solution for stable neutrinos with the global solar neutrino data including the recent results of the SNO experiment can be found in [3,18,19]. In this Letter we consider the possibility for unstable neutrino states and do a combined global statistical analysis of the solar neutrino data including the total rates from the Cl and Ga experiments [20], the zenith-angle recoil energy spectrum from SK [2] and the combined (CC + ES + NC) daynight energy spectrum from SNO [1]. We do our analysis for both two and three generation scenarios. We include the results of the CHOOZ experiment [6] in our three generation analysis.

In Section 2 we briefly present the survival probability for the solar neutrinos with one of the components unstable. In Section 3 we first find the constraints on α coming from the global solar neutrino data within a two-generation framework. We argue that decay of solar neutrinos is largely disfavored as a result of the inclusion of the SNO day–night spectrum. We next extend our analysis to include the third neutrino flavor and present bounds on α , Δm_{21}^2 and $\tan^2\theta_{21}$ for different allowed values of θ_{13} , from a χ^2 analysis which includes both the global solar neutrino data as well as the CHOOZ data. We end with conclusions in Section 4.

2. Formalism

The three-generation mixing matrix relating the mass and flavour eigenstates are given as

$$U = R_{23}R_{13}R_{12}$$

$$= \begin{pmatrix} c_{13}c_{12} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - s_{23}s_{13}c_{12} & c_{23}c_{12} - s_{23}s_{13}s_{12} & s_{23}c_{13} \\ s_{23}s_{12} - s_{13}c_{23}c_{12} & -s_{23}c_{12} - s_{13}s_{12}c_{23} & c_{23}c_{13} \end{pmatrix},$$
(3)

where we neglect the CP violation phases.

Allowing for the possibility of decay of the second mass eigenstate the probability of getting a neutrino of flavour f starting from an initial electron neutrino flavour in sun is²

$$\begin{split} P_{ef} &= a_{e1}^{\odot^2} \big| A_{1f}^{\oplus} \big|^2 + a_{e2}^{\odot^2} |A_{2f}|^2 e^{-\alpha (L - R_{\odot})/E} + a_{e3}^{\odot^2} \big| A_{3f}^{\oplus} \big|^2 \\ &+ 2 a_{e1}^{\odot} a_{e2}^{\odot} e^{-\alpha (L - R_{\odot})/2E} \operatorname{Re} \big[A_{1f}^{\oplus} A_{2f}^{\oplus *} e^{i(E_2 - E_1)(L - R_{\odot})} e^{i(\phi_{2,\odot} - \phi_{1,\odot})} \big], \end{split} \tag{4}$$

where E_i is the energy of the mass eigenstate i, E is the average energy of the neutrino beam— $E_i = p + m_i^2/2p$, the momentum p = E in the ultra-relativistic limit and is taken to be the same for all the components, α is the decay constant, E is the distance from the center of the Sun, E0 is the radius of the Sun, E0 are the phases that arise due to evolution of E1 th mass eigenstate as moves from its point of creation inside the Sun to the surface and E1 is the amplitude of an electron state to be in the mass eigenstate E2 at the surface of the Sun [22]

$$a_{ei}^{\odot 2} = \sum_{j=1,2,3} X_{ij} U_{je}^{\odot 2},\tag{5}$$

where X_{ij} denotes the non-adiabatic jump probability between the ith and jth states inside the Sun and U_{je}^{\odot} denotes the mixing matrix element between the flavour state v_e and the mass eigenstate v_j in Sun. A_{if}^{\oplus} denote the $v_i \rightarrow v_f$ transition amplitudes inside the Earth. We evaluate these amplitudes numerically by assuming the Earth to consist of two constant density slabs [22]. It can be shown that the square bracketed term containing the phases averages out to zero in the range of Δm^2 in which we are interested [23]. For further details of the calculation of the survival probability we refer to [22].

In the two-generation limit including Earth matter effects and decay, the probability of observing the electron neutrinos created in the Sun can be expressed as [13]

$$P_{ee} = P_{ee}^{\text{day}} + \frac{(\sin^2 \theta - P_{2e})(P_{ee}^{\text{day}} + e^{-2\alpha(L - R_{\odot})/E}(P_{ee}^{\text{day}} - 1))}{\cos^2 \theta - \sin^2 \theta e^{-2\alpha(L - R_{\odot})/E}},$$
(6)

where P_{2e} is the transition probability of $\nu_2 \to \nu_e$ at the detector while $P_{ee}^{\rm day}$ is the day-time survival probability when the solar neutrinos do not cross the Earth. Thus $P_{ee}^{\rm day}$ has no Earth matter effects but includes the matter effects inside the Sun and is given by [13]

$$P_{ee}^{\text{day}} = \cos^2 \theta \left[P_J \sin^2 \theta_M + (1 - P_J) \cos^2 \theta_M \right] + \sin^2 \theta \left[(1 - P_J) \sin^2 \theta_M + \cos^2 \theta_M P_J \right] e^{-2\alpha (L - R_{\odot})/E}, \tag{7}$$

where P_J is the non-adiabatic level jumping probability between the two mass eigenstates in the Sun, for which we use the standard expression from [24] and θ_M is the matter mixing angle inside the Sun given by

$$\tan 2\theta_M = \frac{\Delta m^2 \sin 2\theta}{\Delta m^2 \cos 2\theta - 2\sqrt{2} G_F n_e E}.$$
 (8)

² For a rigorous derivation of the probability for the decay plus oscillation scenario see [21].

 n_e being the ambient electron density, E the neutrino energy, and $\Delta m^2 \ (= m_2^2 - m_1^2)$ the mass squared difference in vacuum.

From Eq. (7) we note that the decay term appears with a $\sin^2 \theta$ and is therefore appreciable only for large enough θ . Thus we expect the effect of decay to be maximum in the LMA region. This can also be understood as follows. The ν_e are produced mostly as ν_2 in the solar core. In the LMA region the neutrinos move adiabatically through the Sun and emerge as ν_2 which eventually decays. For the SMA region on the other hand P_J is non-zero and ν_e produced as ν_2 cross over to ν_1 at the resonance and come out as a ν_1 from the solar surface. Since ν_1 is stable, decay does not affect this region.

3. Analysis of data and results

3.1. Bounds from two-generation analysis

First we use the standard χ^2 minimisation procedure and determine the χ^2_{min} and the best-fit values of the oscillation and decay parameters, in a two flavor mixing scenario. Details of our statistical analysis procedure, including the definition of the χ^2 and the correlated error matrix are given in Appendix A. We incorporate the total rate in Cl and Ga, the zenith-angle spectrum data of SK and the SNO day–night spectrum. We find that the global best-fit³ comes in the LMA region with the decay constant $\alpha=0$ and $\tan^2\theta=0.41$, $\Delta m^2=6.06\times 10^{-5}$ eV² [25].

In Fig. 1 we plot the $\Delta\chi^2$ (= $\chi^2 - \chi^2_{min}$) for the two generation neutrino decay scenario, against the decay constant α , keeping Δm^2 and $\tan^2\theta$ free. The figure shows that the fit becomes worse with increasing value of the decay constant. We remind the reader that neutrino decay is important only for LMA and for each value of α on this curve the minimum χ^2 comes with Δm^2 and $\tan^2\theta$ in the LMA region. The inclusion of the SNO data in the global solar neutrino analysis improves the fit in the LMA region for stable neutrinos. Hence for small values of α where neutrinos can be taken as almost stable, the inclusion of the SNO data gives a better fit. However, as α increases the neutrino decay leads to more sterile components in the final state—which is disfavoured by the SNO/SK combination and the fit worsens with SNO included. As is seen from Fig. 1 the global solar neutrino data put an upper bound on the decay constant— α < 7.55 × 10⁻¹² eV² at 99% C.L., when Δm^2 and θ are allowed to take on any value. Before the declaration of the SNO results the bound on α from combined analysis of Cl, Ga and SK data was α < 3.5 × 10⁻¹¹ eV² [13]. Thus the inclusion of the recent SNO results have further tightened the noose on the fraction of neutrinos decaying on their way from the Sun to Earth and neutrino decay is now barely allowed.

In Fig. 2 we plot the allowed areas in the Δm^2 -tan² θ plane for different allowed values of the decay constant α for a two flavor scenario and with global data including SNO. The figure shows that the allowed area in the LMA region is reduced as α increases. As α increases the spectral distortion increases and the effect is more for higher (lower) values of $\tan^2 \theta$ (Δm^2) [13]. Since both the SK as well as the SNO spectra are consistent with no energy distortion, these regions get disallowed with increasing α . Spectral distortion due to decay is less for the high Δm^2 . However, these values for the Δm^2 are now disfavored at more than 3σ by SNO since the values for the ⁸B flux required to explain the suppression in SK and SNO CC measurements are much lower than those consistent with the SNO NC observation. In addition the low energy neutrinos relevant for Ga experiment decay more making the fit to the total rates worse.

³ The bounds that we give here and subsequently apply to the decay model where both final states are sterile. In the Majoron decay model the final state $\bar{\nu}_e$ can interact in the SK/SNO detectors. However, there is an energy degradation and the best-fit values do not change significantly [12]. An interesting possibility where the absolute mass scales of the two neutrino states are approximately degenerate and hence the daughter $\bar{\nu}_e$ is not degraded in energy is considered recently in [17].

⁴ See [3,18,19,25] for recent global analyses and [26,27] for earlier ones.

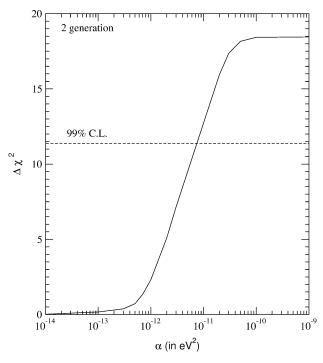


Fig. 1. $\Delta \chi^2$ (= $\chi^2 - \chi^2_{min}$) vs. decay constant α , for two-generations. Also shown is the 99% C.L. limit for three-parameters.

As discussed earlier, for small values of mixing angles the fraction of the decaying component in the ν_e beam $(\sim \sin^2 \theta)$ being very small decay does not have much effect. Hence no new feature is introduced in the SMA region because of decay and it remains disallowed by the global data. On the other hand, in the LOW region though mixing is large, due to small Δm^2 any appreciable decay over the Sun–Earth distance is not obtained, if the bound on the coupling constant from K-decay [10] is to be accounted for. Therefore, LOW region in the parameter space remains unaffected by the unstable ν_2 state, and we do not show it explicitly in Fig. 2.

3.2. Bounds from three-generation analysis

Next we investigate the impact of the unstable ν_2 mass state on the three flavor oscillation scenario with $\Delta m_{21}^2 = \Delta m_{\odot}^2$ and $\Delta m_{31}^2 = \Delta m_{\rm CHOOZ}^2 \simeq \Delta m_{\rm atm}^2 = \Delta m_{32}^2$. For the three generation case the χ^2 is defined as

$$\chi^2 = \chi_{\text{solar}}^2 + \chi_{\text{CHOOZ}}^2 \tag{9}$$

The $\chi^2_{\rm solar}$ is defined in Appendix A while for the expression of $\chi^2_{\rm CHOOZ}$ we refer the reader to [22]. In Fig. 3 we plot the $\Delta\chi^2$ (= $\chi^2 - \chi^2_{\rm min}$) vs. α for various fixed values of θ_{13} allowing the other parameters to take arbitrary values. Δm^2_{31} is varied within the range [1.5–6.0] \times 10⁻³ eV² as obtained from a combined analysis of atmospheric and CHOOZ data [28,29].⁵ This figure indicates the allowed range of α for a fixed θ_{13} . As θ_{13} increases the contribution from $\chi^2_{\rm CHOOZ}$ increases shifting the plots upwards. Consequently the curve corresponding to higher $\tan^2\theta_{13}$ crosses the 99% C.L. limit at a lower α and a more stringent bound is obtained as compared to smaller $\tan^2\theta_{13}$ cases.

⁵ The range of Δm_{31}^2 allowed at 99% C.L. from the combined analysis of final SK + K2K data is [2.3–3.1] × 10⁻³ eV² [30]. However, the values of Δm_{31}^2 that we use are still allowed at the 3σ level.

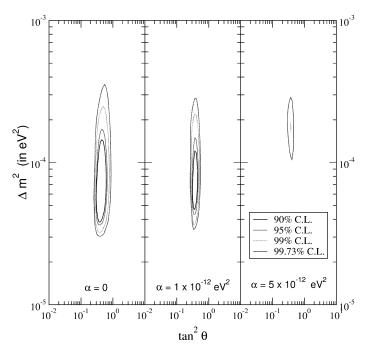


Fig. 2. The 90, 95, 99 and 99.73% C.L. allowed area from the two-generation global analysis of the total rates in Cl and Ga, the SK zenith angle energy spectrum data and the SNO day–night spectrum in presence of decay and oscillation. The C.L. contours are for $\Delta\chi^2$ corresponding to three parameters.

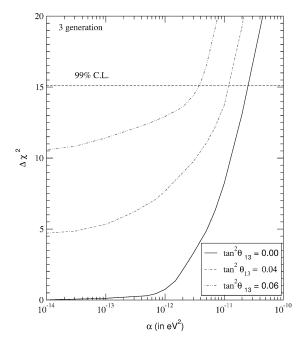


Fig. 3. The $\Delta \chi^2 (= \chi^2 - \chi^2_{min})$ vs. decay constant α for the three generation case for various fixed values of θ_{13} . The other parameters are allowed to take any value.

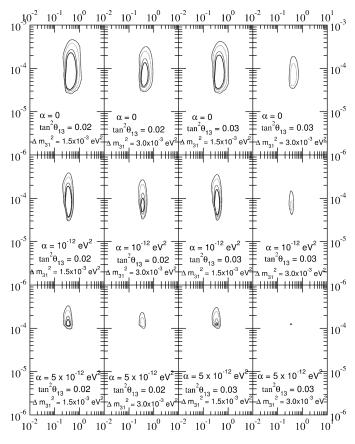


Fig. 4. The 90, 95, 99 and 99.73% C.L. allowed area from the three-generation analysis of the global data in presence of decay and oscillation.

In Fig. 4 we plot the allowed areas in the $\tan^2\theta_{12}$ – Δm_{21}^2 plane for different sets of values of $\tan^2\theta_{13}$ and Δm_{31}^2 at different values of α . For fixed values of $\tan^2\theta_{13}$ and Δm_{31}^2 the allowed area decreases with increasing α because of increased spectral distortion and transition of the solar neutrinos to sterile components. At any given α the allowed area shrinks with the increase of $\tan^2\theta_{13}$ and Δm_{31}^2 . This is again an effect of the CHOOZ data.

4. Conclusions

In this Letter we have done a global χ^2 analysis of the solar neutrino data assuming neutrino decay. We incorporate the full SNO (CC + ES + NC) day–night spectrum data. We present results for both two and three generation scenarios. We find that the best fit is obtained in the LMA region with the decay constant α zero, i.e., for the no decay case. We had pointed earlier [12,13] that the decay scenario was in conflict with the data on total rates because it suppresses low energy neutrinos more than the high energy ones. However, decay also predicts distortion of the neutrino energy spectrum and presence of sterile components in the resultant neutrino beam, both of which are severely disfavored by the recent results from SNO and SK. For the two generation case the bound at 99% C.L. on α that one gets after including the SNO data is $\alpha \le 7.55 \times 10^{-12} \text{ eV}^2$. This corresponds to a rest frame lifetime $\tau_0/m_2 > 8.7 \times 10^{-5} \text{ s/eV}$. This is consistent with astrophysics and cosmology. The effect of decay is not important in the SMA region because the decaying fraction in the solar ν_e beam goes as $\sin^2 \theta$ and this region remains disallowed. There is no change in the allowed areas in the LOW region also because of Eq. (2) and the

bounds on the coupling constant from K decays which restricts $\Delta m^2 \gtrsim 10^{-6} \text{ eV}^2$ and decay over the Sun–Earth distance does not take place in the LOW region. The three generation analysis gives stronger bounds on α for non-zero θ_{13} . In conclusion, the inclusion of the recent SNO data severely constrains decay of the solar neutrinos such that they are largely disfavored. However, non-zero values of α remain allowed at the 99% C.L.

Note added

The long-baseline reactor neutrino experiment KamLAND has released its first data very recently [31]. This experiment has provided the first confirmational evidence for the LMA solution to the solar neutrino problem and is completely consistent with the global solar neutrino data [32,33]. For the values of the decay parameter considered in this Letter, there would be almost no effect on the neutrinos at KamLAND baselines, which on average is about 180 km. Thus the KamLAND results are not expected to be affected at all by the presence of an unstable component in the neutrino beam. However, when combined with the global solar neutrino data in presence of decay, KamLAND could have an impact in reducing the allowed zone in the neutrino parameter space. In particular, KamLAND may disfavor the values of Δm^2 which allow larger values of the decay constant α . But the statistical errors involved in the KamLAND data are still large and even though the allowed areas in the Δm^2 -tan² θ plane does get constricted by KamLAND, the allowed zones are still large enough and should not change the results presented in this Letter in any major way. With better statistics KamLAND may further tighten the constraints on the presence of unstable neutrinos [34].

Appendix A. The statistical analysis of the global solar data

We use the data on total rate from the Cl experiment, the combined rate from the Ga experiments (SAGE + GALLEX + GNO), the 1496 day data on the SK zenith angle energy spectrum and the combined SNO day–night spectrum data. We define the χ^2 function in the "covariance" approach as

$$\chi^2 = \sum_{i,j=1}^{N} \left(R_i^{\text{expt}} - R_i^{\text{theory}} \right) \left(\sigma_{ij}^2 \right)^{-1} \left(R_j^{\text{expt}} - R_j^{\text{theory}} \right), \tag{A.1}$$

where N is the number of data points (2+44+34=80) in our case) and $(\sigma_{ij}^2)^{-1}$ is the inverse of the covariance matrix, containing the squares of the correlated and uncorrelated experimental and theoretical errors. The only correlated error between the total rates of Cl and Ga, the SK zenith-energy spectrum and the SNO day-night spectrum data is the theoretical uncertainty in the 8B flux. However, we choose to keep the 8B flux normalization f_B a free parameter in the theory, to be fixed by the neutral current contribution to the SNO spectrum. We can then block diagonalise the covariance matrix and write the χ^2 as a sum of χ^2 for the rates, the SK spectrum and SNO spectrum.

$$\chi^2 = \chi_{\text{rates}}^2 + \chi_{\text{SKspec}}^2 + \chi_{\text{SNOspec}}^2. \tag{A.2}$$

For χ^2_{rates} we use $R_{\text{Cl}}^{\text{expt}} = 2.56 \pm 0.23$ SNU and $R_{\text{Ga}}^{\text{expt}} = 70.8 \pm 4.4$ SNU. The details of the theoretical errors and their correlations that we use can be found in [26,35].

For the 44 bin SK zenith angle energy spectra we use the data and experimental errors given in [2]. SK divides it is systematic errors into "uncorrelated" and "correlated" systematic errors. We take the "uncorrelated" systematic errors to be uncorrelated in energy but fully correlated in zenith angle. The "correlated" systematic errors, which are fully correlated in energy and zenith angle, include the error in the 8B spectrum shape, the error in the energy resolution function and the error in the absolute energy scale. For each set of theoretical values for Δm^2 , $\tan^2 \theta$

and α we evaluate these systematic errors taking into account the relative signs between the different errors [18]. Finally we take an overall extra systematic error of 2.75% fully correlated in all the bins [2].

Since it is not yet possible to identify the ES, CC and NC events separately in SNO, the SNO Collaboration have made available their results as a combined CC + ES + NC data in 17 day and 17 night energy bins. For the null oscillation case they do give the CC and NC (and ES) rates [1] but firstly these rates would slightly change with the distortion of the ⁸B neutrino spectrum from the Sun and secondly they are highly correlated. They work very well for studying theories with little or no energy distortion such as the LMA and LOW MSW solutions if the (anti)correlations between the CC and NC rates are taken into account and can be used to study the impact of the NC rate of SNO on the oscillation parameter space [3]. They can also be used to give insight into the ⁸B flux and it is suppression by analysing the SK and SNO CC and NC data in a model independent way [3]. However, for theories like neutrino decay where we expect large spectral distortions they cannot be used. Hence we analyse the full day–night spectrum data in this Letter by adding contributions from CC, ES and NC and comparing with the experimental results given in [1]. For the correlated spectrum errors and the construction of the covariance matrix we follow the method of "forward fitting" of the SNO Collaboration detailed in [36].

References

- Q.R. Ahmad, et al., SNO Collaboration, Phys. Rev. Lett. 89 (2002) 011301, nucl-ex/0204008;
 Q.R. Ahmad, et al., SNO Collaboration, Phys. Rev. Lett. 89 (2002) 011302, nucl-ex/0204009.
- [2] S. Fukuda, et al., Super-Kamiokande Collaboration, Phys. Lett. B 539 (2002) 179, hep-ex/0205075.
- [3] A. Bandyopadhyay, S. Choubey, S. Goswami, D.P. Roy, Phys. Lett. B 540 (2002) 14, hep-ph/0204286.
- [4] J.N. Bahcall, M.C. Gonzalez-Garcia, C. Pena-Garay, hep-ph/0204194.
- [5] M. Maltoni, T. Schwetz, M.A. Tortola, J.W. Valle, hep-ph/0207227;M. Maltoni, T. Schwetz, M.A. Tortola, J.W. Valle, hep-ph/0207157.
- [6] M. Apollonio, et al., CHOOZ Collaboration, Phys. Lett. B 466 (1999) 415, hep-ex/9907037;
 M. Apollonio, et al., CHOOZ Collaboration, Phys. Lett. B 420 (1998) 397, hep-ex/9711002.
- [7] A. Acker, S. Pakvasa, S.F. Tuan, S.P. Rosen, Phys. Rev. D 43 (1991) 3083.
- [8] A. Acker, A. Joshipura, S. Pakvasa, Phys. Lett. B 285 (1992) 371.
- [9] A. Acker, S. Pakvasa, Phys. Lett. B 320 (1994) 320, hep-ph/9310207.
- [10] V. Barger, W.Y. Keung, S. Pakvasa, Phys. Lett. B 192 (1987) 460.
- [11] R.S. Raghavan, X.G. He, S. Pakvasa, Phys. Rev. D 38 (1988) 1317.
- [12] S. Choubey, S. Goswami, D. Majumdar, Phys. Lett. B 484 (2000) 73, hep-ph/0004193.
- [13] A. Bandyopadhyay, S. Choubey, S. Goswami, Phys. Rev. D 63 (2001) 113019, hep-ph/0101273.
- [14] C.-K. Chou, M. Cho, Phys. Scr. 64 (2001) 197.
- [15] Q.R. Ahmad, et al., SNO Collaboration, Phys. Rev. Lett. 87 (2001) 071301, nucl-ex/0106015.
- [16] A.S. Joshipura, E. Masso, S. Mohanty, hep-ph/0203181.
- [17] J.F. Beacom, N.F. Bell, Phys. Rev. D 65 (2002) 113009, hep-ph/0204111.
- [18] G.L. Fogli, E. Lisi, A. Marrone, D. Montanino, A. Palazzo, hep-ph/0206162.
- J.N. Bahcall, M.C. Gonzalez-Garcia, C. Pena-Garay, JHEP 0207 (2002) 054, hep-ph/0204314;
 P.C. de Holanda, A.Y. Smirnov, hep-ph/0205241;
 - A. Strumia, C. Cattadori, N. Ferrari, F. Vissani, Phys. Lett. B 541 (2002) 327, hep-ph/0205261.
- [20] B.T. Cleveland, et al., Astrophys. J. 496 (1998) 505;
 - J.N. Abdurashitov, et al., SAGE Collaboration, astro-ph/0204245;
 - W. Hampel, et al., GALLEX Collaboration, Phys. Lett. B 447 (1999) 127;
 - E. Bellotti, Talk at Gran Sasso National Laboratories, Italy, May 17, 2002;
 - T. Kirsten, Talk at Neutrino 2002, Munich, Germany, May 2002.
- [21] M. Lindner, T. Ohlsson, W. Winter, Nucl. Phys. B 607 (2001) 326, hep-ph/0103170.
- [22] A. Bandyopadhyay, S. Choubey, S. Goswami, K. Kar, Phys. Rev. D 65 (2002) 073031, hep-ph/0110307.
- [23] A.S. Dighe, Q.Y. Liu, A.Y. Smirnov, hep-ph/9903329.
- [24] S.T. Petcov, Phys. Lett. B 200 (1988) 373.
- [25] S. Choubey, A. Bandyopadhyay, S. Goswami, D.P. Roy, hep-ph/0209222.
- [26] A. Bandyopadhyay, S. Choubey, S. Goswami, K. Kar, Phys. Lett. B 519 (2001) 83, hep-ph/0106264;
 - S. Choubey, S. Goswami, D.P. Roy, Phys. Rev. D 65 (2002) 073001, hep-ph/0109017;

- S. Choubey, S. Goswami, K. Kar, H.M. Antia, S.M. Chitre, Phys. Rev. D 64 (2001) 113001, hep-ph/0106168.
- [27] G.L. Fogli, E. Lisi, D. Montanino, A. Palazzo, Phys. Rev. D 64 (2001) 093007, hep-ph/0106247;
 - J.N. Bahcall, M.C. Gonzalez-Garcia, C. Pena-Garay, JHEP 0108 (2001) 014, hep-ph/0106258;
 - P.I. Krastev, A.Y. Smirnov, Phys. Rev. D 65 (2002) 073022, hep-ph/0108177;
 - M.V. Garzelli, C. Giunti, JHEP 0112 (2001) 017, hep-ph/0108191.
- [28] M.C. Gonzalez-Garcia, M. Maltoni, C. Pena-Garay, J.W. Valle, Phys. Rev. D 63 (2001) 033005, hep-ph/0009350.
- [29] G.L. Fogli, E. Lisi, A. Marrone, D. Montanino, A. Palazzo, hep-ph/0104221.
- [30] G.L. Fogli, G. Lettera, E. Lisi, A. Marrone, A. Palazzo, A. Rotunno, hep-ph/0208026.
- [31] KamLAND Collaboration, hep-ex/0212021.
- [32] A. Bandyopadhyay, S. Choubey, R. Gandhi, S. Goswami, D.P. Roy, hep-ph/0212146.
- [33] J.N. Bahcall, M.C. Gonzalez-Garcia, C. Pena-Garay, hep-ph/0212147;
 - G.L. Fogli, E. Lisi, A. Marrone, D. Montanino, A. Palazzo, A.M. Rotunno, hep-ph/0212127;
 - P.C. de Holanda, A.Y. Smirnov, hep-ph/0212270;
 - M. Maltoni, T. Schwetz, J.W. Valle, hep-ph/0212129;
 - V. Barger, D. Marfatia, hep-ph/0212126.
- [34] A. Bandyopadhyay, S. Choubey, S. Goswami, in preparation.
- [35] S. Goswami, D. Majumdar, A. Raychaudhuri, Phys. Rev. D 63 (2001) 013003, hep-ph/0003163;
 S. Choubey, S. Goswami, N. Gupta, D.P. Roy, Phys. Rev. D 64 (2001) 053002, hep-ph/0103318.
- [36] SNO Collaboration, HOWTO use the SNO Solar Neutrino Spectral data at http://owl.phy.queensu.ca/sno/prlwebpage/.